

# Package ‘densityratio’

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**Type** Package

**Title** Distribution Comparison Through Density Ratio Estimation

**Version** 0.2.1

**Description** Fast, flexible and user-friendly tools for distribution comparison through direct density ratio estimation. The estimated density ratio can be used for covariate shift adjustment, outlier-detection, change-point detection, classification and evaluation of synthetic data quality. The package implements multiple non-parametric estimation techniques (unconstrained least-squares importance fitting, ulsif(), Kullback-Leibler importance estimation procedure, kliep(), spectral density ratio estimation, spectral(), kernel mean matching, kmm(), and least-squares hetero-distributional subspace search, lhss()). with automatic tuning of hyperparameters. Helper functions are available for two-sample testing and visualizing the density ratios. For an overview on density ratio estimation, see Sugiyama et al. (2012) <[doi:10.1017/CBO9781139035613](https://doi.org/10.1017/CBO9781139035613)> for a general overview, and the help files for references on the specific estimation techniques.

**License** GPL (>= 3)

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<https://github.com/thomvolker/densityratio>

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**NeedsCompilation** yes

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## Contents

colon	3
create_bivariate_plot	3
create_univariate_plot	4
denominator_data	4
denominator_small	5
distance	5
dr.histogram	6
insurance	8
kernel_gaussian	9
kidiq	9
kliep	10
kmm	11
lhss	13
naive	15
numerator_data	17
numerator_small	17
permute	18
plot_bivariate	19
plot_univariate	20
predict.kliep	22
predict.kmm	23
predict.lhss	24
predict.naivedensityratio	25
predict.spectral	26
predict.ulsf	27
print.kliep	28
print.kmm	29
print.lhss	30
print.naivedensityratio	31
print.spectral	32
print.summary.kliep	33
print.summary.kmm	34
print.summary.lhss	35
print.summary.naivedensityratio	36
print.summary.spectral	37
print.summary.ulsf	38

<i>colon</i>	3
--------------	---

print.ulsif . . . . .	39
spectral . . . . .	40
summary.kliep . . . . .	42
summary.kmm . . . . .	43
summary.lhss . . . . .	44
summary.naivedensityratio . . . . .	46
summary.spectral . . . . .	47
summary.ulsif . . . . .	48
ulsif . . . . .	49

<b>Index</b>	52
--------------	----

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<i>colon</i>	<i>colon</i>
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## Description

Colon cancer data set from princeton, containing 2000 gene expressions from 22 colon tumor tissues and 40 non-tumor tissues. The data is collected by Alon et al. (1999) and can be obtained from [here](#).

## Format

A data.frame with 62 rows and 2001 columns (class variable and 2000 gene expressions).

---

create_bivariate_plot	<i>Bivariate plot</i>
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## Description

Bivariate plot

## Usage

```
create_bivariate_plot(data, ext, vars, logscale, show.sample)
```

## Arguments

<code>data</code>	Data frame with the individual values and density ratio estimates
<code>ext</code>	Data frame with the density ratio estimates and sample indicator
<code>vars</code>	Character vector of variable names to be plotted.
<code>logscale</code>	Logical indicating whether the density ratio should be plotted in log scale. Defaults to TRUE.
<code>show.sample</code>	Logical indicating whether to give different shapes to observations, depending on the sample they come from (numerator or denominator). Defaults to FALSE.

**Value**

Bivariate plot

---

`create_univariate_plot`

*Univariate plot*

---

**Description**

Scatterplot of individual values and density ratio estimates. Used internally in `create_univariate_plot()`

**Usage**

```
create_univariate_plot(data, ext, var, y_lab, sample.facet = TRUE)
```

**Arguments**

<code>data</code>	Data frame with the individual values and density ratio estimates
<code>ext</code>	Data frame with the density ratio estimates and sample indicator
<code>var</code>	Name of the variable to be plotted on the x-axis
<code>y_lab</code>	Name of the y-axis label, typically ("Density Ratio" or "Log Density Ratio")
<code>sample.facet</code>	Logical indicating whether to facet the plot by sample. Default is TRUE.

**Value**

A scatterplot of variable values and density ratio estimates.

---

`denominator_data`

*denominator\_data*

---

**Description**

Simulated data set (see `data-raw/generate-data-densityratio.R`) with five variables that are used in the examples.

**Format**

A data frame with 1000 rows and 5 columns:

- x1** Categorical variable with three categories, 'A', 'B' and 'C'
- x2** Categorical variable with two categories, 'G1' and 'G2'
- x3** Continuous variable (normally distributed given x1 and x2)
- x4** Continuous variable (normally distributed)
- x5** Continuous variable (normally distributed)

---

<i>denominator_small</i>	<i>denominator_small</i>
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---

## Description

Subset of the [denominator\\_data](#) with three variables and 50 observations

## Format

A data frame with 100 rows and 3 columns:

- x1** Continuous variable (normally distributed given x1 and x2)
  - x2** Continuous variable (normally distributed)
  - x3** Continuous variable (normally distributed)
- 

<i>distance</i>	<i>Create a Gram matrix with squared Euclidean distances between observations in the input matrix X and the input matrix Y</i>
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---

## Description

Create a Gram matrix with squared Euclidean distances between observations in the input matrix X and the input matrix Y

## Arguments

- |           |  |
|-----------|--|
| X         | A numeric input matrix   |
| Y         | A numeric input matrix with the same variables as X  |
| intercept | Logical indicating whether an intercept should be added to the estimation procedure. In this case, the first column is an all-zero column (which will be transformed into an all-ones column in the kernel). |

---

dr.histogram      *A histogram of density ratio estimates*

---

### Description

Creates a histogram of the density ratio estimates. Useful to understand the distribution of estimated density ratios in each sample, or compare it among samples. It is the default plotting method for density ratio objects.

### Usage

```
dr.histogram(
  x,
  samples = "both",
  logscale = TRUE,
  binwidth = NULL,
  bins = NULL,
  tol = 0.01,
  ...
)

## S3 method for class 'ulsif'
plot(
  x,
  samples = "both",
  logscale = TRUE,
  binwidth = NULL,
  bins = NULL,
  tol = 0.01,
  ...
)

## S3 method for class 'kliep'
plot(
  x,
  samples = "both",
  logscale = TRUE,
  binwidth = NULL,
  bins = NULL,
  tol = 0.01,
  ...
)

## S3 method for class 'kmm'
plot(
  x,
  samples = "both",
```

```
    logscale = TRUE,
    binwidth = NULL,
    bins = NULL,
    tol = 0.01,
    ...
)

## S3 method for class 'spectral'
plot(
  x,
  samples = "both",
  logscale = TRUE,
  binwidth = NULL,
  bins = NULL,
  tol = 0.01,
  ...
)

## S3 method for class 'lhss'
plot(
  x,
  samples = "both",
  logscale = TRUE,
  binwidth = NULL,
  bins = NULL,
  tol = 0.01,
  ...
)

## S3 method for class 'naivedensityratio'
plot(
  x,
  samples = "both",
  logscale = TRUE,
  binwidth = NULL,
  bins = NULL,
  tol = 0.01,
  ...
)
```

## Arguments

x	Density ratio object created with e.g., <a href="#">klied()</a> , <a href="#">ulsif()</a> , or <a href="#">naive()</a>
samples	Character string indicating whether to plot the 'numerator', 'denominator', or 'both' samples. Default is 'both'.
logscale	Logical indicating whether to plot the density ratio estimates on a log scale. Default is TRUE.
binwidth	Numeric indicating the width of the bins, passed on to ggplot2.

<b>bins</b>	Numeric indicating the number of bins. Overriden by binwidth, and passed on to ggplot2.
<b>tol</b>	Numeric indicating the tolerance: values below this value will be set to the tolerance value, for legibility of the plots
<b>...</b>	Additional arguments passed on to predict().

**Value**

- A histogram of density ratio estimates.

**See Also**

- [ulsif](#) for example usage
- [kliep](#) for example usage
- [kmm](#) for example usage
- [spectral](#) for example usage
- [lhss](#) for example usage
- [naive](#) for example usage

**Description**

Insurance data that is openly available (e.g., on [Kaggle](#)).

**Format**

A data.frame with 1338 rows and 7 columns:

- age** Age of the insured (continuous)
- sex** Sex of the insured (binary)
- bmi** Body mass index of the insured (continuous)
- children** Number of children/dependents covered by the insurance (integer)
- smoker** Whether the insured is a smoker (binary)
- region** The region in which the insured lives (categorical)
- charges** The medical costs billed by the insurance (continuous)

---

kernel_gaussian	Create gaussian kernel gram matrix from distance matrix
-----------------	---

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## Description

Create gaussian kernel gram matrix from distance matrix

## Arguments

dist	A numeric distance matrix
sigma	A scalar with the length-scale parameter

---

kidiq	<i>kidiq</i>
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---

## Description

The kidiq data stems from the National Longitudinal Survey of Youth and is used in Gelman and Hill (2007). The data set contains 434 observations measured on five variables, and is obtained from <https://github.com/jknowles/BDAexampleR>.

## Format

A data.frame with 434 rows and 5 columns

**kid\_score** Child's IQ score (continuous)

**mom\_hs** Whether the mother obtained a high school degree (binary)

**mom\_iq** Mother's IQ score (continuous)

**mom\_work** Whether the mother worked in the first three years of the child's life (1: not in the first three years; 2: in the second or third year; 3: parttime in the first year; 4: fulltime in the first year)

**mom\_age** Mother's age (continuous)

---

klied*Kullback-Leibler importance estimation procedure*

---

## Description

Kullback-Leibler importance estimation procedure

## Usage

```
klied(
  df_numerator,
  df_denominator,
  scale = "numerator",
  nsigma = 10,
  sigma_quantile = NULL,
  sigma = NULL,
  ncenters = 200,
  centers = NULL,
  cv = TRUE,
  nfold = 5,
  epsilon = NULL,
  maxit = 5000,
  progressbar = TRUE
)
```

## Arguments

df_numerator	data.frame with exclusively numeric variables with the numerator samples
df_denominator	data.frame with exclusively numeric variables with the denominator samples (must have the same variables as df_denominator)
scale	"numerator", "denominator", or NULL, indicating whether to standardize each numeric variable according to the numerator means and standard deviations, the denominator means and standard deviations, or apply no standardization at all.
nsigma	Integer indicating the number of sigma values (bandwidth parameter of the Gaussian kernel gram matrix) to use in cross-validation.
sigma_quantile	NULL or numeric vector with probabilities to calculate the quantiles of the distance matrix to obtain sigma values. If NULL, nsigma values between 0.25 and 0.75 are used.
sigma	NULL or a scalar value to determine the bandwidth of the Gaussian kernel gram matrix. If NULL, nsigma values between 0.25 and 0.75 are used.
ncenters	Maximum number of Gaussian centers in the kernel gram matrix. Defaults to all numerator samples.
centers	Option to specify the Gaussian samples manually.
cv	Logical indicating whether or not to do cross-validation

nfold	Number of cross-validation folds used in order to calculate the optimal sigma value (default is 5-fold cv).
epsilon	Numeric scalar or vector with the learning rate for the gradient-ascent procedure. If a vector, all values are used as the learning rate. By default, $10^{[-5:-1]}$ is used.
maxit	Maximum number of iterations for the optimization scheme.
progressbar	Logical indicating whether or not to display a progressbar.

### Value

klied-object, containing all information to calculate the density ratio using optimal sigma and optimal weights.

### References

Sugiyama, M., Suzuki, T., Nakajima, S., Kashima, H., Von Bünnau, P., & Kawanabe, M. (2008). Direct importance estimation for covariate shift adaptation. Annals of the Institute of Statistical Mathematics 60, 699-746. Doi: <https://doi.org/10.1007/s10463-008-0197-x>.

### Examples

```
set.seed(123)
# Fit model
dr <- klied(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
klied(numerator_small, denominator_small,
      nsigma = 1, ncenters = 100, nfold = 10,
      epsilon = 10^{[-5:-2]}, maxit = 500)
```

### Description

Kernel mean matching approach to density ratio estimation

## Usage

```
kmm(
  df_numerator,
  df_denominator,
  scale = "numerator",
  constrained = FALSE,
  nsigma = 10,
  sigma_quantile = NULL,
  sigma = NULL,
  ncenters = 200,
  centers = NULL,
  cv = TRUE,
  nfold = 5,
  parallel = FALSE,
  nthreads = NULL,
  progressbar = TRUE,
  osqp_settings = NULL,
  cluster = NULL
)
```

## Arguments

<code>df_numerator</code>	<code>data.frame</code> with exclusively numeric variables with the numerator samples
<code>df_denominator</code>	<code>data.frame</code> with exclusively numeric variables with the denominator samples (must have the same variables as <code>df_denominator</code> )
<code>scale</code>	" <code>numerator</code> ", " <code>denominator</code> ", or <code>NULL</code> , indicating whether to standardize each numeric variable according to the numerator means and standard deviations, the denominator means and standard deviations, or apply no standardization at all.
<code>constrained</code>	logical equals <code>FALSE</code> to use unconstrained optimization, <code>TRUE</code> to use constrained optimization. Defaults to <code>FALSE</code> .
<code>nsigma</code>	Integer indicating the number of sigma values (bandwidth parameter of the Gaussian kernel gram matrix) to use in cross-validation.
<code>sigma_quantile</code>	<code>NULL</code> or numeric vector with probabilities to calculate the quantiles of the distance matrix to obtain sigma values. If <code>NULL</code> , <code>nsigma</code> values between <code>0.25</code> and <code>0.75</code> are used.
<code>sigma</code>	<code>NULL</code> or a scalar value to determine the bandwidth of the Gaussian kernel gram matrix. If <code>NULL</code> , <code>nsigma</code> values between <code>0.25</code> and <code>0.75</code> are used.
<code>ncenters</code>	Maximum number of Gaussian centers in the kernel gram matrix. Defaults to all numerator samples.
<code>centers</code>	Option to specify the Gaussian samples manually.
<code>cv</code>	Logical indicating whether or not to do cross-validation
<code>nfold</code>	Number of cross-validation folds used in order to calculate the optimal <code>sigma</code> value (default is 5-fold <code>cv</code> ).
<code>parallel</code>	logical indicating whether to use parallel processing in the cross-validation scheme.

nthreads	NULL or integer indicating the number of threads to use for parallel processing. If parallel processing is enabled, it defaults to the number of available threads minus one.
progressbar	Logical indicating whether or not to display a progressbar.
osqp_settings	Optional: settings to pass to the osqp solver for constrained optimization.
cluster	Optional: a cluster object to use for parallel processing, see <code>parallel::makeCluster</code> .

### Value

kmm-object, containing all information to calculate the density ratio using optimal sigma and optimal weights.

### References

Huang, J., Smola, A. J., Gretton, A., Borgwardt, K. M., & Schölkopf, B. (2006). Correcting sample selection bias by unlabeled data. In Advances in Neural Information Processing Systems, edited by B. Schölkopf, J. Platt and T. Hoffman. Available from <https://proceedings.neurips.cc/paper/2006/hash/a2186aa7c086b46ad4e8bf81e2a3a19b-Abstract.html>.

### Examples

```
set.seed(123)
# Fit model
dr <- kmm(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kmm(numerator_small, denominator_small,
     nsigma = 5, ncenters = 100, nfold = 10,
     constrained = TRUE)
```

### Description

Least-squares heterodistributional subspace search

## Usage

```
lhss(
  df_numerator,
  df_denominator,
  m = NULL,
  intercept = TRUE,
  scale = "numerator",
  nsigma = 10,
  sigma_quantile = NULL,
  sigma = NULL,
  nlambda = 10,
  lambda = NULL,
  ncenters = 200,
  centers = NULL,
  maxit = 200,
  progressbar = TRUE
)
```

## Arguments

<code>df_numerator</code>	<code>data.frame</code> with exclusively numeric variables with the numerator samples
<code>df_denominator</code>	<code>data.frame</code> with exclusively numeric variables with the denominator samples (must have the same variables as <code>df_denominator</code> )
<code>m</code>	Scalar indicating the dimensionality of the reduced subspace
<code>intercept</code>	<code>logical</code> Indicating whether to include an intercept term in the model. Defaults to <code>TRUE</code> .
<code>scale</code>	" <code>numerator</code> ", " <code>denominator</code> ", or <code>NULL</code> , indicating whether to standardize each numeric variable according to the numerator means and standard deviations, the denominator means and standard deviations, or apply no standardization at all.
<code>nsigma</code>	Integer indicating the number of sigma values (bandwidth parameter of the Gaussian kernel gram matrix) to use in cross-validation.
<code>sigma_quantile</code>	<code>NULL</code> or numeric vector with probabilities to calculate the quantiles of the distance matrix to obtain sigma values. If <code>NULL</code> , <code>nsigma</code> values between <code>0.05</code> and <code>0.95</code> are used.
<code>sigma</code>	<code>NULL</code> or a scalar value to determine the bandwidth of the Gaussian kernel gram matrix. If <code>NULL</code> , <code>nsigma</code> values between <code>0.05</code> and <code>0.95</code> are used.
<code>nlambda</code>	Integer indicating the number of <code>lambda</code> values (regularization parameter), by default, <code>lambda</code> is set to <code>10^seq(3, -3, length.out = nlambda)</code> .
<code>lambda</code>	<code>NULL</code> or numeric vector indicating the <code>lambda</code> values to use in cross-validation
<code>ncenters</code>	Maximum number of Gaussian centers in the kernel gram matrix. Defaults to all numerator samples.
<code>centers</code>	Numeric matrix with the same variables as <code>nu</code> and <code>de</code> that are used as Gaussian centers in the kernel Gram matrix. By default, the matrix <code>nu</code> is used as the matrix with Gaussian centers.
<code>maxit</code>	Maximum number of iterations in the updating scheme.
<code>progressbar</code>	<code>Logical</code> indicating whether or not to display a progressbar.

**Value**

lhss-object, containing all information to calculate the density ratio using optimal sigma, optimal lambda and optimal weights.

**References**

Sugiyama, M., Yamada, M., Von Bünnau, P., Suzuki, T., Kanamori, T. & Kawanabe, M. (2011). Direct density-ratio estimation with dimensionality reduction via least-squares hetero-distributional subspace search. *Neural Networks*, 24, 183-198. [doi:10.1016/j.neunet.2010.10.005](https://doi.org/10.1016/j.neunet.2010.10.005).

**Examples**

```
set.seed(123)
# Fit model
dr <- naive(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
naive(numerator_small, denominator_small, m=2, kernel="epanechnikov")
```

naive

*Naive density ratio estimation***Description**

The naive approach creates separate kernel density estimates for the numerator and the denominator samples, and then evaluates their ratio for the denominator samples. For multivariate data, the density ratio is computed after a orthogonal linear transformation, such that the new variables can be treated as independent. To reduce the dimensionality of the PCA solution, one can set the number of components by setting the `m` parameter to an integer value smaller than the number of variables.

**Usage**

```
naive(
  df_numerator,
  df_denominator,
  m = NULL,
  bw = "SJ",
```

```

kernel = "gaussian",
n = 2L^11,
...
)

```

## Arguments

<code>df_numerator</code>	<code>data.frame</code> with exclusively numeric variables with the numerator samples
<code>df_denominator</code>	<code>data.frame</code> with exclusively numeric variables with the denominator samples (must have the same variables as <code>df_denominator</code> )
<code>m</code>	integer Optional parameter to reduce the dimensionality of the data in multi-variate density ratio estimation problems. If missing, the number of variables in the data is used. If set to an integer value smaller than the number of variables, the first <code>m</code> principal components are used to estimate the density ratio. If set to <code>NULL</code> , the square root of the number of variables is used (for consistency with other methods).
<code>bw</code>	the smoothing bandwidth to be used. See <a href="#">stats::density</a> for more information.
<code>kernel</code>	the kernel to be used. See <a href="#">stats::density</a> for more information.
<code>n</code>	integer the number of equally spaced points at which the density is to be estimated. When <code>n &gt; 512</code> , it is rounded up to a power of 2 during the calculations (as fast Fourier transform is used) and the final result is interpolated by <a href="#">stats::approx</a> . So it makes sense to specify <code>n</code> as a power of two.
<code>...</code>	further arguments passed to <a href="#">stats::density</a>

## Value

`naivedensityratio` object

## See Also

[stats::density\(\)](#)

## Examples

```

set.seed(123)
# Fit model
dr <- naive(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))

```

```
# Fit model with custom parameters  
naive(numerator_small, denominator_small, m=2, kernel="epanechnikov")
```

---

*numerator\_data**numerator\_data*

## Description

Simulated data set (see `data-raw/generate-data-densityratio.R`) with five variables that are used in the examples.

## Format

A data frame with 1000 rows and 5 columns:

- x1** Categorical variable with three categories, 'A', 'B' and 'C'
  - x2** Categorical variable with two categories, 'G1' and 'G2'
  - x3** Continuous variable (normally distributed given x1 and x2)
  - x4** Continuous variable (normally distributed given x3)
  - x5** Continuous variable (mixture of two normally distributed variables)
- 

*numerator\_small**numerator\_small*

## Description

Subset of the [numerator\\_data](#) with three variables and 50 observations

## Format

A data frame with 50 rows and 3 columns:

- x1** Continuous variable (normally distributed given x1 and x2)
- x2** Continuous variable (normally distributed given x3)
- x3** Continuous variable (mixture of two normally distributed variables)

permute	<i>Single permutation</i>
---------	---------------------------

## Description

Single permutation  
 Single permutation statistic of `ulsif` object  
 Single permutation statistic of `kliep` object  
 Single permutation statistic of `kmm` object  
 Single permutation statistic of `lhss` object  
 Single permutation statistic of `spectral` object  
 Single permutation statistic of `naivedensityratio` object

## Usage

```
permute(object, ...)

## S3 method for class 'ulsif'
permute(object, stacked, nnu, nde, ...)

## S3 method for class 'kliep'
permute(object, stacked, nnu, nde, min_pred = sqrt(.Machine$double.eps), ...)

## S3 method for class 'kmm'
permute(object, stacked, nnu, nde, ...)

## S3 method for class 'lhss'
permute(object, stacked, nnu, nde, ...)

## S3 method for class 'spectral'
permute(object, stacked, nnu, nde, ...)

## S3 method for class 'naivedensityratio'
permute(object, stacked, nnu, nde, min_pred, max_pred, ...)
```

## Arguments

object	naivedensityratio object
...	Additional arguments to pass through to specific permute functions.
stacked	matrix with stacked numerator and denominator samples
nnu	Scalar with numerator sample size
nde	Scalar with denominator sample size
min_pred	Minimum value of the predicted density ratio
max_pred	Maximum value of the predicted density ratio

**Value**

permutation statistic for a single permutation of the data  
permutation statistic for a single permutation of the data  
permutation statistic for a single permutation of the data  
permutation statistic for a single permutation of the data  
permutation statistic for a single permutation of the data  
permutation statistic for a single permutation of the data  
permutation statistic for a single permutation of the data

---

**plot\_bivariate** *Densityratio in two-dimensional plot*

---

**Description**

Plots a scatterplot of two variables, with densityratio mapped to the colour scale.

**Usage**

```
plot_bivariate(  
  x,  
  vars = NULL,  
  samples = "both",  
  grid = FALSE,  
  logscale = TRUE,  
  show.sample = FALSE,  
  tol = 0.01,  
  ...  
)
```

**Arguments**

x	Density ratio object created with e.g., <a href="#">kliep()</a> , <a href="#">ulsif()</a> , or <a href="#">naive()</a>
vars	Character vector of variable names for which all pairwise bivariate plots are created
samples	Character string indicating whether to plot the 'numerator', 'denominator', or 'both' samples. Default is 'both'.
grid	Logical indicating whether output should be a list of individual plots ("individual"), or one facetted plot with all variables ("assembled"). Defaults to "individual".
logscale	Logical indicating whether to plot the density ratio estimates on a log scale. Default is TRUE.
show.sample	Logical indicating whether to give different shapes to observations, depending on the sample they come from (numerator or denominator). Defaults to FALSE.

**tol** Numeric indicating the tolerance: values below this value will be set to the tolerance value, for legibility of the plots  
**...** Additional arguments passed to the predict() function.

### Value

Bivariate scatter plots of all combinations of variables in vars.

### Examples

```
set.seed(123)
# Fit model
dr <- ulsif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulsif(numerator_small, denominator_small, sigma = 2, lambda = 2)
```

**plot\_univariate** *Scatter plot of density ratios and individual variables*

### Description

A scatter plot showing the relationship between estimated density ratios and individual variables.

### Usage

```
plot_univariate(
  x,
  vars = NULL,
  samples = "both",
  logscale = TRUE,
  grid = FALSE,
  sample.facet = FALSE,
  nrow.panel = NULL,
  tol = 0.01,
  ...
)
```

## Arguments

x	Density ratio object created with e.g., <code>kliexp()</code> , <code>ulsif()</code> , or <code>naive()</code>
vars	Character vector of variable names to be plotted.
samples	Character string indicating whether to plot the 'numerator', 'denominator', or 'both' samples. Default is 'both'.
logscale	Logical indicating whether to plot the density ratio estimates on a log scale. Default is TRUE.
grid	Logical indicating whether output should be a list of individual plots ("individual"), or one faceted plot with all variables ("assembled"). Defaults to "individual".
sample.facet	Logical indicating whether to facet the plot by sample, i.e, showing plots separate for each sample, and side to side. Defaults to FALSE.
nrow.panel	Integer indicating the number of rows in the assembled plot. If NULL, the number of rows is automatically calculated.
tol	Numeric indicating the tolerance: values below this value will be set to the tolerance value, for legibility of the plots
...	Additional arguments passed to the predict() function.

## Value

Scatter plot of density ratios and individual variables.

## Examples

```
set.seed(123)
# Fit model
dr <- ulsif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulsif(numerator_small, denominator_small, sigma = 2, lambda = 2)
```

**predict.kliep***Obtain predicted density ratio values from a kliep object***Description**

Obtain predicted density ratio values from a kliep object

**Usage**

```
## S3 method for class 'kliep'
predict(object, newdata = NULL, sigma = c("sigmaopt", "all"), ...)
```

**Arguments**

object	A kliep object
newdata	Optional matrix new data set to compute the density
sigma	A scalar with the Gaussian kernel width
...	Additional arguments to be passed to the function

**Value**

An array with predicted density ratio values from possibly new data, but otherwise the numerator samples.

**See Also**

[predict](#), [kliep](#)

**Examples**

```
set.seed(123)
# Fit model
dr <- kliep(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kliep(numerator_small, denominator_small,
      nsigma = 1, ncenters = 100, nfold = 10,
      epsilon = 10^{2:-5}, maxit = 500)
```

---

predict.kmm*Obtain predicted density ratio values from a kmm object*

---

## Description

Obtain predicted density ratio values from a kmm object

## Usage

```
## S3 method for class 'kmm'  
predict(object, newdata = NULL, sigma = c("sigmaopt", "all"), ...)
```

## Arguments

object	A kmm object
newdata	Optional matrix new data set to compute the density
sigma	A scalar with the Gaussian kernel width
...	Additional arguments to be passed to the function

## Value

An array with predicted density ratio values from possibly new data, but otherwise the numerator samples.

## See Also

[predict](#), [kmm](#)

## Examples

```
set.seed(123)  
# Fit model  
dr <- kmm(numerator_small, denominator_small)  
# Inspect model object  
dr  
# Obtain summary of model object  
summary(dr)  
# Plot model object  
plot(dr)  
# Plot density ratio for each variable individually  
plot_univariate(dr)  
# Plot density ratio for each pair of variables  
plot_bivariate(dr)  
# Predict density ratio and inspect first 6 predictions  
head(predict(dr))  
# Fit model with custom parameters  
kmm(numerator_small, denominator_small,  
     nsigma = 5, ncenters = 100, nfold = 10,
```

```
constrained = TRUE)
```

**`predict.lhss`***Obtain predicted density ratio values from a lhss object***Description**

Obtain predicted density ratio values from a lhss object

**Usage**

```
## S3 method for class 'lhss'
predict(
  object,
  newdata = NULL,
  sigma = c("sigmaopt", "all"),
  lambda = c("lambdaopt", "all"),
  ...
)
```

**Arguments**

<code>object</code>	A lhss object
<code>newdata</code>	Optional matrix new data set to compute the density
<code>sigma</code>	A scalar with the Gaussian kernel width
<code>lambda</code>	A scalar with the regularization parameter
<code>...</code>	Additional arguments to be passed to the function

**Value**

An array with predicted density ratio values from possibly new data, but otherwise the numerator samples.

**See Also**

[predict](#), [lhss](#)

**Examples**

```
set.seed(123)
# Fit model (minimal example to limit computation time)
dr <- lhss(numerator_small, denominator_small,
            nsigma = 5, nlambda = 3, ncenters = 50, maxit = 100)
# Inspect model object
dr
# Obtain summary of model object
```

```
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
```

---

**predict.naivedensityratio**

*Obtain predicted density ratio values from a naivedensityratio object*

---

**Description**

Obtain predicted density ratio values from a naivedensityratio object

**Usage**

```
## S3 method for class 'naivedensityratio'
predict(object, newdata = NULL, log = FALSE, tol = 1e-06, ...)
```

**Arguments**

object	A naive object
newdata	Optional matrix new data set to compute the density
log	A logical indicating whether to return the log of the density ratio
tol	Minimal density value to avoid numerical issues
...	Additional arguments to be passed to the function

**Value**

An array with predicted density ratio values from possibly new data, but otherwise the numerator samples.

**See Also**

[predict](#), [naive](#)

## Examples

```
set.seed(123)
# Fit model
dr <- naive(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
naive(numerator_small, denominator_small, m=2, kernel="epanechnikov")
```

**predict.spectral**      *Obtain predicted density ratio values from a spectral object*

## Description

Obtain predicted density ratio values from a spectral object

## Usage

```
## S3 method for class 'spectral'
predict(
  object,
  newdata = NULL,
  sigma = c("sigmaopt", "all"),
  m = c("opt", "all"),
  ...
)
```

## Arguments

<code>object</code>	A spectral object
<code>newdata</code>	Optional <code>matrix</code> new data set to compute the density
<code>sigma</code>	A scalar with the Gaussian kernel width
<code>m</code>	integer indicating the dimension of the eigenvector expansion
<code>...</code>	Additional arguments to be passed to the function

**Value**

An array with predicted density ratio values from possibly new data, but otherwise the numerator samples.

**See Also**

[predict](#), [spectral](#)

---

<a href="#">predict.ulif</a>	<i>Obtain predicted density ratio values from a ulif object</i>
------------------------------	---

---

**Description**

Obtain predicted density ratio values from a ulif object

**Usage**

```
## S3 method for class 'ulif'
predict(
  object,
  newdata = NULL,
  sigma = c("sigmaopt", "all"),
  lambda = c("lambdaopt", "all"),
  ...
)
```

**Arguments**

object	A ulif object
newdata	Optional matrix new data set to compute the density
sigma	A scalar with the Gaussian kernel width
lambda	A scalar with the regularization parameter
...	Additional arguments to be passed to the function

**Value**

An array with predicted density ratio values from possibly new data, but otherwise the numerator samples.

**See Also**

[predict](#), [ulif](#)

## Examples

```
set.seed(123)
# Fit model
dr <- ulsif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulsif(numerator_small, denominator_small, sigma = 2, lambda = 2)
```

**print.kliep**

*Print a kliep object*

## Description

Print a kliep object

## Usage

```
## S3 method for class 'kliep'
print(x, digits = max(3L, getOption("digits")) - 3L), ...)
```

## Arguments

- x Object of class kliep.
- digits Number of digits to use when printing the output.
- ... further arguments on how to format the number of digits.

## Value

**invisible** The inputted kliep object.

## See Also

[print, kliep](#)

## Examples

```
set.seed(123)
# Fit model
dr <- kliep(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kliep(numerator_small, denominator_small,
      nsigma = 1, ncenters = 100, nfold = 10,
      epsilon = 10^{2:-5}, maxit = 500)
```

---

**print.kmm**

*Print a kmm object*

---

## Description

Print a kmm object

## Usage

```
## S3 method for class 'kmm'
print(x, digits = max(3L, getOption("digits")) - 3L), ...)
```

## Arguments

- |        |  |
|--------|--|
| x      | Object of class kmm.                                     |
| digits | Number of digits to use when printing the output.        |
| ...    | further arguments on how to format the number of digits. |

## Value

**invisible** The inputted kmm object.

## See Also

[print, kmm](#)

## Examples

```
set.seed(123)
# Fit model
dr <- kmm(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kmm(numerator_small, denominator_small,
     nsigma = 5, ncenters = 100, nfold = 10,
     constrained = TRUE)
```

**print.lhss**

*Print a lhss object*

## Description

Print a lhss object

## Usage

```
## S3 method for class 'lhss'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

## Arguments

- x Object of class lhss.
- digits Number of digits to use when printing the output.
- ... further arguments on how to format the number of digits.

## Value

`invisible` The inputted lhss object.

## See Also

[print](#), [lhss](#)

## Examples

```
set.seed(123)
# Fit model (minimal example to limit computation time)
dr <- lhss(numerator_small, denominator_small,
            nsigma = 5, nlambda = 3, nccenters = 50, maxit = 100)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
```

## print.naivedensityratio

*Print a naivedensityratio object*

## Description

Print a naivedensityratio object

## Usage

```
## S3 method for class 'naivedensityratio'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

## Arguments

- x Object of class naivesubspacedensityratio.
- digits Number of digits to use when printing the output.
- ... further arguments on how to format the number of digits.

## Value

invisible The inputted naivedensityratio object.

## See Also

[print](#), [naive](#)

## Examples

```
set.seed(123)
# Fit model
dr <- naive(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
naive(numerator_small, denominator_small, m=2, kernel="epanechnikov")
```

**print.spectral** *Print a spectral object*

## Description

Print a spectral object

## Usage

```
## S3 method for class 'spectral'
print(x, digits = max(3L, getOption("digits")) - 3L), ...)
```

## Arguments

- x Object of class `spectral`.
- digits Number of digits to use when printing the output.
- ... further arguments on how to format the number of digits.

## Value

`invisible` The inputted spectral object.

## See Also

[print, spectral](#)

## Examples

```
set.seed(123)
# Fit model
dr <- spectral(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
spectral(numerator_small, denominator_small, sigma = 2)
```

**print.summary.kliep** *Print a summary.kliep object*

## Description

Print a summary.kliep object

## Usage

```
## S3 method for class 'summary.kliep'
print(x, digits = max(3L, getOption("digits")) - 3L), ...)
```

## Arguments

- x Object of class summary.kliep.
- digits Number of digits to use when printing the output.
- ... further arguments on how to format the number of digits.

## Value

invisible The inputted summary.kliep object.

## See Also

[print](#), [summary.kliep](#), [kliep](#)

## Examples

```
set.seed(123)
# Fit model
dr <- kliep(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kliep(numerator_small, denominator_small,
      nsigma = 1, ncenters = 100, nfold = 10,
      epsilon = 10^{2:-5}, maxit = 500)
```

**print.summary.kmm** *Print a summary.kmm object*

## Description

Print a `summary.kmm` object

## Usage

```
## S3 method for class 'summary.kmm'
print(x, digits = max(3L, getOption("digits")) - 3L), ...)
```

## Arguments

- x Object of class `summary.kmm`.
- digits Number of digits to use when printing the output.
- ... further arguments on how to format the number of digits.

## Value

`invisible` The inputted `summary.kmm` object.

## See Also

[print](#), [summary.kmm](#), [kmm](#)

## Examples

```
set.seed(123)
# Fit model
dr <- kmm(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kmm(numerator_small, denominator_small,
     nsigma = 5, ncenters = 100, nfold = 10,
     constrained = TRUE)
```

---

`print.summary.lhss`     *Print a summary.lhss object*

---

## Description

Print a `summary.lhss` object

## Usage

```
## S3 method for class 'summary.lhss'
print(x, digits = max(3L, getOption("digits")) - 3L), ...)
```

## Arguments

- `x`              Object of class `summary.lhss`.
- `digits`          Number of digits to use when printing the output.
- `...`              further arguments on how to format the number of digits.

## Value

`invisible` The inputted `summary.lhss` object.

## See Also

[print](#), [summary.lhss](#), [lhss](#)

## Examples

```
set.seed(123)
# Fit model (minimal example to limit computation time)
dr <- lhss(numerator_small, denominator_small,
            nsigma = 5, nlambda = 3, nccenters = 50, maxit = 100)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
```

**print.summary.naivedensityratio**  
*Print a summary.naivedensityratio object*

## Description

Print a summary.naivedensityratio object

## Usage

```
## S3 method for class 'summary.naivedensityratio'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
```

## Arguments

- x Object of class summary.naivedensityratio.
- digits Number of digits to use when printing the output.
- ... further arguments on how to format the number of digits.

## Value

**invisible** The inputted summary.naivedensityratio object.

## See Also

[print](#), [summary.naivedensityratio](#), [naive](#)

## Examples

```
set.seed(123)
# Fit model
dr <- naive(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
naive(numerator_small, denominator_small, m=2, kernel="epanechnikov")
```

---

## print.summary.spectral

*Print a summary.spectral object*

---

## Description

Print a summary.spectral object

## Usage

```
## S3 method for class 'summary.spectral'
print(x, digits = max(3L, getOption("digits")) - 3L), ...)
```

## Arguments

- x Object of class summary.spectral.
- digits Number of digits to use when printing the output.
- ... further arguments on how to format the number of digits.

## Value

invisible The inputted summary.spectral object.

## See Also

[print](#), [summary.spectral](#), [spectral](#)

## Examples

```
set.seed(123)
# Fit model
dr <- spectral(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
spectral(numerator_small, denominator_small, sigma = 2)
```

**print.summary.ulsif** *Print a summary.ulsif object*

## Description

Print a `summary.ulsif` object

## Usage

```
## S3 method for class 'summary.ulsif'
print(x, digits = max(3L, getOption("digits")) - 3L), ...)
```

## Arguments

- `x` Object of class `summary.ulsif`.
- `digits` Number of digits to use when printing the output.
- `...` further arguments on how to format the number of digits.

## Value

`invisible` The inputted `summary.ulsif` object.

## See Also

[print](#), [summary.ulsif](#), [ulsif](#)

## Examples

```
set.seed(123)
# Fit model
dr <- ulif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulif(numerator_small, denominator_small, sigma = 2, lambda = 2)
```

---

print.ulif

*Print a ulif object*

---

## Description

Print a ulif object

## Usage

```
## S3 method for class 'ulif'
print(x, digits = max(3L, getOption("digits")) - 3L), ...)
```

## Arguments

- x Object of class ulif.
- digits Number of digits to use when printing the output.
- ... further arguments on how to format the number of digits.

## Value

invisible The inputted ulif object.

## See Also

[print, ulif](#)

## Examples

```
set.seed(123)
# Fit model
dr <- ulsif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulsif(numerator_small, denominator_small, sigma = 2, lambda = 2)
```

**spectral**

*Spectral series based density ratio estimation*

## Description

Spectral series based density ratio estimation

## Usage

```
spectral(
  df_numerator,
  df_denominator,
  m = NULL,
  scale = "numerator",
  nsigma = 10,
  sigma_quantile = NULL,
  sigma = NULL,
  ncenters = NULL,
  cv = TRUE,
  nfold = 10,
  parallel = FALSE,
  nthreads = NULL,
  progressbar = TRUE
)
```

## Arguments

**df\_numerator** data.frame with exclusively numeric variables with the numerator samples

df_denominator	data.frame with exclusively numeric variables with the denominator samples (must have the same variables as df_denominator)
m	Integer vector indicating the number of eigenvectors to use in the spectral series expansion. Defaults to 50 evenly spaced values between 1 and the number of denominator samples (or the largest number of samples that can be used as centers in the cross-validation scheme).
scale	"numerator", "denominator", or NULL, indicating whether to standardize each numeric variable according to the numerator means and standard deviations, the denominator means and standard deviations, or apply no standardization at all.
nsigma	Integer indicating the number of sigma values (bandwidth parameter of the Gaussian kernel gram matrix) to use in cross-validation.
sigma_quantile	NULL or numeric vector with probabilities to calculate the quantiles of the distance matrix to obtain sigma values. If NULL, nsigma values between 0.05 and 0.95 are used.
sigma	NULL or a scalar value to determine the bandwidth of the Gaussian kernel gram matrix. If NULL, nsigma values between 0.05 and 0.95 are used.
ncenters	integer If smaller than the number of denominator observations, an approximation to the eigenvector expansion based on only ncenters samples is performed, instead of the full expansion. This can be useful for large datasets. Defaults to NULL, such that all denominator samples are used.
cv	logical indicating whether to use cross-validation to determine the optimal sigma value and the optimal number of eigenvectors.
nfold	Integer indicating the number of folds to use in the cross-validation scheme. If cv is FALSE, this parameter is ignored.
parallel	logical indicating whether to use parallel processing in the cross-validation scheme.
nthreads	NULL or integer indicating the number of threads to use for parallel processing. If parallel processing is enabled, it defaults to the number of available threads minus one.
progressbar	Logical indicating whether or not to display a progressbar.

## Value

spectral-object, containing all information to calculate the density ratio using optimal sigma and optimal spectral series expansion.

## References

Izbicki, R., Lee, A. & Schafer, C. (2014). High-Dimensional Density Ratio Estimation with Extensions to Approximate Likelihood Computation. Proceedings of Machine Learning Research 33, 420-429. Available from <https://proceedings.mlr.press/v33/izbicki14.html>.

## Examples

```
set.seed(123)
# Fit model
dr <- spectral(numerator_small, denominator_small)
```

```
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
spectral(numerator_small, denominator_small, sigma = 2)
```

**summary.kliep**

*Extract summary from kliep object, including two-sample significance test for homogeneity of the numerator and denominator samples*

**Description**

Extract summary from kliep object, including two-sample significance test for homogeneity of the numerator and denominator samples

**Usage**

```
## S3 method for class 'kliep'
summary(
  object,
  test = FALSE,
  n_perm = 100,
  parallel = FALSE,
  cluster = NULL,
  min_pred = 1e-06,
  ...
)
```

**Arguments**

<b>object</b>	Object of class kliep
<b>test</b>	logical indicating whether to statistically test for homogeneity of the numerator and denominator samples.
<b>n_perm</b>	Scalar indicating number of permutation samples
<b>parallel</b>	logical indicating to run the permutation test in parallel
<b>cluster</b>	NULL or a cluster object created by makeCluster. If NULL and parallel = TRUE, it uses the number of available cores minus 1.
<b>min_pred</b>	Scalar indicating the minimum value for the predicted density ratio values (used in the divergence statistic) to avoid negative density ratio values.
<b>...</b>	further arguments passed to or from other methods.

**Value**

Summary of the fitted density ratio model

**Examples**

```
set.seed(123)
# Fit model
dr <- kliep(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kliep(numerator_small, denominator_small,
      nsigma = 1, ncenters = 100, nfold = 10,
      epsilon = 10^{2:-5}, maxit = 500)
```

**summary.kmm**

*Extract summary from kmm object, including two-sample significance test for homogeneity of the numerator and denominator samples*

**Description**

Extract summary from kmm object, including two-sample significance test for homogeneity of the numerator and denominator samples

**Usage**

```
## S3 method for class 'kmm'
summary(
  object,
  test = FALSE,
  n_perm = 100,
  parallel = FALSE,
  cluster = NULL,
  min_pred = 1e-06,
  ...
)
```

## Arguments

<code>object</code>	Object of class <code>kmm</code>
<code>test</code>	logical indicating whether to statistically test for homogeneity of the numerator and denominator samples.
<code>n_perm</code>	Scalar indicating number of permutation samples
<code>parallel</code>	logical indicating to run the permutation test in parallel
<code>cluster</code>	NULL or a cluster object created by <code>makeCluster</code> . If NULL and <code>parallel = TRUE</code> , it uses the number of available cores minus 1.
<code>min_pred</code>	Scalar indicating the minimum value for the predicted density ratio values (used in the divergence statistic) to avoid negative density ratio values.
<code>...</code>	further arguments passed to or from other methods.

## Value

Summary of the fitted density ratio model

## Examples

```
set.seed(123)
# Fit model
dr <- kmm(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
kmm(numerator_small, denominator_small,
     nsigma = 5, ncenters = 100, nfold = 10,
     constrained = TRUE)
```

`summary.lhss`

*Extract summary from lhss object, including two-sample significance test for homogeneity of the numerator and denominator samples*

## Description

Extract summary from `lhss` object, including two-sample significance test for homogeneity of the numerator and denominator samples

**Usage**

```
## S3 method for class 'lhss'
summary(
  object,
  test = FALSE,
  n_perm = 100,
  parallel = FALSE,
  cluster = NULL,
  ...
)
```

**Arguments**

<code>object</code>	Object of class <code>lhss</code>
<code>test</code>	logical indicating whether to statistically test for homogeneity of the numerator and denominator samples.
<code>n_perm</code>	Scalar indicating number of permutation samples
<code>parallel</code>	logical indicating to run the permutation test in parallel
<code>cluster</code>	<code>NULL</code> or a cluster object created by <code>makeCluster</code> . If <code>NULL</code> and <code>parallel = TRUE</code> , it uses the number of available cores minus 1.
<code>...</code>	further arguments passed to or from other methods.

**Value**

Summary of the fitted density ratio model

**Examples**

```
set.seed(123)
# Fit model (minimal example to limit computation time)
dr <- lhss(numerator_small, denominator_small,
            nsigma = 5, nlambda = 3, ncenters = 50, maxit = 100)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
```

**summary.naivedensityratio**

*Extract summary from naivedensityratio object, including two-sample significance test for homogeneity of the numerator and denominator samples*

## Description

Extract summary from naivedensityratio object, including two-sample significance test for homogeneity of the numerator and denominator samples

## Usage

```
## S3 method for class 'naivedensityratio'
summary(
  object,
  test = FALSE,
  n_perm = 100,
  parallel = FALSE,
  cluster = NULL,
  ...
)
```

## Arguments

<code>object</code>	Object of class <code>naivedensityratio</code>
<code>test</code>	logical indicating whether to statistically test for homogeneity of the numerator and denominator samples.
<code>n_perm</code>	Scalar indicating number of permutation samples
<code>parallel</code>	logical indicating to run the permutation test in parallel
<code>cluster</code>	NULL or a cluster object created by <code>makeCluster</code> . If NULL and <code>parallel</code> = TRUE, it uses the number of available cores minus 1.
<code>...</code>	further arguments passed to or from other methods.

## Value

Summary of the fitted density ratio model

## Examples

```
set.seed(123)
# Fit model
dr <- naive(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
```

```

summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
naive(numerator_small, denominator_small, m=2, kernel="epanechnikov")

```

**summary.spectral**

*Extract summary from spectral object, including two-sample significance test for homogeneity of the numerator and denominator samples*

**Description**

Extract summary from spectral object, including two-sample significance test for homogeneity of the numerator and denominator samples

**Usage**

```

## S3 method for class 'spectral'
summary(
  object,
  test = FALSE,
  n_perm = 100,
  parallel = FALSE,
  cluster = NULL,
  ...
)

```

**Arguments**

object	Object of class spectral
test	logical indicating whether to statistically test for homogeneity of the numerator and denominator samples.
n_perm	Scalar indicating number of permutation samples
parallel	logical indicating to run the permutation test in parallel
cluster	NULL or a cluster object created by makeCluster. If NULL and parallel = TRUE, it uses the number of available cores minus 1.
...	further arguments passed to or from other methods.

**Value**

Summary of the fitted density ratio model

## Examples

```
set.seed(123)
# Fit model
dr <- spectral(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
spectral(numerator_small, denominator_small, sigma = 2)
```

**summary.ulsif**

*Extract summary from ulsif object, including two-sample significance test for homogeneity of the numerator and denominator samples*

## Description

Extract summary from ulsif object, including two-sample significance test for homogeneity of the numerator and denominator samples

## Usage

```
## S3 method for class 'ulsif'
summary(
  object,
  test = FALSE,
  n_perm = 100,
  parallel = FALSE,
  cluster = NULL,
  ...
)
```

## Arguments

<b>object</b>	Object of class <code>ulsif</code>
<b>test</b>	logical indicating whether to statistically test for homogeneity of the numerator and denominator samples.
<b>n_perm</b>	Scalar indicating number of permutation samples
<b>parallel</b>	logical indicating to run the permutation test in parallel

cluster	NULL or a cluster object created by <code>makeCluster</code> . If NULL and <code>parallel = TRUE</code> , it uses the number of available cores minus 1.
...	further arguments passed to or from other methods.

**Value**

Summary of the fitted density ratio model

**Examples**

```
set.seed(123)
# Fit model
dr <- ulsif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulsif(numerator_small, denominator_small, sigma = 2, lambda = 2)
```

**Description**

Unconstrained least-squares importance fitting

**Usage**

```
ulsif(
  df_numerator,
  df_denominator,
  intercept = TRUE,
  scale = "numerator",
  nsigma = 10,
  sigma_quantile = NULL,
  sigma = NULL,
  nlambda = 20,
  lambda = NULL,
  ncenters = 200,
```

```

centers = NULL,
parallel = FALSE,
nthreads = NULL,
progressbar = TRUE
)

```

## Arguments

<code>df_numerator</code>	<code>data.frame</code> with exclusively numeric variables with the numerator samples
<code>df_denominator</code>	<code>data.frame</code> with exclusively numeric variables with the denominator samples (must have the same variables as <code>df_denominator</code> )
<code>intercept</code>	logical Indicating whether to include an intercept term in the model. Defaults to TRUE.
<code>scale</code>	" <code>numerator</code> ", " <code>denominator</code> ", or <code>NULL</code> , indicating whether to standardize each numeric variable according to the numerator means and standard deviations, the denominator means and standard deviations, or apply no standardization at all.
<code>nsigma</code>	Integer indicating the number of sigma values (bandwidth parameter of the Gaussian kernel gram matrix) to use in cross-validation.
<code>sigma_quantile</code>	<code>NULL</code> or numeric vector with probabilities to calculate the quantiles of the distance matrix to obtain sigma values. If <code>NULL</code> , <code>nsigma</code> values between 0.05 and 0.95 are used.
<code>sigma</code>	<code>NULL</code> or a scalar value to determine the bandwidth of the Gaussian kernel gram matrix. If <code>NULL</code> , <code>nsigma</code> values between 0.05 and 0.95 are used.
<code>nlambda</code>	Integer indicating the number of lambda values (regularization parameter), by default, <code>lambda</code> is set to <code>10^seq(3, -3, length.out = nlambda)</code> .
<code>lambda</code>	<code>NULL</code> or numeric vector indicating the lambda values to use in cross-validation
<code>ncenters</code>	Maximum number of Gaussian centers in the kernel gram matrix. Defaults to all numerator samples.
<code>centers</code>	<code>NULL</code> or numeric matrix with the same dimensions as the data, indicating the centers for the Gaussian kernel gram matrix.
<code>parallel</code>	logical indicating whether to use parallel processing in the cross-validation scheme.
<code>nthreads</code>	<code>NULL</code> or integer indicating the number of threads to use for parallel processing. If parallel processing is enabled, it defaults to the number of available threads minus one.
<code>progressbar</code>	Logical indicating whether or not to display a progressbar.

## Value

`ulsif`-object, containing all information to calculate the density ratio using optimal sigma and optimal weights.

## References

Kanamori, T., Hido, S., & Sugiyama, M. (2009). A least-squares approach to direct importance estimation. *Journal of Machine Learning Research*, 10, 1391-1445. Available from <https://jmlr.org/papers/v10/kanamori09a.html>

## Examples

```
set.seed(123)
# Fit model
dr <- ulsif(numerator_small, denominator_small)
# Inspect model object
dr
# Obtain summary of model object
summary(dr)
# Plot model object
plot(dr)
# Plot density ratio for each variable individually
plot_univariate(dr)
# Plot density ratio for each pair of variables
plot_bivariate(dr)
# Predict density ratio and inspect first 6 predictions
head(predict(dr))
# Fit model with custom parameters
ulsif(numerator_small, denominator_small, sigma = 2, lambda = 2)
```

# Index

- \* **colon**
  - colon, 3
- \* **datasets**
  - colon, 3
  - denominator\_data, 4
  - denominator\_small, 5
  - insurance, 8
  - kidiq, 9
  - numerator\_data, 17
  - numerator\_small, 17
- \* **data**
  - colon, 3
  - denominator\_data, 4
  - denominator\_small, 5
  - insurance, 8
  - kidiq, 9
  - numerator\_data, 17
  - numerator\_small, 17
- \* **insurance**
  - insurance, 8
- \* **kidiq**
  - kidiq, 9
- \* **kliep**
  - predict.kliep, 22
- \* **kmm**
  - predict.kmm, 23
- \* **lhss**
  - predict.lhss, 24
- \* **naive**
  - predict.naivedensityratio, 25
- \* **predict**
  - predict.kliep, 22
  - predict.kmm, 23
  - predict.lhss, 24
  - predict.naivedensityratio, 25
  - predict.spectral, 26
  - predict.ulsfif, 27
- \* **spectral**
  - predict.spectral, 26
- \* **ulsif**
  - predict.ulsfif, 27
- colon, 3
- create\_bivariate\_plot, 3
- create\_univariate\_plot, 4
- create\_univariate\_plot(), 4
- denominator\_data, 4, 5
- denominator\_small, 5
- distance, 5
- dr.histogram, 6
- insurance, 8
- kernel\_gaussian, 9
- kidiq, 9
- kliep, 8, 10, 22, 28, 33
- kliep(), 7, 19, 21
- kmm, 8, 11, 23, 29, 34
- lhss, 8, 13, 24, 30, 35
- naive, 8, 15, 25, 31, 36
- naive(), 7, 19, 21
- numerator\_data, 17, 17
- numerator\_small, 17
- permute, 18
- plot.kliep(dr.histogram), 6
- plot.kmm(dr.histogram), 6
- plot.lhss(dr.histogram), 6
- plot.naivedensityratio(dr.histogram), 6
- plot.spectral(dr.histogram), 6
- plot.ulsfif(dr.histogram), 6
- plot\_bivariate, 19
- plot\_univariate, 20
- predict, 22–25, 27
- predict.kliep, 22
- predict.kmm, 23
- predict.lhss, 24

predict.naivedensityratio, 25  
predict.spectral, 26  
predict.ulsif, 27  
print, 28–39  
print.kliep, 28  
print.kmm, 29  
print.lhss, 30  
print.naivedensityratio, 31  
print.spectral, 32  
print.summary.kliep, 33  
print.summary.kmm, 34  
print.summary.lhss, 35  
print.summary.naivedensityratio, 36  
print.summary.spectral, 37  
print.summary.ulsif, 38  
print.ulsif, 39  
  
spectral, 8, 27, 32, 37, 40  
stats::approx, 16  
stats::density, 16  
stats::density(), 16  
summary.kliep, 33, 42  
summary.kmm, 34, 43  
summary.lhss, 35, 44  
summary.naivedensityratio, 36, 46  
summary.spectral, 37, 47  
summary.ulsif, 38, 48  
  
ulsif, 8, 27, 38, 39, 49  
ulsif(), 7, 19, 21