

# Package ‘cicalc’

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**Type** Package

**Title** Calculate Confidence Intervals

**Version** 0.1.0

**Description** This calculates a variety of different CIs for proportions and difference of proportions that are commonly used in the pharmaceutical industry including Wald, Wilson, Clopper-Pearson, Agresti-Coull and Jeffreys for proportions. And Miettinen-Nurminen (1985) <[doi:10.1002/sim.4780040211](https://doi.org/10.1002/sim.4780040211)>, Wald, Haldane, and Mee <[https://www.lexjansen.com/wuss/2016/127\\_Final\\_Paper\\_PDF.pdf](https://www.lexjansen.com/wuss/2016/127_Final_Paper_PDF.pdf)> for difference in proportions.

**License** Apache License (>= 2)

**URL** <https://gsk-biostatistics.github.io/cicalc/>

**Depends** R (>= 4.1.0)

**Imports** broom, cli, dplyr, forcats, glue, purrr, rlang, tidyr

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ci\_prop\_agresti\_coull *Agresti-Coull CI*

---

## Description

Calculates the Agresti-Coull interval (created by Alan Agresti and Brent Coull) by (for 95% CI) adding two successes and two failures to the data and then using the Wald formula to construct a CI.

## Usage

```
ci_prop_agresti_coull(x, conf.level = 0.95, data = NULL)
```

## Arguments

|            |                                                                                                              |
|------------|--------------------------------------------------------------------------------------------------------------|
| x          | (binary/numeric/logical)<br>vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1) |
| conf.level | (scalar numeric)<br>a scalar in (0,1) indicating the confidence level. Default is 0.95                       |
| data       | (data.frame)<br>Optional data frame containing the variables specified in x and by.                          |

## Details

$$\left( \frac{\tilde{p} + z_{\alpha/2}^2/2}{n + z_{\alpha/2}^2} \pm z_{\alpha/2} \sqrt{\frac{\tilde{p}(1 - \tilde{p})}{n} + \frac{z_{\alpha/2}^2}{4n^2}} \right)$$

**Value**

An object containing the following components:

|            |                                        |
|------------|----------------------------------------|
| n          | Number of responses                    |
| N          | Total number                           |
| estimate   | The point estimate of the proportion   |
| conf.low   | Lower bound of the confidence interval |
| conf.high  | Upper bound of the confidence interval |
| conf.level | The confidence level used              |
| method     | Type of method used                    |

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ci\_prop\_clopper\_pearson

*Clopper-Pearson CI*


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**Description**

Calculates the Clopper-Pearson interval by calling `stats::binom.test()`. Also referred to as the exact method.

**Usage**

```
ci_prop_clopper_pearson(x, conf.level = 0.95, data = NULL)
```

**Arguments**

|            |                                                                                                              |
|------------|--------------------------------------------------------------------------------------------------------------|
| x          | (binary/numeric/logical)<br>vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1) |
| conf.level | (scalar numeric)<br>a scalar in (0,1) indicating the confidence level. Default is 0.95                       |
| data       | (data.frame)<br>Optional data frame containing the variables specified in x and by.                          |

**Details**

$$\left( \frac{k}{n} \pm z_{\alpha/2} \sqrt{\frac{\frac{k}{n}(1 - \frac{k}{n})}{n} + \frac{z_{\alpha/2}^2}{4n^2}} \right) / \left( 1 + \frac{z_{\alpha/2}^2}{n} \right)$$

**Value**

An object containing the following components:

|            |                                        |
|------------|----------------------------------------|
| n          | Number of responses                    |
| N          | Total number                           |
| estimate   | The point estimate of the proportion   |
| conf.low   | Lower bound of the confidence interval |
| conf.high  | Upper bound of the confidence interval |
| conf.level | The confidence level used              |
| method     | Type of method used                    |

---

|                      |                                                                  |
|----------------------|------------------------------------------------------------------|
| ci_prop_diff_haldane | <i>Haldane Confidence Interval for Difference in Proportions</i> |
|----------------------|------------------------------------------------------------------|

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**Description**

Haldane Confidence Interval for Difference in Proportions

**Usage**

```
ci_prop_diff_haldane(x, by, conf.level = 0.95, data = NULL)
```

**Arguments**

|            |                                                                                                                                                                                         |
|------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| x          | (binary/numeric/logical)<br>vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)                                                                            |
| by         | (string)<br>A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument. |
| conf.level | (scalar numeric)<br>a scalar in (0,1) indicating the confidence level. Default is 0.95                                                                                                  |
| data       | (data.frame)<br>Optional data frame containing the variables specified in x and by.                                                                                                     |

**Details**

The confidence interval is calculated by  $\theta^* \pm w$  where:

$$\theta^* = \frac{(\hat{p}_1 - \hat{p}_2) + z^2 v(1 - 2\hat{\psi})}{1 + z^2 u}$$

where

$$w = \frac{z}{1 + z^2 u} \sqrt{u\{4\hat{\psi}(1 - \hat{\psi}) - (\hat{p}_1 - \hat{p}_2)^2\} + 2v(1 - 2\hat{\psi})(\hat{p}_1 - \hat{p}_2) + 4z^2 v^2(1 - 2\hat{\psi})^2}$$

$$\hat{\psi} = \frac{\hat{p}_1 + \hat{p}_2}{2}$$

$$u = \frac{1/n_1 + 1/n_2}{4}$$

$$v = \frac{1/n_1 - 1/n_2}{4}$$

**Value**

An object containing the following components:

|            |                                                              |
|------------|--------------------------------------------------------------|
| n          | The number of responses for each group                       |
| N          | The total number in each group                               |
| estimate   | The point estimate of the difference in proportions (theta*) |
| conf.low   | Lower bound of the confidence interval                       |
| conf.high  | Upper bound of the confidence interval                       |
| conf.level | The confidence level used                                    |
| method     | Haldane Confidence Interval                                  |

**References**

Constructing Confidence Intervals for the Differences of Binomial Proportions in SAS

**Examples**

```
responses <- expand(c(9, 3), c(10, 10))
arm <- rep(c("treat", "control"), times = c(10, 10))

# Calculate 95% confidence interval for difference in proportions
ci_prop_diff_haldane(x = responses, by = arm)
```

---

|                 |                                                                         |
|-----------------|-------------------------------------------------------------------------|
| ci_prop_diff_jp | <i>Jeffreys-Perks Confidence Interval for Difference in Proportions</i> |
|-----------------|-------------------------------------------------------------------------|

---

**Description**

Jeffreys-Perks Confidence Interval for Difference in Proportions

**Usage**

```
ci_prop_diff_jp(x, by, conf.level = 0.95, data = NULL)
```

**Arguments**

|                         |                                                                                                                                                                                                      |
|-------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>x</code>          | (binary/numeric/logical)<br>vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)                                                                                         |
| <code>by</code>         | (string)<br>A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the <code>data</code> argument. |
| <code>conf.level</code> | (scalar numeric)<br>a scalar in (0,1) indicating the confidence level. Default is 0.95                                                                                                               |
| <code>data</code>       | (data.frame)<br>Optional data frame containing the variables specified in <code>x</code> and <code>by</code> .                                                                                       |

**Details**

The confidence interval is calculated by  $\theta^* \pm w$  where:

$$\theta^* = \frac{(\hat{p}_1 - \hat{p}_2) + z^2 v (1 - 2\hat{\psi})}{1 + z^2 u}$$

where

$$w = \frac{z}{1 + z^2 u} \sqrt{u\{4\hat{\psi}(1 - \hat{\psi}) - (\hat{p}_1 - \hat{p}_2)^2\} + 2v(1 - 2\hat{\psi})(\hat{p}_1 - \hat{p}_2) + 4z^2 v^2 (1 - 2\hat{\psi})^2}$$

$$\hat{\psi} = \frac{1}{2} \left( \frac{x_1 + 1/2}{n_1 + 1} + \frac{x_2 + 1/2}{n_2 + 1} \right)$$

$$u = \frac{1/n_1 + 1/n_2}{4}$$

$$v = \frac{1/n_1 - 1/n_2}{4}$$

**Value**

An object containing the following components:

|                         |                                                              |
|-------------------------|--------------------------------------------------------------|
| <code>n</code>          | The number of responses for each group                       |
| <code>N</code>          | The total number in each group                               |
| <code>estimate</code>   | The point estimate of the difference in proportions (theta*) |
| <code>conf.low</code>   | Lower bound of the confidence interval                       |
| <code>conf.high</code>  | Upper bound of the confidence interval                       |
| <code>conf.level</code> | The confidence level used                                    |
| <code>method</code>     | Jeffreys-Perks Confidence Interval                           |

**References**

Constructing Confidence Intervals for the Differences of Binomial Proportions in SAS

**Examples**

```

responses <- expand(c(9, 3), c(10, 10))
arm <- rep(c("treat", "control"), times = c(10, 10))

# Calculate 95% confidence interval for difference in proportions
ci_prop_diff_jp(x = responses, by = arm)

```

---

|                  |                                                              |
|------------------|--------------------------------------------------------------|
| ci_prop_diff_mee | <i>Mee Confidence Interval for Difference in Proportions</i> |
|------------------|--------------------------------------------------------------|

---

**Description**

Mee Confidence Interval for Difference in Proportions

**Usage**

```
ci_prop_diff_mee(x, by, conf.level = 0.95, delta = NULL, data = NULL)
```

**Arguments**

|            |                                                                                                                                                                                                                                                                  |
|------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| x          | (binary/numeric/logical)<br>vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)                                                                                                                                                     |
| by         | (string)<br>A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.                                                                          |
| conf.level | (scalar numeric)<br>a scalar in (0,1) indicating the confidence level. Default is 0.95                                                                                                                                                                           |
| delta      | (numeric)<br>Optionally a single number or a vector of numbers between -1 and 1 (not inclusive) to set the difference between two groups under the null hypothesis. If provided, the function returns the test statistic and p-value under the delta hypothesis. |
| data       | (data.frame)<br>Optional data frame containing the variables specified in x and by.                                                                                                                                                                              |

**Details**

The confidence interval is calculated by  $\theta^* \pm w$  where:

$$\theta^* = \frac{(\hat{p}_1 - \hat{p}_2) + z^2 v(1 - 2\hat{\psi})}{1 + z^2 u}$$

where

$$w = \frac{z}{1 + z^2 u} \sqrt{u\{4\hat{\psi}(1 - \hat{\psi}) - (\hat{p}_1 - \hat{p}_2)^2\} + 2v(1 - 2\hat{\psi})(\hat{p}_1 - \hat{p}_2) + 4z^2 v^2(1 - 2\hat{\psi})^2}$$

$$\hat{\psi} = \frac{1}{2} \left( \frac{x_1 + 1/2}{n_1 + 1} + \frac{x_2 + 1/2}{n_2 + 1} \right)$$
$$u = \frac{1/n_1 + 1/n_2}{4}$$
$$v = \frac{1/n_1 - 1/n_2}{4}$$

**Value**

An object containing the following components:

|            |                                                             |
|------------|-------------------------------------------------------------|
| n          | The number of responses for each group                      |
| N          | The total number in each group                              |
| estimate   | The point estimate of the difference in proportions (p1-p2) |
| conf.low   | Lower bound of the confidence interval                      |
| conf.high  | Upper bound of the confidence interval                      |
| conf.level | The confidence level used                                   |
| method     | Mee Confidence Interval                                     |

**References**

Constructing Confidence Intervals for the Differences of Binomial Proportions in SAS

**Examples**

```
responses <- expand(c(9, 3), c(10, 10))
arm <- rep(c("treat", "control"), times = c(10, 10))

# Calculate 95% confidence interval for difference in proportions
ci_prop_diff_mee(x = responses, by = arm)
```

---

|                 |                                                                             |
|-----------------|-----------------------------------------------------------------------------|
| ci_prop_diff_mn | <i>Miettinen-Nurminen Confidence Interval for Difference in Proportions</i> |
|-----------------|-----------------------------------------------------------------------------|

---

**Description**

Calculates the Miettinen-Nurminen (MN) confidence interval for the difference between two proportions. This method can be more accurate than traditional methods, especially with small sample sizes or proportions close to 0 or 1.

**Usage**

```
ci_prop_diff_mn(x, by, conf.level = 0.95, delta = NULL, data = NULL)
```

### Arguments

|            |                                                                                                                                                                                                                                                                  |
|------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| x          | (binary/numeric/logical)<br>vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)                                                                                                                                                     |
| by         | (string)<br>A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.                                                                          |
| conf.level | (scalar numeric)<br>a scalar in (0,1) indicating the confidence level. Default is 0.95                                                                                                                                                                           |
| delta      | (numeric)<br>Optionally a single number or a vector of numbers between -1 and 1 (not inclusive) to set the difference between two groups under the null hypothesis. If provided, the function returns the test statistic and p-value under the delta hypothesis. |
| data       | (data.frame)<br>Optional data frame containing the variables specified in x and by.                                                                                                                                                                              |

### Details

The function implements the Miettinen-Nurminen method to compute confidence intervals for the difference between two proportions. This approach:

- Calculates the Miettinen-Nurminen score test statistic for different possible values of the proportion difference (delta)
- Identifies the delta values where the test statistic equals the critical value corresponding to the desired confidence level
- Returns these boundary values as the confidence interval limits

The method uses a score test with a small-sample correction factor, making it more accurate than normal approximation methods, especially for small samples or extreme proportions. The equation for the test statistics is as follows:

$$H_0 : \hat{d} - \delta \leq 0 \quad \text{vs.} \quad H_1 : \hat{d} - \delta > 0$$

$$T_\delta = \frac{\hat{p}_x - \hat{p}_y - \delta}{\sigma_{mn}(\delta)}$$

where  $\hat{p}_* = s_*/n_*$  represent the observed number of successes divided by the number of participant in that group. The  $\sigma_{mn}(\delta)$  is a function of the delta values and is create with the following equation"  $\tilde{p}_*$  represent the MLE of the proportions.

$$\sigma_{mn}(\delta) = \sqrt{\left[ \frac{\tilde{p}_y(1 - \tilde{p}_y)}{n_x} + \frac{\tilde{p}_x(1 - \tilde{p}_x)}{n_y} \right] \left( \frac{N}{N-1} \right)}$$

$\tilde{p}_x = 2p \cdot \cos(a) - \frac{L_2}{3L_3}$  and  $\tilde{p}_y = \tilde{p}_x + \delta$  where:

- $p = \pm \sqrt{\frac{L_2^2}{(3L_3)^2} - \frac{L_1}{3L_3}}$
- $a = 1/3[\pi + \cos^{-1}(q/p^3)]$
- $q = \frac{L_2^3}{(3L_3)^3} - \frac{L_1L_2}{6L_3^2} + \frac{L_0}{2L_3}$
- $L_3 = n_x + n_y$
- $L_2 = (n_x + 2n_y)\delta - N - (s_x + s_y)$
- $L_1 = (n_y\delta - L_3 - 2s_y)\delta + s_x + s_y$
- $L_0 = s_y\delta(1 - \delta)$

For more information about these equations see Miettinen (1985)

## Value

An object containing the following components:

|            |                                                                           |
|------------|---------------------------------------------------------------------------|
| estimate   | The point estimate of the difference in proportions (p_x - p_y)           |
| conf.low   | Lower bound of the confidence interval                                    |
| conf.high  | Upper bound of the confidence interval                                    |
| conf.level | The confidence level used                                                 |
| delta      | delta value(s) used                                                       |
| statistic  | Z-Statistic under the null hypothesis based on the given 'delta'          |
| p.value    | p-value under the null hypothesis based on the given 'delta'              |
| method     | Description of the method used ("Miettinen-Nurminen Confidence Interval") |

If delta is not provided statistic and p.value will be NULL

## References

Miettinen, O. S., & Nurminen, M. (1985). Comparative analysis of two rates. *Statistics in Medicine*, 4(2), 213-226.

## Examples

```
# Generate binary samples
responses <- expand(c(9, 3), c(10, 10))
arm <- rep(c("treat", "control"), times = c(10, 10))

# Calculate 95% confidence interval for difference in proportions
ci_prop_diff_mn(x = responses, by = arm)

# Calculate 99% confidence interval
ci_prop_diff_mn(x = responses, by = arm, conf.level = 0.99)

# Calculate the p-value under the null hypothesis delta = -0.1
ci_prop_diff_mn(x = responses, by = arm, delta = -0.1)

# Calculate from a data.frame
data <- data.frame(responses, arm)
ci_prop_diff_mn(x = responses, by = arm, data = data)
```

---

ci\_prop\_diff\_mn\_strata

*Stratified Miettinen-Nurminen Confidence Interval for Difference in Proportions*


---

## Description

Calculates Stratified Miettinen-Nurminen (MN) confidence intervals and corresponding point estimates for the difference between two proportions

## Usage

```
ci_prop_diff_mn_strata(
  x,
  by,
  strata,
  method = c("score", "summary score"),
  conf.level = 0.95,
  delta = NULL,
  data = NULL
)
```

## Arguments

|            |                                                                                                                                                                                                                                                                                |
|------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| x          | (binary/numeric/logical)<br>vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)                                                                                                                                                                   |
| by         | (string)<br>A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument.                                                                                        |
| strata     | (numeric)<br>A vector specifying the stratum for each observation. It needs to be the length of x or a multiple of x if multiple levels of strata are present. Can also be a column name (or vector of column names NOT quoted) if a data frame provided in the data argument. |
| method     | (string)<br>Specifying how the CIs should be calculated. It must equal either 'score' or 'summary score'. See details for more information about the implementation differences.                                                                                               |
| conf.level | (scalar numeric)<br>a scalar in (0,1) indicating the confidence level. Default is 0.95                                                                                                                                                                                         |
| delta      | (numeric)<br>Optionally a single number or a vector of numbers between -1 and 1 (not inclusive) to set the difference between two groups under the null hypothesis. If provided, the function returns the test statistic and p-value under the delta hypothesis.               |

data (data.frame)  
Optional data frame containing the variables specified in x and by.

### Details

The function implements the stratified Miettinen-Nurminen method to compute confidence intervals for the difference between two proportions across multiple strata.

$$H_0 : \hat{d} - \delta \leq 0 \quad \text{vs.} \quad H_1 : \hat{d} - \delta > 0$$

The "score" method is a weighted MN score first described in the original 1985 paper. The formula is:

- Calculates weights for each stratum as  $w_i = \frac{n_{xi} \cdot n_{yi}}{n_{xi} + n_{yi}}$
- Computes the overall weighted difference  $\hat{d} = \frac{\sum w_i \hat{p}_{xi}}{\sum w_i} - \frac{\sum w_i \hat{p}_{yi}}{\sum w_i}$
- Uses the stratified test statistic:

$$Z_\delta = \frac{\hat{d} - \delta}{\sqrt{\sum_{i=1}^k \left( \frac{w_i}{\sum w_i} \right)^2 \cdot \hat{\sigma}_{mn}^2(d)}}$$

- Finds the range of all values of  $\delta$  for which the stratified test statistic ( $Z_\delta$ ) falls in the acceptance region  $\{Z_\delta < z_{\alpha/2}\}$

The  $\hat{\sigma}_{mn}^2(\hat{d})$  is the Miettinen-Nurminen variance estimate. See the details of [ci\\_prop\\_diff\\_mn\(\)](#) for how  $\hat{\sigma}_{mn}^2(\delta)$  is calculated.

The "summary score" method follows the meta-analyses proposed in Agresti 2013 and is consistent with the "Summary Score Confidence Limits" method used in SAS. The formula is:

- The point estimate of the stratified risk difference is a weighted average of the midpoints of the within-stratum MN confidence intervals:

$$\hat{d}_S = \sum_i \hat{d}_i w_i$$

- Define  $s_i$  as the width of the CI for the  $i$ th stratum divided by  $2 \times z_{\alpha/2}$  and then stratum weights are given by

$$w_i = \left( \frac{1}{s_i^2} \right) / \sum_i \left( \frac{1}{s_i^2} \right)$$

- The variance of  $\hat{d}_S$  is computed as

$$\widehat{\text{Var}}(\hat{d}_S) = \frac{1}{\sum_i \left( \frac{1}{s_i^2} \right)}$$

- Confidence limits for the stratified risk difference estimate are

$$\hat{d}_S \pm \left( z_{\alpha/2} \times \widehat{\text{Var}}(\hat{d}_S) \right)$$

**Value**

An object containing the following components:

|            |                                                                                               |
|------------|-----------------------------------------------------------------------------------------------|
| estimate   | The point estimate of the difference in proportions ( $p_x - p_y$ )                           |
| conf.low   | Lower bound of the confidence interval                                                        |
| conf.high  | Upper bound of the confidence interval                                                        |
| conf.level | The confidence level used                                                                     |
| delta      | delta value(s) used                                                                           |
| statistic  | Z-Statistic under the null hypothesis based on the given 'delta'                              |
| p.value    | p-value under the null hypothesis based on the given 'delta'                                  |
| method     | Description of the method used ("Stratified {method} Miettinen-Nurminen Confidence Interval") |

If delta is not provided statistic and p.value will be NULL

**References**

Miettinen, O. S., & Nurminen, M. (1985). Comparative analysis of two rates. *Statistics in Medicine*, 4(2), 213-226.

**Common Risk Difference :: Base SAS(R) 9.4 Procedures Guide: Statistical Procedures, Third Edition**

Agresti, A. (2013). *Categorical Data Analysis*. 3rd Edition. John Wiley & Sons, Hoboken, NJ

**Examples**

```
# Generate binary samples with strata
responses <- expand(c(9, 3, 7, 2), c(10, 10, 10, 10))
arm <- rep(c("treat", "control"), 20)
strata <- rep(c("stratum1", "stratum2"), times = c(20, 20))

# Calculate stratified confidence interval for difference in proportions
ci_prop_diff_mn_strata(x = responses, by = arm, strata = strata)

# Using the summary score method
ci_prop_diff_mn_strata(x = responses, by = arm, strata = strata,
                      method = "summary score")

# Calculate 99% confidence interval
ci_prop_diff_mn_strata(x = responses, by = arm, strata = strata,
                      conf.level = 0.99)

# Calculate p-value under null hypothesis delta = 0.2
ci_prop_diff_mn_strata(x = responses, by = arm, strata = strata,
                      delta = 0.2)
```

---

|                   |                                                               |
|-------------------|---------------------------------------------------------------|
| ci_prop_diff_wald | <i>Wald Confidence Interval for Difference in Proportions</i> |
|-------------------|---------------------------------------------------------------|

---

### Description

Calculates the Wald interval by following the usual textbook definition for a difference in proportions confidence interval using the normal approximation.

### Usage

```
ci_prop_diff_wald(x, by, conf.level = 0.95, correct = FALSE, data = NULL)
```

### Arguments

|            |                                                                                                                                                                                         |
|------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| x          | (binary/numeric/logical)<br>vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)                                                                            |
| by         | (string)<br>A character or factor vector with exactly two unique levels identifying the two groups to compare. Can also be a column name if a data frame provided in the data argument. |
| conf.level | (scalar numeric)<br>a scalar in (0,1) indicating the confidence level. Default is 0.95                                                                                                  |
| correct    | (logical)<br>apply continuity correction.                                                                                                                                               |
| data       | (data.frame)<br>Optional data frame containing the variables specified in x and by.                                                                                                     |

### Details

$$(\hat{p}_1 - \hat{p}_2) \pm z_{\alpha/2} \sqrt{\frac{\hat{p}_1(1 - \hat{p}_1)}{n_1} + \frac{\hat{p}_2(1 - \hat{p}_2)}{n_2}}$$

### Value

An object containing the following components:

|            |                                                                 |
|------------|-----------------------------------------------------------------|
| n          | Number of responses in each by group                            |
| N          | Total number in each by group                                   |
| estimate   | The point estimate of the difference in proportions (p_1 - p_2) |
| conf.low   | Lower bound of the confidence interval                          |
| conf.high  | Upper bound of the confidence interval                          |
| conf.level | The confidence level used                                       |
| method     | Type of method used                                             |

**Examples**

```

responses <- expand(c(9, 3), c(10, 10))
arm <- rep(c("treat", "control"), times = c(10, 10))

# Calculate 95% confidence interval for difference in proportions
ci_prop_diff_wald(x = responses, by = arm)

```

---

|                  |                    |
|------------------|--------------------|
| ci_prop_jeffreys | <i>Jeffreys CI</i> |
|------------------|--------------------|

---

**Description**

Calculates the Jeffreys interval, an equal-tailed interval based on the non-informative Jeffreys prior for a binomial proportion.

**Usage**

```
ci_prop_jeffreys(x, conf.level = 0.95, data = NULL)
```

**Arguments**

|            |                                                                                                              |
|------------|--------------------------------------------------------------------------------------------------------------|
| x          | (binary/numeric/logical)<br>vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1) |
| conf.level | (scalar numeric)<br>a scalar in (0,1) indicating the confidence level. Default is 0.95                       |
| data       | (data.frame)<br>Optional data frame containing the variables specified in x and by.                          |

**Details**

$$\left( \text{Beta} \left( \frac{k}{2} + \frac{1}{2}, \frac{n-k}{2} + \frac{1}{2} \right)_{\alpha}, \text{Beta} \left( \frac{k}{2} + \frac{1}{2}, \frac{n-k}{2} + \frac{1}{2} \right)_{1-\alpha} \right)$$

**Value**

An object containing the following components:

|            |                                        |
|------------|----------------------------------------|
| n          | Number of responses                    |
| N          | Total number                           |
| estimate   | The point estimate of the proportion   |
| conf.low   | Lower bound of the confidence interval |
| conf.high  | Upper bound of the confidence interval |
| conf.level | The confidence level used              |
| method     | Type of method used                    |

ci\_prop\_wald

*Wald CI***Description**

Calculates the Wald interval by following the usual textbook definition for a single proportion confidence interval using the normal approximation.

**Usage**

```
ci_prop_wald(x, conf.level = 0.95, correct = FALSE, data = NULL)
```

**Arguments**

|            |                                                                                                              |
|------------|--------------------------------------------------------------------------------------------------------------|
| x          | (binary/numeric/logical)<br>vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1) |
| conf.level | (scalar numeric)<br>a scalar in (0,1) indicating the confidence level. Default is 0.95                       |
| correct    | (logical)<br>apply continuity correction.                                                                    |
| data       | (data.frame)<br>Optional data frame containing the variables specified in x and by.                          |

**Details**

$$\hat{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}}$$

**Value**

An object containing the following components:

|            |                                        |
|------------|----------------------------------------|
| n          | Number of responses                    |
| N          | Total number                           |
| estimate   | The point estimate of the proportion   |
| conf.low   | Lower bound of the confidence interval |
| conf.high  | Upper bound of the confidence interval |
| conf.level | The confidence level used              |
| method     | Type of method used                    |

Examples

```
# example code
x <- c(
  TRUE, TRUE, TRUE, TRUE, TRUE,
  FALSE, FALSE, FALSE, FALSE, FALSE
)

ci_prop_wald(x, conf.level = 0.9)
```

---

|                |           |
|----------------|-----------|
| ci_prop_wilson | Wilson CI |
|----------------|-----------|

---

Description

Calculates the Wilson interval by calling `stats::prop.test()`. Also referred to as Wilson score interval.

Usage

```
ci_prop_wilson(x, conf.level = 0.95, correct = FALSE, data = NULL)
```

Arguments

- x (binary/numeric/logical)  
vector of a binary values, i.e. a logical vector, or numeric with values `c(0, 1)`
- conf.level (scalar numeric)  
a scalar in (0,1) indicating the confidence level. Default is 0.95
- correct (logical)  
apply continuity correction.
- data (data.frame)  
Optional data frame containing the variables specified in x and by.

Details

$$\frac{\hat{p} + \frac{z_{\alpha/2}^2}{2n} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n} + \frac{z_{\alpha/2}^2}{4n^2}}}{1 + \frac{z_{\alpha/2}^2}{n}}$$

Value

An object containing the following components:

- n Number of responses
- N Total number
- estimate The point estimate of the proportion

|            |                                        |
|------------|----------------------------------------|
| conf.low   | Lower bound of the confidence interval |
| conf.high  | Upper bound of the confidence interval |
| conf.level | The confidence level used              |
| method     | Type of method used                    |

---

ci\_prop\_wilson\_strata *Stratified Wilson CI*

---

### Description

Calculates the stratified Wilson confidence interval for unequal proportions as described in Xin YA, Su XG. Stratified Wilson and Newcombe confidence intervals for multiple binomial proportions. *Statistics in Biopharmaceutical Research*. 2010;2(3).

### Usage

```
ci_prop_wilson_strata(
  x,
  strata,
  weights = NULL,
  conf.level = 0.95,
  max.iterations = 10L,
  correct = FALSE,
  data = NULL
)
```

### Arguments

|                |                                                                                                                                                                                                                                                                                |
|----------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| x              | (binary/numeric/logical)<br>vector of a binary values, i.e. a logical vector, or numeric with values c(0, 1)                                                                                                                                                                   |
| strata         | (numeric)<br>A vector specifying the stratum for each observation. It needs to be the length of x or a multiple of x if multiple levels of strata are present. Can also be a column name (or vector of column names NOT quoted) if a data frame provided in the data argument. |
| weights        | (numeric)<br>weights for each level of the strata. If NULL, they are estimated using the iterative algorithm that minimizes the weighted squared length of the confidence interval.                                                                                            |
| conf.level     | (scalar numeric)<br>a scalar in (0,1) indicating the confidence level. Default is 0.95                                                                                                                                                                                         |
| max.iterations | (positive integer)<br>maximum number of iterations for the iterative procedure used to find estimates of optimal weights.                                                                                                                                                      |

|         |                                                                                                                                      |
|---------|--------------------------------------------------------------------------------------------------------------------------------------|
| correct | (scalar logical)<br>include the continuity correction. For further information, see for example <a href="#">stats::prop.test()</a> . |
| data    | (data.frame)<br>Optional data frame containing the variables specified in x and by.                                                  |

## Details

$$\frac{\hat{p}_j + \frac{z_{\alpha/2}^2}{2n_j} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}_j(1-\hat{p}_j)}{n_j} + \frac{z_{\alpha/2}^2}{4n_j^2}}}{1 + \frac{z_{\alpha/2}^2}{n_j}}$$

## Value

An object containing the following components:

|            |                                                                                                                               |
|------------|-------------------------------------------------------------------------------------------------------------------------------|
| n          | Number of responses                                                                                                           |
| N          | Total number                                                                                                                  |
| estimate   | The point estimate of the proportion                                                                                          |
| conf.low   | Lower bound of the confidence interval                                                                                        |
| conf.high  | Upper bound of the confidence interval                                                                                        |
| conf.level | The confidence level used                                                                                                     |
| weights    | Weights of each strata, will be the same as the input unless unspecified, then it will be the dynamically calculated weights. |
| method     | Type of method used                                                                                                           |

## Examples

```
# Stratified Wilson confidence interval with unequal probabilities

set.seed(1)
rsp <- sample(c(TRUE, FALSE), 100, TRUE)
strata_data <- data.frame(
  x = sample(c(TRUE, FALSE), 100, TRUE),
  "f1" = sample(c("a", "b"), 100, TRUE),
  "f2" = sample(c("x", "y", "z"), 100, TRUE),
  stringsAsFactors = TRUE
)
strata <- interaction(strata_data)
n_strata <- ncol(table(rsp, strata)) # Number of strata

ci_prop_wilson_strata(
  x = rsp, strata = strata,
  conf.level = 0.90
)

# Not automatic setting of weights
```

```
ci_prop_wilson_strata(
  x = rsp, strata = strata,
  weights = rep(1 / n_strata, n_strata),
  conf.level = 0.90
)
```

---

 expand

---

*Expand Count Data into Binary Vectors*


---

### Description

Converts count data (number of successes and total sample size) into a binary vector of TRUE/FALSE values. This is useful for converting summary statistics back into raw data format for analysis functions that require individual-level data.

### Usage

```
expand(x, n)
```

### Arguments

|   |                                                                                |
|---|--------------------------------------------------------------------------------|
| x | Integer (or vector of integers) representing the number of successes.          |
| n | Integer (or vector of integers) representing the total number of participants. |

### Details

For each pair of values in x and n, the function creates a vector with x TRUE values followed by n-x FALSE values. If multiple pairs are provided, the resulting vectors are concatenated in order.

### Value

A logical vector where TRUE represents a success and FALSE represents a failure. The length of the vector equals the sum of all sample sizes.

### Examples

```
# Convert 4 successes out of 13 participants to binary data
expand(4, 13)

# Convert multiple groups of data
# Group 1: 9 successes out of 10
# Group 2: 3 successes out of 10
expand(c(9, 3), c(10, 10))
```

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