

Package ‘bayesdistreg’

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Type Package

Title Bayesian Distribution Regression

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Description Implements Bayesian Distribution Regression methods. This package contains functions for three estimators (non-asymptotic, semi-asymptotic and asymptotic) and related routines for Bayesian Distribution Regression in Huang and Tsayawo (2018) <[doi:10.2139/ssrn.3048658](https://doi.org/10.2139/ssrn.3048658)> which is also the recommended reference to cite for this package. The functions can be grouped into three (3) categories. The first computes the logit likelihood function and posterior densities under uniform and normal priors. The second contains Independence and Random Walk Metropolis-Hastings Markov Chain Monte Carlo (MCMC) algorithms as functions and the third category of functions are useful for semi-asymptotic and asymptotic Bayesian distribution regression inference.

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asymcnfB	<i>Asymmetric simultaneous bayesian confidence bands</i>
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Description

asymcnfB obtains asymmetric bayesian distribution confidence bands

Usage

```
asymcnfB(DF, DFmat, alpha = 0.05, scale = FALSE)
```

Arguments

DF	the target distribution/quantile function as a vector
DFmat	the matrix of draws of the distribution, rows correspond to elements in DF
alpha	level such that 1-alpha is the desired probability of coverage
scale	logical for scaling using the inter-quartile range

Value

cstar - a constant to add and subtract from DF to create confidence bands if no scaling=FALSE else a vector of length DF.

Examples

```
set.seed(14); m=matrix(rbeta(500,1,4),nrow = 5) + 1:5
DF = apply(m,1,mean); plot(1:5,DF,type="l",ylim = c(min(m),max(m)), xlab = "Index")
asyCB<- asymcnfB(DF,DFmat = m)
lines(1:5,DF-asyCB$cmin,lty=2); lines(1:5,DF+asyCB$cmax,lty=2)
```

distreg

Bayesian distribution regression

Description

distreg draws randomly from the density of $F(y_0)$ at a threshold value y_0

Usage

```
distreg(thresh, data0, MH = "IndepMH", ...)
```

Arguments

thresh	threshold value that is used to binarise the continuous outcome variable
data0	original data set with the first column being the continuous outcome variable
MH	metropolis-hastings algorithm to use; default:"IndepMH", alternative "RWMH"
...	any additional inputs to pass to the MH algorithm

Value

fitob a vector of fitted values corresponding to the distribution at threshold thresh

Examples

```
data0=faithful[,c(2,1)]; qnt<-quantile(data0[,1],0.25)
distob<- distreg(qnt,data0,iter = 102, burn = 2);
plot(density(distob,.1),main="Kernel density plot")
```

distreg.asymp *Asymptotic distribution regression*

Description

`distreg.asymp` takes input object from `dr_asymp()` for asymptotic bayesian distribution.

Usage

```
distreg.asymp(ind, drabj, data, vcovfn = "vcov", ...)
```

Arguments

ind	index of object in list <code>drabj</code> (i.e. a threshold value) from which to take draws
drabj	object from <code>dr_asymp()</code>
data	dataframe, first column is the outcome
vcovfn	a string denoting the function to extract the variance-covariance. Defaults at "vcov". Other variance-covariance estimators in the sandwich package are usable.
...	additional input to pass to <code>vcovfn</code>

Value

a mean `Fhat` and a variance `varF`

Examples

```
y = faithful$waiting
x = scale(cbind(faithful$eruptions, faithful$eruptions^2))
qtaus = quantile(y,c(0.05,0.25,0.5,0.75,0.95))
drabj<- dr_asymp(y=y,x=x,thresh = qtaus); data = data.frame(y,x)
(asymp.obj<- distreg.asymp(ind=2,drabj,data,vcovfn="vcov"))
```

distreg.sas *Semi-asymptotic bayesian distribution*

Description

`distreg.sas` takes input object from `dr_asymp()` for semi asymptotic bayesian distribution. This involves taking random draws from the normal approximation of the posterior at each threshold value.

Usage

```
distreg.sas(ind, drabj, data, vcovfn = "vcov", iter = 100)
```

Arguments

ind	index of object in list drabj (i.e. a threshold value) from which to take draws
drabj	object from dr_asympar()
data	dataframe, first column is the outcome
vcovfn	a string denoting the function to extract the variance-covariance. Defaults at "vcov". Other variance-covariance estimators in the sandwich package are usable.
iter	number of draws to simulate

Value

fitob vector of random draws from density of F(yo) using semi-asymptotic BDR

Examples

```
y = faithful$waiting
x = scale(cbind(faithful$eruptions,faithful$eruptions^2))
qtaus = quantile(y,c(0.05,0.25,0.5,0.75,0.95))
drabj<- dr_asympar(y=y,x=x,thresh = qtaus); data = data.frame(y,x)
drsas1 = lapply(1:5,distreg.sas,drabj=drabj,data=data,iter=100)
drsas2 = lapply(1:5,distreg.sas,drabj=drabj,data=data,vcovfn="vcovHC",iter=100)
par(mfrow=c(3,2));invisible(lapply(1:5,function(i)plot(density(drsas1[[i]],.1))));par(mfrow=c(1,1))
par(mfrow=c(3,2));invisible(lapply(1:5,function(i)plot(density(drsas2[[i]],.1))));par(mfrow=c(1,1))
```

Description

distreg draws randomly from the density of counterfactual of F(yo) at a threshold value yo

Usage

```
distreg_cfa(thresh, data0, MH = "IndepMH", cft, cfIND, ...)
```

Arguments

thresh	threshold value that is used to binarise the continuous outcome variable
data0	original data set with the first column being the continuous outcome variable
MH	metropolis-hastings algorithm to use; default:"IndepMH", alternative "RWMH"
cft	column vector of counterfactual treatment
cfIND	the column index(indices) of treatment variable(s) to replace with cft in data0
...	any additional inputs to pass to the MH algorithm

Value

robj a list of a vector of fitted values corresponding to random draws from $F(y_0)$, counterfactual $F(y_0)$, and the parameters

Examples

```
data0=faithful[,c(2,1)]; qnt<-quantile(data0[,1],0.25)
cfIND=2 #Note: the first column is the outcome variable.
cft=0.95*data0[,cfIND] # a decrease by 5%
dist_cfa<- distreg_cfa(qnt,data0,cft,cfIND,MH="IndepMH",iter = 102, burn = 2)
par(mfrow=c(1,2)); plot(density(dist_cfa$counterfactual,.1),main="Original")
plot(density(dist_cfa$counterfactual,.1),main="Counterfactual"); par(mfrow=c(1,1))
```

distreg_cfa.sas

*Semi-asymptotic counterfactual distribution***Description**

`distreg_cfa.sas` takes input object from `dr_asympar()` for counterfactual semi asymptotic bayesian distribution. This involves taking random draws from the normal approximation of the posterior at each threshold value.

Usage

```
distreg_cfa.sas(ind, drabj, data, cft, cfIND, vcovfn = "vcov",
                 iter = 100)
```

Arguments

ind	index of object in list <code>drabj</code> (i.e. a threshold value) from which to take draws
drabj	object from <code>dr_asympar()</code>
data	dataframe, first column is the outcome
cft	column vector of counterfactual treatment
cfIND	the column index(indices) of treatment variable(s) to replace with <code>cft</code> in <code>data0</code>
vcovfn	a string denoting the function to extract the variance-covariance. Defaults at "vcov". Other variance-covariance estimators in the sandwich package are usable.
iter	number of draws to simulate

Value

fitob vector of random draws from density of $F(y_0)$ using semi-asymptotic BDR

Examples

```
y = faithful$waiting
x = scale(cbind(faithful$eruptions,faithful$eruptions^2))
qtaus = quantile(y,c(0.05,0.25,0.5,0.75,0.95))
drabj<- dr_asympar(y=y,x=x,thresh = qtaus); data = data.frame(y,x)
cfIND=2 #Note: the first column is the outcome variable.
cft=0.95*data[,cfIND] # a decrease by 5%
cfa.sasobj<- distreg_cfa.sas(ind=2,drabj,data,cft,cfIND,vcovfn="vcov")
par(mfrow=c(1,2)); plot(density(cfa.sasobj$original,.1),main="Original")
plot(density(cfa.sasobj$counterfactual,.1),main="Counterfactual"); par(mfrow=c(1,1))
```

dr_asympar

Binary glm object at several threshold values

Description

dr_asympar computes a normal approximation of the likelihood at a vector of threshold values

Usage

```
dr_asympar(y, x, thresh, ...)
```

Arguments

y	outcome variable
x	matrix of covariates
thresh	vector of threshold values on the support of outcome y
...	additional arguments to pass to lapl_aprx2

Value

a list of glm objects corresponding to thresh

Examples

```
y = faithful$waiting
x = scale(cbind(faithful$eruptions,faithful$eruptions^2))
qtaus = quantile(y,c(0.05,0.25,0.5,0.75,0.95))
drabj<- dr_asympar(y=y,x=x,thresh = qtaus)
lapply(drabj,coef); lapply(drabj,vcov)
# mean and covariance at respective threshold values
```

fitdist*The distribution of mean fitted logit probabilities***Description**

`fitdist` function generates a vector of mean fitted probabilities that constitute the distribution. This involves marginalising out covariates.

Usage

```
fitdist(Matparam, data)
```

Arguments

<code>Matparam</code>	an $M \times k$ matrix of parameter draws, each being a $1 \times k$ vector
<code>data</code>	dataframe used to obtain <code>Matparam</code>

Value

dist fitted (marginalised) distribution

fitlogit*Fitted logit probabilities***Description**

`fitlogit` obtains a vector of fitted logit probabilities given parameters (`pars`) and data

Usage

```
fitlogit(pars, data)
```

Arguments

<code>pars</code>	vector of parameters
<code>data</code>	data frame. The first column of the data frame ought to be the binary dependent variable

Value

vec vector of fitted logit probabilities

IndepMH*Independence Metropolis-Hastings Algorithm*

Description

IndepMH computes random draws of parameters using a specified proposal distribution.

Usage

```
IndepMH(data, propob = NULL, posterior = NULL, iter = 1500,
        burn = 500, vscale = 1.5, start = NULL, prior = "Uniform",
        mu = 0, sig = 10)
```

Arguments

data	data required for the posterior distribution
propob	a list of mean and variance-covariance of the normal proposal distribution (default:NULL)
posterior	the posterior distribution. It is set to null in order to use the logit posterior. The user can specify log posterior as a function of parameters and data (pars,data)
iter	number of random draws desired (default: 1500)
burn	burn-in period for the MH algorithm (default: 500)
vscale	a positive value to scale up or down the variance-covariance matrix in the proposal distribution
start	starting values of parameters for the MH algorithm. It is automatically generated but the user can also specify.
prior	the prior distribution (default: "Normal", alternative: "Uniform")
mu	the mean of the normal prior distribution (default:0)
sig	the variance of the normal prior distribution (default:10)

Value

val a list of matrix of draws pardraws and the acceptance rate

Examples

```
y = indicat(faithful$waiting,70)
x = scale(cbind(faithful$eruptions,faithful$eruptions^2))
data = data.frame(y,x); propob<- lapl_aprx(y,x)
IndepMH_n<- IndepMH(data=data,propob,iter = 102, burn = 2) # prior="Normal"
IndepMH_u<- IndepMH(data=data,propob,prior="Uniform",iter = 102, burn = 2) # prior="Uniform"
par(mfrow=c(3,1));invisible(apply(IndepMH_n$Matprm,2,function(x)plot(density(x))))
invisible(apply(IndepMH_u$Matprm,2,function(x)plot(density(x))));par(mfrow=c(1,1))
```

indicat	<i>Indicator function</i>
----------------	---------------------------

Description

This function creates 0-1 indicators for a given threshold y_0 and vector y

Usage

```
indicat(y, y0)
```

Arguments

y	vector y
y0	threshold value y_0

Value

```
val
```

jdpar.asymp	<i>Joint asymptotic mutivariate density of parameters</i>
--------------------	---

Description

`jdpar.asymp` takes input object from `dr_asymp()` for asymptotic bayesian distribution. It returns objects for joint mutivariate density of parameters across several thresholds. Check for positive definiteness of the covariance matrix, else exclude thresholds yielding negative eigen values.

Usage

```
jdpar.asymp(drabj, data, jdf = FALSE, vcovfn = "vcovHC", ...)
```

Arguments

drabj	object from <code>dr_asymp()</code>
data	dataframe, first column is the outcome
jdf	logical to return joint density of $F(y_0)$ across thresholds in <code>drabj</code>
vcovfn	a string denoting the function to extract the variance-covariance. Defaults at "vcov". Other variance-covariance estimators in the sandwich package are usable.
...	additional input to pass to <code>vcovfn</code>

Value

mean vector Theta and variance-covariance matrix vcovpar of parameters across thresholds and if jdF=TRUE, a mean vector mnF and a variance-covariance matrix vcovF of F(yo)

Examples

```
y = faithful$waiting
x = scale(cbind(faithful$eruptions,faithful$eruptions^2))
qtaus = quantile(y,c(0.05,0.25,0.5,0.75,0.95))
drabj<- dr_asympar(y=y,x=x,thresh = qtaus); data = data.frame(y,x)
(drjasy = jdpar.asymp(drabj=drabj,data=data,jdF=TRUE))
```

jntCBOM

*Montiel Olea and Plagborg-Moller (2018) confidence bands***Description**

jntCBOM implements calibrated symmetric confidence bands (algorithm 2) in Montiel Olea and Plagborg-Moller (2018).

Usage

```
jntCBOM(DF, DFmat, alpha = 0.05, eps = 0.001)
```

Arguments

DF	the target distribution/quantile function as a vector
DFmat	the matrix of draws of the distribution, rows correspond to indices elements in DF
alpha	level such that 1-alpha is the desired probability of coverage
eps	steps by which the grid on 1-alpha:alpha/2 is searched.

Value

CB - confidence band, zeta - the optimal level

Examples

```
set.seed(14); m=matrix(rbeta(500,1,4),nrow = 5) + 1:5
DF = apply(m,1,mean); plot(1:5,DF,type="l",ylim = c(min(m),max(m)), xlab = "Index")
j0MCB<- jntCBOM(DF,DFmat = m)
lines(1:5,j0MCB$CB[,1],lty=2); lines(1:5,j0MCB$CB[,2],lty=2)
```

lapl_aprx*Laplace approximation of posterior to normal***Description**

This function generates mode and variance-covariance for a normal proposal distribution for the bayesian logit.

Usage

```
lapl_aprx(y, x, glmobj = FALSE)
```

Arguments

- | | |
|--------|--|
| y | the binary dependent variable y |
| x | the matrix of independent variables. |
| glmobj | logical for returning the logit glm object |

Value

val A list of mode variance-covariance matrix, and scale factor for proposal draws from the multivariate normal distribution.

Examples

```
y = indicat(faithful$waiting,mean(faithful$waiting))
x = scale(cbind(faithful$eruptions,faithful$eruptions^2))
gg<- lapl_aprx(y,x)
```

lapl_aprx2*Laplace approximation of posterior to normal***Description**

lapl_aprx2 is a more flexible alternative to **lapl_aprx**. This creates **glm** objects from which joint asymptotic distributions can be computed.

Usage

```
lapl_aprx2(y, x, family = "binomial", ...)
```

Arguments

y	the binary dependent variable y
x	the matrix of independent variables.
family	a parameter to be passed <code>glm()</code> , defaults to the logit model
...	additional parameters to be passed to <code>glm()</code>

Value

val A list of mode variance-covariance matrix, and scale factor for proposal draws from the multivariate normal distribution.

Examples

```
y = indicat(faithful$waiting,mean(faithful$waiting))
x = scale(cbind(faithful$eruptions,faithful$eruptions^2))
(gg<- lapl_aprx2(y,x)); coef(gg); vcov(gg)
```

logit	<i>Logit likelihood function</i>
-------	----------------------------------

Description

`logit` is the logistic likelihood function given data.

Usage

```
logit(start, data, Log = TRUE)
```

Arguments

start	vector of starting values
data	dataframe. The first column should be the dependent variable.
Log	a logical input (defaults to <code>True</code>) to take the log of the likelihood.

Value

`like` returns the likelihood function value.

Examples

```
y = indicat(faithful$waiting,mean(faithful$waiting))
x = scale(cbind(faithful$eruptions,faithful$eruptions^2))
data = data.frame(y,x)
logit(rep(0,3),data)
```

LogitLink*Logit function***Description**

This is the link function for logit regression

Usage

```
LogitLink(x)
```

Arguments

x	Random variable
---	-----------------

Value

val Probability value from the logistic function

parLply*Parallel compute***Description**

parLply uses parLapply from the parallel package with a function as input

Usage

```
parLply(vec, fn, type = "FORK", no_cores = 1, ...)
```

Arguments

vec	vector of inputs over which to parallel compute
fn	the function
type	this option is set to "FORK", use "PSOCK" on windows
no_cores	the number of cores to use. Defaults at 1
...	extra inputs to fn()

Value

out parallel computed output

par_distreg

*Parallel compute bayesian distribution regression***Description**

par_distreg uses parallel computation to compute bayesian distribution regression for a given vector of threshold values and a data (with first column being the continuous outcome variable)

Usage

```
par_distreg(thresh, data0, fn = distreg, no_cores = 1,
            type = "PSOCK", ...)
```

Arguments

thresh	vector of threshold values.
data0	the original data set with a continous dependent variable in the first column
fn	bayesian distribution regression function. the default is distreg provided in the package
no_cores	number of cores for parallel computation
type	type passed to makeCluster() in the package parallel
...	any additional input parameters to pass to fn

Value

mat a G x M matrix of output (G is the length of thresh, M is the number of draws)

Examples

```
data0=faithful[,c(2,1)]; qnts<-quantile(data0[,1],c(0.05,0.25,0.5,0.75,0.95))
out<- par_distreg(qnts,data0,no_cores=1,iter = 102, burn = 2)
par(mfrow=c(3,2));invisible(apply(out,1,function(x)plot(density(x,30))));par(mfrow=c(1,1))
```

posterior

*Posterior distribution***Description**

posterior computes the value of the posterior at parameter values pars

Usage

```
posterior(pars, data, Log = TRUE, mu = 0, sig = 25,
          prior = "Normal")
```

Arguments

pars	parameter values
data	dataframe. The first column must be the binary dependent variable
Log	logical to take the log of the posterior.(defaults to TRUE)
mu	mean of prior of each parameter value in case the prior is Normal (default: 0)
sig	standard deviation of prior of each parameter in case the prior is Normal (default: 25)
prior	string input of "Normal" or "Uniform" prior distribution to use

Value

val value function of the posterior

Examples

```
y = indicat(faithful$waiting,mean(faithful$waiting))
x = scale(cbind(faithful$eruptions,faithful$eruptions^2))
data = data.frame(y,x)
posterior(rep(0,3),data,Log = FALSE,mu=0,sig = 10,prior = "Normal") # no log
posterior(rep(0,3),data,Log = TRUE,mu=0,sig = 10,prior = "Normal") # log
posterior(rep(0,3),data,Log = TRUE) # use default values
```

prior_n*Normal Prior distribution***Description**

This normal prior distribution is a product of univariate N(mu,sig)

Usage

```
prior_n(pars, mu, sig, Log = FALSE)
```

Arguments

pars	parameter values
mu	mean value of each parameter value
sig	standard deviation of each parameter value
Log	logical to take the log of prior or not (defaults to FALSE)

Value

val Product of probability values for each parameter

Examples

```
prior_n(rep(0,6),0,10,Log = TRUE) #log of prior
prior_n(rep(0,6),0,10,Log = FALSE) #no log
```

prior_u

*Uniform Prior distribution***Description**

This uniform prior distribution proportional to 1

Usage

```
prior_u(pars)
```

Arguments

pars	parameter values
-------------	------------------

Value

val value of joint prior =1 for the uniform prior

quant_bdr

*Quantile conversion of a bayesian distribution matrix***Description**

quant_bdr converts a bayesian distribution regression matrix from par_distreg() output to a matrix of quantile distribution.

Usage

```
quant_bdr(taus, thresh, mat)
```

Arguments

taus	a vector of quantile indices
thresh	a vector of threshold values used in a par_distreg() type function
mat	bayesian distribution regression output matrix

Value

qmat matrix of quantile distribution

RWMH

*Random Walk Metropolis-Hastings Algorithm***Description**

RWMH computes random draws of parameters using a specified proposal distribution. The default is the normal distribution

Usage

```
RWMH(data, propob = NULL, posterior = NULL, iter = 1500,
      burn = 500, vscale = 1.5, start = NULL, prior = "Normal",
      mu = 0, sig = 10)
```

Arguments

data	data required for the posterior distribution. First column is the outcome
propob	a list of mean and variance-covariance of the normal proposal distribution (default: NULL i.e. internally generated)
posterior	the posterior distribution. It is set to null in order to use the logit posterior. The user can specify log posterior as a function of parameters and data (pars,data)
iter	number of random draws desired
burn	burn-in period for the Random Walk MH algorithm
vscale	a positive value to scale up or down the variance-covariance matrix in the proposal distribution
start	starting values of parameters for the MH algorithm. It is automatically generated from the proposal distribution but the user can also specify.
prior	the prior distribution (default: "Normal", alternative: "Uniform")
mu	the mean of the normal prior distribution (default:0)
sig	the variance of the normal prior distribution (default:10)

Value

val a list of matrix of draws Matparam and the acceptance rate

Examples

```
y = indicat(faithful$waiting,70)
x = scale(cbind(faithful$eruptions,faithful$eruptions^2))
data = data.frame(y,x); propob<- lapl_aprx(y,x)
RWMHob_n<- RWMH(data=data,propob,iter = 102, burn = 2) # prior="Normal"
RWMHob_u<- RWMH(data=data,propob,prior="Uniform",iter = 102, burn = 2)
par(mfrow=c(3,1));invisible(apply(RWMHob_n$Matparam,2,function(x)plot(density(x))))
invisible(apply(RWMHob_u$Matparam,2,function(x)plot(density(x))));par(mfrow=c(1,1))
```

simcnfB*Symmetric simultaneous bayesian confidence bands*

Description

simcnfB obtains symmetric bayesian distribution confidence bands

Usage

```
simcnfB(DF, DFmat, alpha = 0.05, scale = FALSE)
```

Arguments

DF	the target distribution/quantile function as a vector
DFmat	the matrix of draws of the distribution, rows correspond to elements in DF
alpha	level such that 1-alpha is the desired probability of coverage
scale	logical for scaling using the inter-quartile range

Value

cstar - a constant to add and subtract from DF to create confidence bands if no scaling=FALSE else a vector of length DF.

Examples

```
set.seed(14); m=matrix(rbeta(500,1,4),nrow = 5) + 1:5
DF = apply(m,1,mean); plot(1:5,DF,type="l",ylim = c(0,max(m)), xlab = "Index")
symCB<- simcnfB(DF,DFmat = m)
lines(1:5,DF-symCB,lty=2); lines(1:5,DF+symCB,lty=2)
```

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