Package 'HDMAADMM'

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Type Package

Title ADMM for High-Dimensional Mediation Models

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Description We use the Alternating Direction Method of Multipliers (ADMM) for parameter estimation in high-dimensional, single-modality mediation models. To improve the sensitivity and specificity of estimated mediation effects, we offer the sure independence screening (SIS) function for dimension reduction. The available penalty options include Lasso, Elastic Net, Pathway Lasso, and Network-constrained Penalty. The methods employed in the package are based on Boyd, S., Parikh, N., Chu, E., Peleato, B., & Eckstein, J. (2011). <doi:10.1561/2200000016>, Fan, J., & Lv, J. (2008) <doi:10.1111/j.1467-9868.2008.00674.x>, Li, C., & Li, H. (2008) <doi:10.1093/bioinformatics/btn081>, Tibshirani, R. (1996) <doi:10.1111/j.2517-6161.1996.tb02080.x>, Zhao, Y., & Luo, X. (2022) <doi:10.4310/21-sii673>, and Zou, H., & Hastie, T. (2005) <doi:10.1111/j.1467-9868.2005.00503.x>.

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LinkingTo Rcpp, RcppEigen

Suggests roxygen2

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BugReports https://github.com/psyen0824/HDMAADMM/issues

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Description

This package enables the estimation of single-modality high-dimensional mediation models. We employ penalized maximum likelihood and solve the estimation using the Alternating Direction Method of Multipliers (ADMM) to provide high-dimensional mediator estimates. To improve the sensitivity and specificity of non-zero mediators, we offer the sure independence screening (SIS) function for dimension reduction. The available penalty options include Lasso, Elastic Net, Pathway Lasso, and Network-constrained Penalty.

References

1. Tibshirani, R. (1996). Regression Shrinkage and Selection via the Lasso. Journal of the Royal Statistical Society. Series B (Methodological), 58(1), 267–288.

2. Zou, H., & Hastie, T. (2005). Regularization and Variable Selection via the Elastic Net. Journal of the Royal Statistical Society. Series B (Statistical Methodology), 67(2), 301–320.

3. Li, C., Li, H. (2008). Network-constrained regularization and variable selection for analysis of genomic data, Bioinformatics, 24(9), 1175–1182,

4. Zhao, Y., & Luo, X. (2022). Pathway Lasso: pathway estimation and selection with high-dimensional mediators. Statistics and its interface, 15(1), 39.

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cvSingleModalityAdmm   *Cross Validation for High-dimensional Single Mediation Models*

Description

Cross Validation for High-dimensional Single Mediation Models

Usage

```
cvSingleModalityAdmm(
  X,
  Y,
  M1,
  numFolds = 10,
  typeMeasure = "rmse",
  lambda1a,
  lambda1b,
  lambda1g,
  lambda2a,
  lambda2b,
  rho = 1,
  penalty = "ElasticNet",
  penaltyParameterList = list(),
  SIS = FALSE,
  SISThreshold = 2,
  maxIter = 3000,
  tol = 1e-04,
  verbose = FALSE,
  debug = FALSE
)
```

Arguments

X	The matrix of independent variables (exposure/treatment/group).
Y	The vector of dependent variable (outcome response).
M1	The single-modality mediator.
numFolds	The number of folds. The default is 10. Although nfolds can be as large as the sample size (leave-one-out CV), it is not recommended for large datasets. Smallest value allowable is nfolds=3.
typeMeasure	Default is "rmse".
rho, lambda1g, lambda1a, lambda1b, lambda2a, lambda2b, penaltyParameterList	
	Allow to put sequences for each parameter. Please refer to the function, `singleModalityAdmm` for the details.
penalty, SIS, SISThreshold, maxIter, tol, verbose, debug	
	Please refer to the function, `singleModalityAdmm`.

Value

An `cvSingleModalityAdmm` object which is a matrix containing all the combinations of parameter sequences with an additional column called `measure`.

Examples

```
## Generate Empirical Data
```

```
simuData <- modalityMediationDataGen(seed = 20231201)

## Cross-Validation for ElasticNet penalty
cvElasticNetResults <- cvSingleModalityAdmm(
  X = simuData$MediData$X, Y = simuData$MediData$Y, M1 = simuData$MediData$M1,
  numFolds = 5, typeMeasure = "rmse",
  rho = c(0.9, 1, 1.1), lambda1a = c(0.1, 0.5, 1), lambda1b = c(0.1, 0.3),
  lambda1g = c(1, 2), lambda2a = c(0.5, 1), lambda2b = c(0.5, 1),
  penalty = "ElasticNet"
)

## Cross-Validation for Pathway Lasso penalty (lambda2a, lambda2b are not tuned.)
cvPathwayLassoResults <- cvSingleModalityAdmm(
  X = simuData$MediData$X, Y = simuData$MediData$Y, M1 = simuData$MediData$M1,
  numFolds = 5, typeMeasure = "rmse",
  rho = c(0.9, 1, 1.1), lambda1a = c(0.1, 0.5, 1), lambda1b = c(0.1, 0.3),
  lambda1g = c(1, 2), lambda2a = 1, lambda2b = 1,
  penalty = "PathwayLasso", penaltyParameterList = list(kappa = c(0.5, 1), nu = c(1, 2))
)
```

---

fitted.SingleModalityAdmm

Fitted Response of SingleModalityAdmm Fits

Description

Fitted Response of SingleModalityAdmm Fits

Usage

```
## S3 method for class 'SingleModalityAdmm'
fitted(object, ...)
```

Arguments

object	A fitted obejct of class inheriting from SingleModalityAdmm.
...	further arguments passed to or from other methods.

Value

fitted.SingleModalityAdmm returns a vector which is fitted values.

modalityMediationDataGen

Data Generation for High-Dimensional Mediation Model

Description

Data Generation for High-Dimensional Mediation Model

Usage

```
modalityMediationDataGen(
  n = 100,
  p = 50,
  sigmaY = 1,
  sizeNonZero = c(3, 3, 4),
  alphaMean = c(6, 4, 2),
  alphaSd = 0.1,
  betaMean = c(6, 4, 2),
  betaSd = 0.1,
  sigmaM1 = NULL,
  gamma = 3,
  generateLaplacianMatrix = FALSE,
  seed = 20231201
)
```

Arguments

n	The number of subjects for the high-dimensional mediation model)
p	The number of high-dimensional mediators.
sigmaY	The argument "sigmaY" represents the standard deviation (SD) of the error distribution for the dependent variable.
sizeNonZero	The number of nonzero mediators. Here, we provide simulated scenarios that could produce large, medium, and small mediated effects, generating from a normal distribution.
alphaMean, alphaSd	
	The mean and SD vector of the effect between the mediator and independent variable.
betaMean, betaSd	
	The mean and SD vector of the effect between the mediator and dependent variable.
sigmaM1	The covariance matrix of the error distribution among mediators. Default is `diag(p)`.
gamma	The true value of direct effect.
generateLaplacianMatrix	
	A logical value to specify whether to generate Laplacian matrix for network penalty.
seed	The random seed. Default is NULL to use the current seed.

Value

A object with three elements.

- MediData: The simulated data for high-dimensional mediation model.

- MediPara: The true value for mediated effect and direct effect.

- Info : The output includes random seed, parameter setting, and Laplacian matrix for generating mediation model.

Examples

```
simuData <- modalityMediationDataGen(seed = 20231201)
```

---

predict.SingleModalityAdmm

Predict Method for SingleModalityAdmm Fits

Description

Predict Method for SingleModalityAdmm Fits

Usage

```
## S3 method for class 'SingleModalityAdmm'
predict(object, newdata, ...)
```

Arguments

object	A fitted obejct of class inheriting from `SingleModalityAdmm`.
newdata	Default is `NULL`. A matrix with variables to predict.
...	further arguments passed to or from other methods.

Value

predict.SingleModalityAdmm returns a vector which is the predicted values based on `newdata`.

singleModalityAdmm   *High-dimensional Single Modality Mediation Models*

Description

High-dimensional Single Modality Mediation Models

Usage

```
singleModalityAdmm(
  X,
  Y,
  M1,
  rho = 1,
  lambda1a,
  lambda1b,
  lambda1g,
  lambda2a,
  lambda2b,
  penalty = "ElasticNet",
  penaltyParameterList = list(),
  SIS = FALSE,
  SISThreshold = 2,
  maxIter = 3000L,
  tol = 0.001,
  verbose = FALSE,
  verboseOptions = list(numIter = 10L, numAlpha = 1L, numBeta = 1L, numGamma = 1L)
)
```

Arguments

X	The matrix of independent variables (exposure/treatment/group).
Y	The vector of dependent variable (outcome response).
M1	The single-modality mediator.
rho	The augmented Lagrangian parameter for ADMM.
lambda1a	The L1-norm penalty for the effect between mediator and independent variables.
lambda1b	The L1-norm penalty for the effect between mediator and dependent variable.
lambda1g	The L1-norm penalty for the direct effect. Default is **10** to adress overestimate issue.
lambda2a	The L2-norm penalty for the effect between mediator and independent variables. It's not used when Penalty is `PathwayLasso`.
lambda2b	The L2-norm penalty for the effect between mediator and dependent variable. It's not used when Penalty is `PathwayLasso`.

| penalty | A string to specify the penalty. Default is `ElasticNet`. Possible methods are Elastic Net (`ElasticNet`), Pathway Lasso (`PathywayLasso`), and Network-constrained Penalty (`Network`). |

penaltyParameterList

- Penalty=`PathwayLasso` needs two parameters.
  - kappa The L1-norm penalty for pathway Lasso.
  - nu The L2-norm penalty for pathway Lasso.
- Penalty=`Network` needs one parameter.
  - laplacianMatrix The Laplacian matrix applied on network penalty.
- Penalty=`ElasticNet` don't need other parameters.

SIS	A logical value to specify whether to perform sure independence screening (SIS).
SISThreshold	The threshold value for the target reduced dimension for mediators. The default is "2," which reduces the dimension to 2*n/log(n).
maxIter	The maximum iterations. Default is `3000`.
tol	The tolerence of convergence threshold. Default is `1e-3`.
verbose	A logical value to specify whether to print the iteration process.
verboseOptions	A list of values:

- numIter: The number of iterations to print.
- numAlpha: The number of `alpha` to print.
- numBeta: The number of `beta` to print.
- numGamma: The number of `gamma` to print.

Value

A object, SingleModalityAdmm, with three elements.

- gamma: estimated direct effect.
- alpha: estimate effect between mediator and independent variables.
- beta : estimate effect between mediator and dependent variable.

Examples

```
## Generate Empirical Data
simuData <- modalityMediationDataGen(seed = 20231201, generateLaplacianMatrix = TRUE)

## Parameter Estimation for ElasticNet penalty
modelElasticNet <- singleModalityAdmm(
  X = simuData$MediData$X, Y = simuData$MediData$Y, M1 = simuData$MediData$M1,
  rho = 1, lambda1a = 1, lambda1b = 0.1, lambda1g = 2, lambda2a = 1, lambda2b = 1,
  penalty = "ElasticNet"
)

# fitted & predict
fitted(modelElasticNet)
predict(modelElasticNet, matrix(c(0, 1), ncol=1))
```

```
## Parameter Estimation for Pathway Lasso penalty
modelPathwayLasso <- singleModalityAdmm(
  X = simuData$MediData$X, Y = simuData$MediData$Y, M1 = simuData$MediData$M1,
  rho = 1, lambda1a = 1, lambda1b = 0.1, lambda1g = 2, lambda2a = 1, lambda2b = 1,
  penalty = "PathwayLasso", penaltyParameterList = list(kappa = 1, nu = 2)
)

## Parameter Estimation for Network penalty
modelNetwork <- singleModalityAdmm(
  X = simuData$MediData$X, Y = simuData$MediData$Y, M1 = simuData$MediData$M1,
  rho = 1, lambda1a = 1, lambda1b = 0.1, lambda1g = 2, lambda2a = 1, lambda2b = 1,
 penalty = "Network", penaltyParameterList = list(laplacianMatrix = simuData$Info$laplacianMatrix)
)

## Parameter Estimation for Network penalty with a customized Laplacian matrix
set.seed(20231201)
p <- ncol(simuData$MediData$M1)
W <- matrix(0, nrow = p, ncol = p)
W[lower.tri(W)] <- runif(p*(p-1)/2, 0, 1)
W[upper.tri(W)] <- t(W)[upper.tri(W)]
diag(W) <- 1
L <- weightToLaplacian(W)
modelNetwork <- singleModalityAdmm(
  X = simuData$MediData$X, Y = simuData$MediData$Y, M1 = simuData$MediData$M1,
  rho = 1, lambda1a = 1, lambda1b = 0.1, lambda1g = 2, lambda2a = 1, lambda2b = 1,
  penalty = "Network", penaltyParameterList = list(laplacianMatrix = L)
)

## With sure independence screening
## Generate Empirical Data
simuData <- modalityMediationDataGen(n = 50, p = 1000, seed = 20231201)

## Parameter Estimation for ElasticNet penalty
modelElasticNetSIS <- singleModalityAdmm(
  X = simuData$MediData$X, Y = simuData$MediData$Y, M1 = simuData$MediData$M1,
  rho = 1, lambda1a = 1, lambda1b = 0.1, lambda1g = 2, lambda2a = 1, lambda2b = 1,
  penalty = "ElasticNet", SIS = TRUE
)
fitted(modelElasticNetSIS)
predict(modelElasticNetSIS, matrix(c(0, 1), ncol=1))
```

---

weightToLaplacian	*Helper function to convert Weight Matrix to Laplacian Matrix*

Description

Helper function to convert Weight Matrix to Laplacian Matrix

Usage

```
weightToLaplacian(W)
```

Arguments

W   The weight matrix for n nodes which should be nxn matrix.

Value

L nxn Laplacian matrix.

Examples

```
set.seed(20231201)
p <- 5
W <- matrix(0, nrow = p, ncol = p)
W[lower.tri(W)] <- runif(p*(p-1)/2, 0, 1)
W[upper.tri(W)] <- t(W)[upper.tri(W)]
diag(W) <- 1
(L <- weightToLaplacian(W))
```

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