

# Package ‘fabCI’

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**Title** FAB Confidence Intervals

**Version** 0.2

**Description** Frequentist assisted by Bayes (FAB) confidence interval construction. See 'Adaptive multigroup confidence intervals with constant coverage' by Yu and Hoff <[DOI:10.1093/biomet/asy009](https://doi.org/10.1093/biomet/asy009)> and 'Exact adaptive confidence intervals for linear regression coefficients' by Hoff and Yu <[DOI:10.1214/18-EJS1517](https://doi.org/10.1214/18-EJS1517)>.

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## R topics documented:

ebayes_est . . . . .	2
fabregCI . . . . .	3
fabtCI . . . . .	3
fabtzCI . . . . .	4
fabzCI . . . . .	5
hhetmodel . . . . .	6
hhommodel . . . . .	7
multifabCI . . . . .	8
multifabCIIhom . . . . .	9
radon . . . . .	10
sfabz . . . . .	10
umauregCI . . . . .	11

**ebayes\_est***Empirical Bayes estimation of hyperparameters***Description**

Compute empirical Bayes estimates of the error variance and distribution of the regression coefficients.

**Usage**

```
ebayes_est(y, X, emu = FALSE, dof = min(50, round(0.5 * (dim(X)[1] - dim(X)[2]))))
```

**Arguments**

<code>y</code>	a numeric vector of data
<code>X</code>	a design matrix
<code>emu</code>	(logical) estimate mean of coefficient (TRUE) or assume it is zero (FALSE)?
<code>dof</code>	degrees of freedom to use for the t-quantiles (the remainder go to adaptive estimation of the prior)

**Details**

This function computes the adaptive FAB confidence interval for each coefficient in a linear regression model.

**Value**

A list (s,sigma2,tau2,mu) where

1. `s` an estimate of the error standard deviation
2. `sigma2` an estimate of the error variance, independent of `s`
3. `tau2` an estimate of the coefficient variance, independent of `s`
4. `mu` an estimate of the coefficient mean, independent of `s`

**Author(s)**

Peter Hoff

fabregCI

*FAB regression coefficient intervals***Description**

Compute the adaptive FAB t-intervals for the coefficients of a regression model.

**Usage**

```
fabregCI(y, X, alpha = 0.05, dof = min(50, round(0.5 * (dim(X)[1] - dim(X)[2]))), verbose = TRUE)
```

**Arguments**

y	a numeric vector of data
X	a design matrix
alpha	the type I error rate, so 1-alpha is the coverage rate
dof	degrees of freedom to use for the t-quantiles (the remainder go to adaptive estimation of the prior)
verbose	logical, print progress or not

**Details**

This function computes the adaptive FAB confidence interval for each coefficient in a linear regression model.

**Value**

A matrix where each row corresponds to the interval and OLS estimate of a coefficient.

**Author(s)**

Peter Hoff

fabtCI

*FAB t-interval***Description**

Computation of a 1-alpha FAB t-interval

**Usage**

```
fabtCI(y, psi = c(0, 100, 1, 2), alpha = 0.05)
```

## Arguments

<i>y</i>	a numeric vector with at least two non-missing values
<i>psi</i>	a length-four vector of hyperparameters for the prior
<i>alpha</i>	the type I error rate, so 1-alpha is the coverage rate

## Details

A FAB interval is the "frequentist" interval procedure that is Bayes optimal: It minimizes the prior expected interval width among all interval procedures with exact 1-alpha frequentist coverage. This function computes the FAB t-interval for the mean of a normal population with an unknown variance, given a user-specified prior distribution determined by *psi*. The prior is that the population mean and variance are independently distributed as normal and inverse-gamma random variables. Referring to the elements of *psi* as *mu*, *t2*, *s20*, *nu0*, the prior is determined as follows:

1. *mu* is the prior expectation of the mean
2. *t2* is the prior variance of the mean
3. the population variance is  $\text{inverse-gamma}(\nu_0/2, \nu_0 s^2/2)$

## Author(s)

Peter Hoff

## Examples

```
y<-rnorm(10)
fabtCI(y,c(0,10,1,5))
fabtCI(y,c(0,1/10,1,5))
fabtCI(y,c(2,10,1,5))
fabtCI(y,c(0,1/10,1,5))
```

**fabtzCI**

*z-optimal FAB t-interval*

## Description

Computation of a 1-alpha FAB t-interval using z-optimal spending function

## Usage

```
fabtzCI(y, s, dof, alpha = 0.05, psi = list(mu = 0, tau2 = 1e+05, sigma2 =
1))
```

**Arguments**

y	a numeric scalar, a normally distributed statistic
s	a numeric scalar, the standard error of y
dof	positive integer, degrees of freedom for s
alpha	the type I error rate, so 1-alpha is the coverage rate
psi	a list of parameters for the spending function, including <ol style="list-style-type: none"> <li>1. mu, the prior expectation of <math>E[y]</math></li> <li>2. tau2, the prior variance of <math>E[y]</math></li> <li>3. sigma2 the variance of y</li> </ol>

**Examples**

```
n<-10
y<-rnorm(n)
fabzCI(mean(y),sqrt(var(y)/n),n-1)
t.test(y)$conf.int
```

fabzCI

*FAB z-interval***Description**

Computation of a 1-alpha FAB z-interval

**Usage**

```
fabzCI(y, mu, t2, s2, alpha = 0.05)
```

**Arguments**

y	a numeric scalar
mu	a numeric scalar
t2	a positive numeric scalar
s2	a positive numeric scalar
alpha	the type I error rate, so 1-alpha is the coverage rate

**Details**

A FAB interval is the "frequentist" interval procedure that is Bayes optimal: It minimizes the prior expected interval width among all interval procedures with exact 1-alpha frequentist coverage. This function computes the FAB z-interval for the mean of a normal population with an known variance, given a user-specified prior distribution determined by `psi`. The prior is that the population mean is normally distributed. Referring to the elements of `psi` as `mu`, `t2`, `s2`, the prior and population variance are determined as follows:

1. mu is the prior expectation of the mean
2. t2 is the prior variance of the mean
3. s2 is the population variance

**Author(s)**

Peter Hoff

**Examples**

```
y<-0
fabzCI(y,0,10,1)
fabzCI(y,0,1/10,1)
fabzCI(y,2,10,1)
fabzCI(y,0,1/10,1)
```

**hhetmodel**

*Hierarchical heteroscedastic model estimates*

**Description**

Estimate across-group heterogeneity of means and variances

**Usage**

```
hhetmodel(y, g)
```

**Arguments**

<i>y</i>	a numeric vector of data
<i>g</i>	a group membership vector, of the same length as <i>y</i>

**Details**

This function estimates parameters in a hierarchical model for normally distributed groups, where the across-group model for means is normal and the across group model for variances is inverse-gamma.

**Value**

A vector (mu,t2,s20,nu0), where

1. mu is the mean of the group means
2. t2 is the variance of the group means
3. the the distribution of group variances is inverse-gamma(nu0/2,nu0 s20/2)

**Author(s)**

Peter Hoff

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**hhommodel***Hierarchical homoscedastic model estimates*

---

**Description**

Estimate across-group heterogeneity of means

**Usage**

```
hhommodel(y, g, group, p1)
```

**Arguments**

y	a numeric vector of data
g	a group membership vector, of the same length as y
group	the index of the group
p1	number of groups used to pool sample variance

**Details**

This function estimates parameters in a hierarchical model for normally distributed groups, where the across-group model for means is normal and the variance is the same across groups.

**Value**

A vector (s2,df,muw,t2w,s2w), where

1. s2 is the pooled variance
2. df is the degree of freedom of the t-quantiles
3. muw is the estimate mean of the group means
4. t2w is the estimate variance of the group means
5. s2w is the estimate within-group variance

**Author(s)**

Chaoyu Yu

**multifabCI***Multigroup FAB t-intervals***Description**

Computation of 1-alpha FAB t-intervals for heteroscedastic multigroup data.

**Usage**

```
multifabCI(y, g, alpha = 0.05)
```

**Arguments**

- |       |  |
|-------|--|
| y     | a numeric vector of data                               |
| g     | a group membership vector, of the same length as y     |
| alpha | the type I error rate, so 1-alpha is the coverage rate |

**Details**

For each group j, this function computes an estimate of the parameters in a hierarchical model for means and variances from data other than group j, and uses this information to construct a FAB t-interval for group j. These intervals have 1-alpha frequentist coverage, assuming within-group normality.

**Author(s)**

Peter Hoff

**Examples**

```
## -- simulated data
p<-10 ; n<-10
y<-rnorm(n*p) ; g<-rep(1:p,n)

## -- more interesting data takes longer
# data(radon) ; y<-radon[,2] ; g<-radon[,1]

## -- FAB t-intervals
FCI<-multifabCI(y,g)

## -- UMAU t-intervals
ybar<-tapply(y,g,mean) ; ssd<-tapply(y,g,sd) ; n<-table(g)
qtn<-cbind( qt(.025,n-1), qt(.975,n-1) )
UCI<-sweep(sweep(qtn,1,ssd/sqrt(n),"*"),1,ybar,"+")

mean( (UCI[,2]-UCI[,1])/(FCI[,2]-FCI[,1]) , na.rm=TRUE)
```

---

multifabCIhom*Multigroup FAB t-intervals for the homoscedastic model*

---

**Description**

Computation of 1-alpha FAB t-intervals for homoscedastic multigroup data.

**Usage**

```
multifabCIhom(y, g, alpha = 0.05, prop = 0.5)
```

**Arguments**

y	a numeric vector of data
g	a group membership vector, of the same length as y
alpha	the type I error rate, so 1-alpha is the coverage rate
prop	the proportion of groups to obtain the sample variance estimate

**Details**

For each group j, this function computes an estimate of the parameters in a hierarchical model for means using data from other groups, and uses this information to construct a FAB t-interval for group j. These intervals have 1-alpha frequentist coverage, assuming within-group normality and that the within group variance is the same across groups.

**Author(s)**

Chaoyu Yu

**Examples**

```
## -- simulate the data
mu = 0; sigma2 = 10; tau2 = 1; p = 100;
theta = rnorm(p,mu,sqrt(tau2))
ns = round(runif(p,2,18))
Y=c()
for(i in 1:p){
  d2 = rnorm(ns[i],theta[i],sqrt(sigma2))
  d1 = rep(i,ns[i])
  d = cbind(d1,d2)
  Y = rbind(Y,d)}
y = Y[,2]
g = Y[,1]

## -- FAB t-intervals
FCI = multifabCIhom(y,g)

## -- UMAU t-intervals
```

```
ybar<-tapply(y,g,mean) ; ssd<-tapply(y,g,sd) ; n<-table(g)
qtn<-cbind( qt(.025,n-1), qt(.975,n-1) )
UCI<-sweep(sweep(qtn,1,ssd/sqrt(n),"*"),1,ybar,"+")
mean( (UCI[,2]-UCI[,1])/(FCI[,2]-FCI[,1]) , na.rm=TRUE)
```

**radon***Minnesota Radon Dataset***Description**

Radon levels in 919 homes from 85 Minnesota counties

**Usage**

```
data(radon)
```

**Format**

A numeric matrix

**Source**

<http://www.stat.columbia.edu/~gelman/arm/software/>

**sfabz***Bayes-optimal spending function***Description**

Compute Bayes optimal spending function

**Usage**

```
sfabz(theta, psi, alpha = 0.05)
```

**Arguments**

- |       |  |
|-------|--|
| theta | value of theta being tested  |
| psi   | a list of parameters for the spending function, including <ol style="list-style-type: none"> <li>1. mu, the prior expectation of E[y]</li> <li>2. tau2, the prior variance of E[y]</li> <li>3. sigma2 the variance of y</li> </ol> |
| alpha | level of test  |

**Details**

This function computes the value of  $s$  that minimizes the acceptance probability of a biased level-alpha test for a normal population with known variance, under a specified prior predictive distribution.

**Author(s)**

Peter Hoff

---

umauregCI

*UMAU regression coefficient intervals*

---

**Description**

Compute the usual t-intervals for the coefficients of a regression model

**Usage**

```
umauregCI(y, X, alpha = 0.05)
```

**Arguments**

- |       |  |
|-------|--|
| y     | a numeric vector of data                               |
| X     | a design matrix  |
| alpha | the type I error rate, so 1-alpha is the coverage rate |

**Details**

This function computes the 'usual' uniformly most accurate unbiased confidence interval for each coefficient in a linear regression model.

**Value**

A matrix where each row corresponds to the interval and OLS estimate of a coefficient.

**Author(s)**

Peter Hoff

# Index

- \* **datasets**
  - radon, 10
- \* **htest**
  - fabtCI, 3
  - fabzCI, 5
  - hhetmodel, 6
  - hhommodel, 7
  - multifabCI, 8
  - multifabCIhom, 9
- ebayes\_est, 2
- fabregCI, 3
- fabtCI, 3
- fabtzCI, 4
- fabzCI, 5
- hhetmodel, 6
- hhommodel, 7
- multifabCI, 8
- multifabCIhom, 9
- radon, 10
- sfabz, 10
- umauregCI, 11