Package 'rcDEA'

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Title Robust and Conditional Data Envelopment Analysis (DEA)
Version 1.0
Maintainer Anna Mergoni <anna.mergoni@kuleuven.be></anna.mergoni@kuleuven.be>
Description With this package we provide an easy method to compute robust and conditional Data Envelopment Analysis (DEA), Free Disposal Hull (FDH) and Benefit of the Doubt (BOD) scores. The robust approach is based on the work of Cazals, Florens and Simar (2002) <doi:10.1016 s0304-4076(01)00080-x="">. The conditional approach is based on Daraio and Simar (2007) <doi:10.1007 s11123-007-0049-3="">. Besides we provide graphs to help with the choice of m. We relay on the 'Benchmarking' package to compute the efficiency scores and on the 'np' package to compute non parametric estimation of similarity among units.</doi:10.1007></doi:10.1016>
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Author Anna Mergoni [aut, cre] (ORCID: https://orcid.org/0000-0002-9128-5341)
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conditional_BOD

Conditional BOD function

Description

This function allows to compute Robust and Conditional BOD scores.

Usage

```
conditional_BOD(
  output,
  exogenous = FALSE,
  m,
  B,
  alpha = FALSE,
  RTS = "CRS",
  ORIENTATION = "in",
  similarity = FALSE,
  inclusion = FALSE,
  print = FALSE
)
```

Arguments

output

matrix (or vector) of indicators along which the units are evaluated.

exogenous

matrix (or vector) of exogenous variables involved in the conditional analysis. The similarity among the units is determined according to the exogeneous variable(s) using the function npudensbw and npudens (from the package np) with

epanechnikov kernel.

m

number of unit to be included in the reference set

В

number of bootstrap replicates

alpha

This allow to choose the size of the Confidence Intervals computed. By defaulta

alpha = FALSE. In this case no confidence interval are computed

RTS

Default = "CRS". For more details see the dea function in the package Benchmarking. Text string or a number defining the underlying DEA technology / returns to scale assumption. 0 fdh Free disposability hull, no convexity assumption 1 vrs Variable returns to scale, convexity and free disposability 2 drs Decreasing returns to scale, convexity, down-scaling and free disposability 3 crs Constant returns to scale, convexity and free disposability 4 irs Increasing returns to scale, (up-scaling, but not down-scaling), convexity and free disposability 5 irs2 Increasing returns to scale (up-scaling, but not down-scaling), additivity, and free disposability 6 add Additivity (scaling up and down, but only with integers), and free disposability; also known af replicability and free disposability, the free disposability and replicability hull (frh) – no convexity assumption 7 fdh+ A combination of free disposability and restricted or local constant return to scale 10 vrs+ As vrs, but with restrictions on the individual lambdas via param

conditional BOD 3

ORIENTATION Default = "in". For more details see the dea function in the package Benchmarking. Input efficiency "in" (1), output efficiency "out" (2), and graph efficiency "graph" (3). For use with DIRECT, an additional option is "in-out" (0). matrix of similarities. In alternative to provide the exogenous variables, the similarity matrix of similarities can be directly provided. This allow to customize the estimation of the similarities. If inclusion = TRUE the unit under analysis is included in the reference set. So, inclusion no super efficient scores are allowed. By default inclusion = FALSE. print If print = TRUE the number of the unit under evaluation is printed. In case of large sample the function could require some time, so it could be useful to control how many units have already been evaluated and which one still have to be evaluated. By default print = FALSE.

Value

If the parameter alpha is specified, the function returns a data frame with three numeric columns. The first column is the vector representing the conditional BOD scores (eff); the second column is the vector representing the lower bound of the condifence interval (ci_low); the third column is the vector representing the upper bound of the confidence interval (Ci_up). If alpha is not specified, the functions returns only the first column of the data frame (eff).

```
#Example with a very small sample to decrease computational time
          y1 <-runif(50, 50, 75)
          y2 <-runif(50, 30, 75)
          y \leftarrow cbind(y1, y2)
          z \leftarrow ifelse(rnorm(50, 0, 1)>0, 1, 0)
          #Conditional BOD
          c_BOD <- conditional_BOD(output = y, exogenous = z,</pre>
                                     m = 30, B = 50)
          summary(c_BOD$eff)
#Example with bigger sample
          y1 <-runif(100, 50, 75)
          y2 <-runif(100, 30, 75)
          y <- cbind(y1, y2)
          z <- ifelse(rnorm(100, 0, 1)>0, 1, 0)
          #Conditional BOD
          c_BOD <- conditional_BOD(output = y, exogenous = z,</pre>
                                     similarity = FALSE,
                                     m = 30, B = 50
          summary(c_BOD$eff)
```

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conditional_DEA

Conditional DEA function

Description

This function allows to compute Robust and Conditional DEA scores.

Usage

```
conditional_DEA(
  input,
  output,
  exogenous = FALSE,
  alpha = FALSE,
  m,
  B,
  RTS = "crs",
  ORIENTATION = "in",
  similarity = FALSE,
  inclusion = FALSE,
  print = FALSE
)
```

Arguments

input matrix (or vector) of inputs along which the units are evaluated.

output matrix (or vector) of outputs along which the units are evaluated.

exogenous matrix (or vector) of exogenous variables involved in the conditional analysis.

The similarity among the units is determined according to the exogeneous variable(s) using the function npudensbw and npudens (from the package np) with

epanechnikov kernel.

alpha This allow to choose the size of the Confidence Intervals computed. By defaulta

alpha = FALSE. In this case no confidence interval are computed

m number of unit to be included in the reference set

B number of bootstrap replicates

For more details see the dea function in the package Benchmarking. Text string

or a number defining the underlying DEA technology / returns to scale assumption. 0 fdh Free disposability hull, no convexity assumption 1 vrs Variable returns to scale, convexity and free disposability 2 drs Decreasing returns to scale, convexity, down-scaling and free disposability 3 crs Constant returns to scale, convexity and free disposability 4 irs Increasing returns to scale, (up-scaling, but not down-scaling), convexity and free disposability 5 irs2 Increasing returns to scale (up-scaling, but not down-scaling), additivity, and free disposability 6 add Additivity (scaling up and down, but only with integers), and free disposability; also known af replicability and free disposability, the free disposability and

conditional DEA 5

replicability hull (frh) – no convexity assumption 7 fdh+ A combination of free disposability and restricted or local constant return to scale 10 vrs+ As vrs, but with restrictions on the individual lambdas via param

ORIENTATION For more details see the dea function in the package Benchmarking. Input ef-

ficiency "in" (1), output efficiency "out" (2), and graph efficiency "graph" (3).

For use with DIRECT, an additional option is "in-out" (0).

similarity matrix of similarities. In alternative to provide the exogenous variables, the

matrix of similarities can be directly provided. This allow to customize the

estimation of the similarities.

inclusion If inclusion = TRUE the unit under analysis is included in the reference set. So,

no super efficient scores are allowed. By default inclusion = FALSE.

print If print = TRUE the number of the unit under evaluation is printed. In case

of large sample the function could require some time, so it could be useful to control how many units have already been evaluated and which one still have to

be evaluated. By default print = FALSE.

Value

If the parameter alpha is specified, the function returns a data frame with three numeric columns. The first column is the vector representing the conditional DEA scores (eff); the second column is the vector representing the lower bound of the condifence interval (ci_low); the third column is the vector representing the upper bound of the confidence interval (Ci_up). If alpha is not specified, the functions returns only the first column of the data frame (eff).

```
#Example with a very small sample to decrease computational time.
          x1 < -runif(50, 50, 75)
          x2 <-runif(50, 30, 75)
          x \leftarrow cbind(x1, x2)
          e < - rnorm(50, 0, 36)
          a1 <- 0.4
          a2 <- 0.6
          y < -a1*x1 + a2*x2 + e
          z <- ifelse(rnorm(50, 0, 1)>0, 1, 0)
          #Conditional DEA
          c_DEA <- conditional_DEA(input = x, output = y, exogenous = z,</pre>
                                     m = 30, B = 50,
                                     RTS = "crs", ORIENTATION = "in")
          summary(c_DEA$eff)
          #Example with bigger sample
          x1 <-runif(100, 50, 75)
          x2 <-runif(100, 30, 75)
          x \leftarrow cbind(x1, x2)
          a1 <- 0.4
          a2 <- 0.6
          y <- a1*x1 + a2*x2
          z <- ifelse(rnorm(100, 0, 1)>0, 1, 0)
```

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graph1_m_BOD

Graph to select m

Description

This function allows to draw a graph that relates the number of super efficient units and the choice of m

Usage

```
graph1_m_BOD(
  output,
  mseries,
  B,
  RTS = "crs",
  ORIENTATION = "in",
  check = c(1),
  col = c("black"),
  print = TRUE
)
```

Arguments

output

matrix (or vector) of indicators along which the units are evaluated.

mseries

vector containing the different values of f that needed to be tested.

В

number of bootstrap replicates

RTS

For more details see the dea function in the package Benchmarking. Text string or a number defining the underlying DEA technology / returns to scale assumption. 0 fdh Free disposability hull, no convexity assumption 1 vrs Variable returns to scale, convexity and free disposability 2 drs Decreasing returns to scale, convexity, down-scaling and free disposability 3 crs Constant returns to scale, convexity and free disposability 4 irs Increasing returns to scale, (up-scaling, but not down-scaling), convexity and free disposability 5 irs2 Increasing returns to scale (up-scaling, but not down-scaling), additivity, and free disposability 6 add Additivity (scaling up and down, but only with integers), and free disposability; also known af replicability and free disposability, the free disposability and replicability hull (frh) – no convexity assumption 7 fdh+ A combination of free disposability and restricted or local constant return to scale 10 vrs+ As vrs, but with restrictions on the individual lambdas via param

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ORIENTATION	For more details see the dea function in the package Benchmarking. Input efficiency "in" (1), output efficiency "out" (2), and graph efficiency "graph" (3). For use with DIRECT, an additional option is "in-out" (0).
check	vector containing the values of the thresholds to be considered to define the superefficient units
col	vector containing the colors. the vector col must contain the same number of element of the vector check.
print	If print = TRUE the number of the unit under evaluation is printed. In case of large sample the function could require some time, so it could be useful to control how many units have already been evaluated and which one still have to be evaluated. By default print = FALSE.

Value

This function return a plot, representing the percentage of super-efficient units for the different values of m. A unit is defined as super-efficient if it gets a value higher than a certain treshold (normally 1) in the robust analysis. Each line of the plot represent different values of the tresholds.

```
#Example with a very small sample to decrease computational time.
y1 <-runif(20, 50, 75)
y2 <-runif(20, 30, 75)
y <- cbind(y1, y2)
check <- c(1, 1.05, 1.5)
colors <- c("black", "red", "blue")</pre>
graph1_m_BOD(output = y, mseries = c(5, 10, 15),
             B = 50, RTS = "crs", ORIENTATION = "in",
             check = check, col = colors)
 #An example with a larger sample size.
 x1 <-runif(100, 50, 75)
 x2 <-runif(100, 30, 75)
 x \leftarrow cbind(x1, x2)
 y \leftarrow cbind(x+runif(100, -10, 0), rnorm(100, 15, 4))
graph1_m_BOD(output = y,
       mseries = c(20, 30, 40, 50, 60, 70, 80),
       B = 50,
       RTS = "crs", ORIENTATION = "in",
       check = c(1, 1.05, 1.2, 1.5),
       col = c("black", "red", "blue", "green"))
```

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graph1_m_DEA

Graph to select m

Description

This function allows to draw a graph that relates the number of super efficient units and the choice of m

Usage

```
graph1_m_DEA(
   input,
   output,
   mseries,
   B,
   RTS = "crs",
   ORIENTATION = "in",
   check = c(1),
   col = c("black"),
   print = TRUE
)
```

Arguments

input matrix (or vector) of inputs along which the units are evaluated.

output matrix (or vector) of outputs along which the units are evaluated.

mseries vector containing the different values of f that needed to be tested.

B number of bootstrap replicates

RTS For more details see the dea function in the package Benchmarking. Text string

or a number defining the underlying DEA technology / returns to scale assumption. 0 fdh Free disposability hull, no convexity assumption 1 vrs Variable returns to scale, convexity and free disposability 2 drs Decreasing returns to scale, convexity, down-scaling and free disposability 3 crs Constant returns to scale, convexity and free disposability 4 irs Increasing returns to scale, (up-scaling, but not down-scaling), convexity and free disposability 5 irs2 Increasing returns to scale (up-scaling, but not down-scaling), additivity, and free disposability 6 add Additivity (scaling up and down, but only with integers), and free disposability; also known af replicability and free disposability, the free disposability and replicability hull (frh) – no convexity assumption 7 fdh+ A combination of free disposability and restricted or local constant return to scale 10 vrs+ As vrs, but

with restrictions on the individual lambdas via param

ORIENTATION For more details see the dea function in the package Benchmarking. Input ef-

ficiency "in" (1), output efficiency "out" (2), and graph efficiency "graph" (3).

For use with DIRECT, an additional option is "in-out" (0).

check vector containing the values of the thresholds to be considered to define the

superefficient units

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vector containing the colors, the vector col must contain the same number of element of the vector check.

print If print = TRUE the number of the unit under evaluation is printed. In case of large sample the function could require some time, so it could be useful to control how many units have already been evaluated and which one still have to

be evaluated. By default print = FALSE.

Value

This function return a plot, representing the percentage of super-efficient units for the different values of m. A unit is defined as super-efficient if it gets a value higher than a certain treshold (normally 1) in the robust analysis. Each line of the plot represent different values of the tresholds.

```
#Example with a very small sample to decrease computational time.
x1 <-runif(20, 50, 75)
x2 <-runif(20, 30, 75)
x \leftarrow cbind(x1, x2)
e < - rnorm(20, 0, 36)
a1 <- 0.4
a2 <- 0.6
y < -a1*x1 + a2*x2 + e
check <- c(1, 1.05, 1.5)
colors <- c("black", "red", "blue")</pre>
graph1_m_DEA(input = x, output = y, mseries = c(5, 10, 15, 20),
             B = 50, RTS = "crs", ORIENTATION = "in",
             check = check, col = colors)
#An example with a larger sample size.
x1 <-runif(100, 50, 75)
x2 <-runif(100, 30, 75)
x \leftarrow cbind(x1, x2)
y \leftarrow cbind(x+runif(100, -10, 0), rnorm(100, 15, 4))
check <- c(1, 1.05, 1.2, 1.5)
colors <- c("black", "red", "blue", "green")</pre>
graph1_m_DEA(input = x, output = y, mseries = c(20, 30, 40, 50, 60, 70, 80),
             B = 50, RTS = "crs", ORIENTATION = "in",
             check = check,
             col = colors)
```

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graph2_m_BOD	Graph to select m
--------------	-------------------

Description

This function allows to draw a graph that relates the average efficiency score and the choice of m

Usage

```
graph2_m_BOD(output, mseries, B, RTS = "crs", ORIENTATION = "in", print = TRUE)
```

Arguments

output matrix (or vector) of indicators along which the units are evaluated.

mseries vector containing the different values of m that needed to be tested.

B number of bootstrap replicates

RTS For more details see the dea function in the package Benchmarking. Text string

or a number defining the underlying DEA technology / returns to scale assumption. 0 fdh Free disposability hull, no convexity assumption 1 vrs Variable returns to scale, convexity and free disposability 2 drs Decreasing returns to scale, convexity, down-scaling and free disposability 3 crs Constant returns to scale, convexity and free disposability 4 irs Increasing returns to scale, (up-scaling, but not down-scaling), convexity and free disposability 5 irs2 Increasing returns to scale (up-scaling, but not down-scaling), additivity, and free disposability 6 add Additivity (scaling up and down, but only with integers), and free disposability; also known af replicability and free disposability, the free disposability and replicability hull (frh) – no convexity assumption 7 fdh+ A combination of free disposability and restricted or local constant return to scale 10 vrs+ As vrs, but

with restrictions on the individual lambdas via param

ORIENTATION For more details see the dea function in the package Benchmarking. Input ef-

ficiency "in" (1), output efficiency "out" (2), and graph efficiency "graph" (3).

For use with DIRECT, an additional option is "in-out" (0).

print If print = TRUE the number of the unit under evaluation is printed. In case

of large sample the function could require some time, so it could be useful to control how many units have already been evaluated and which one still have to

be evaluated. By default print = FALSE.

Value

This function return a plot representing the average score from the robust analysis for the different values of m chosen.

graph2_m_DEA

Examples

graph2_m_DEA

Graph to select m

Description

This function allows to draw a graph that relates the average efficiency score and the choice of m

Usage

```
graph2_m_DEA(
   input,
   output,
   mseries,
   B,
   RTS = "crs",
   ORIENTATION = "in",
   print = TRUE
)
```

Arguments

input matrix (or vector) of inputs along which the units are evaluated.

output matrix (or vector) of outputs along which the units are evaluated.

mseries vector containing the different values of m that needed to be tested.

B number of bootstrap replicates

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RTS

For more details see the dea function in the package Benchmarking. Text string or a number defining the underlying DEA technology / returns to scale assumption. 0 fdh Free disposability hull, no convexity assumption 1 vrs Variable returns to scale, convexity and free disposability 2 drs Decreasing returns to scale, convexity, down-scaling and free disposability 3 crs Constant returns to scale, convexity and free disposability 4 irs Increasing returns to scale, (up-scaling, but not down-scaling), convexity and free disposability 5 irs2 Increasing returns to scale (up-scaling, but not down-scaling), additivity, and free disposability 6 add Additivity (scaling up and down, but only with integers), and free disposability; also known af replicability and free disposability, the free disposability and replicability hull (frh) – no convexity assumption 7 fdh+ A combination of free disposability and restricted or local constant return to scale 10 vrs+ As vrs, but with restrictions on the individual lambdas via param

ORIENTATION

For more details see the dea function in the package Benchmarking. Input efficiency "in" (1), output efficiency "out" (2), and graph efficiency "graph" (3). For use with DIRECT, an additional option is "in-out" (0).

print

If print = TRUE, the number of the unit under evaluation is printed. In case of large sample the function could require some time, so it could be useful to control how many units have already been evaluated and which one still have to be evaluated. By default print = FALSE.

Value

This function return a plot representing the average score from the robust analysis for the different values of m chosen.

```
#Example with a very small sample to decrease computational time.
x1 <-runif(20, 50, 75)
x2 <-runif(20, 30, 75)
x \leftarrow cbind(x1, x2)
e < -rnorm(20, 0, 36)
a1 <- 0.4
a2 <- 0.6
y <- a1*x1 + a2*x2 + e
graph2_m_DEA(input = x, output = y, mseries = c(5, 10, 15, 20),
             B = 50, RTS = "crs", ORIENTATION = "in")
#An example with a larger sample size.
x1 <-runif(100, 50, 75)
x2 <-runif(100, 30, 75)
x \leftarrow cbind(x1, x2)
y \leftarrow cbind(x+runif(100, -10, 0), rnorm(100, 15, 4))
graph2_m_DEA(input = x, output = y,
             mseries = c(20, 30, 40, 50, 60, 70, 80), B = 50,
             RTS = "crs", ORIENTATION = "in")
```

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robust_BOD

Robust BOD function

Description

This function allows to compute Robust BOD scores.

Usage

```
robust_BOD(
  output,
  m,
  B,
  alpha = FALSE,
  RTS = "CRS",
  ORIENTATION = "in",
  inclusion = FALSE,
  print = FALSE
)
```

Arguments

output matrix (or vector) of indicators along which the units are evaluated.

m number of unit to be included in the reference set

B number of bootstrap replicates

alpha This allow to choose the size of the Confidence Intervals computed. By defaulta

alpha = FALSE. In this case no confidence interval are computed

RTS Default = "CRS". For more details see the dea function in the package Bench-

marking. Text string or a number defining the underlying DEA technology / returns to scale assumption. 0 fdh Free disposability hull, no convexity assumption 1 vrs Variable returns to scale, convexity and free disposability 2 drs Decreasing returns to scale, convexity, down-scaling and free disposability 3 crs Constant returns to scale, convexity and free disposability 4 irs Increasing returns to scale, (up-scaling, but not down-scaling), convexity and free disposability 5 irs2 Increasing returns to scale (up-scaling, but not down-scaling), additivity, and free disposability 6 add Additivity (scaling up and down, but only with integers), and free disposability; also known af replicability and free disposability, the free disposability and replicability hull (frh) – no convexity assumption 7 fdh+ A combination of free disposability and restricted or local constant return to scale 10 vrs+ As vrs, but with restrictions on the individual lambdas via param

ORIENTATION

Default = "in". For more details see the dea function in the package Benchmarking. Input efficiency "in" (1), output efficiency "out" (2), and graph efficiency "graph" (3). For use with DIRECT, an additional option is "in-out" (0).

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inclusion If inclusion = TRUE the unit under analysis is included in the reference set. So,

no super efficient scores are allowed. By default inclusion = FALSE.

print If print = TRUE the number of the unit under evaluation is printed. In case of large sample the function could require some time, so it could be useful to

control how many units have already been evaluated and which one still have to be evaluated. By default print = FALSE.

Value

If the parameter alpha is specified, the function returns a data frame with three numeric columns. The first column is the vector representing the robust BOD scores (eff); the second column is the vector representing the lower bound of the condifence interval (ci_low); the third column is the vector representing the upper bound of the confidence interval (Ci_up). If alpha is not specified, the functions returns only the first column of the data frame (eff).

Examples

```
#Example with a very small sample to decrease computational time.
          y1 <-runif(50, 50, 75)
          y2 <-runif(50, 30, 75)
          y \leftarrow cbind(y1, y2)
          #Robust BOD
          r_BOD \leftarrow robust_BOD(output = y, m = 30, B = 50,
                                RTS = "crs", ORIENTATION = "in", print = TRUE)
          summary(r_BOD$eff)
          ## Not run: #Example with random data x and y
          y1 <-runif(100, 50, 75)
          y2 <-runif(100, 30, 75)
          y \leftarrow cbind(y1, y2)
          #Robust BOD
          r_BOD \leftarrow robust_BOD(output = y, m = 30, B = 50,
                                RTS = "crs", ORIENTATION = "in", print = TRUE)
          summary(r_BOD$eff)
## End(Not run)
```

robust_DEA

Robust Data Envelopment Analysis (DEA)

Description

This function allows to compute Robust DEA scores.

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Usage

```
robust_DEA(
  input,
  output,
  m,
  B,
  RTS = "crs",
  ORIENTATION = "in",
  alpha = FALSE,
  inclusion = FALSE,
  print = FALSE
)
```

Arguments

input matrix (or vector) of inputs along which the units are evaluated.

output matrix (or vector) of outputs along which the units are evaluated.

m number of unit to be included in the reference set

B number of bootstrap replicates

For more details see the dea function in the package Benchmarking. Text string

or a number defining the underlying DEA technology / returns to scale assumption. 0 fdh Free disposability hull, no convexity assumption 1 vrs Variable returns to scale, convexity and free disposability 2 drs Decreasing returns to scale, convexity, down-scaling and free disposability 3 crs Constant returns to scale, convexity and free disposability 4 irs Increasing returns to scale, (up-scaling, but not down-scaling), convexity and free disposability 5 irs2 Increasing returns to scale (up-scaling, but not down-scaling), additivity, and free disposability 6 add Additivity (scaling up and down, but only with integers), and free disposability; also known af replicability and free disposability, the free disposability and replicability hull (frh) – no convexity assumption 7 fdh+ A combination of free disposability and restricted or local constant return to scale 10 vrs+ As vrs, but

with restrictions on the individual lambdas via param

ORIENTATION For more details see the dea function in the package Benchmarking. Input ef-

ficiency "in" (1), output efficiency "out" (2), and graph efficiency "graph" (3).

For use with DIRECT, an additional option is "in-out" (0).

alpha This allow to choose the size of the Confidence Intervals computed. By defaulta

alpha = FALSE. In this case no confidence interval are computed

inclusion If inclusion = TRUE the unit under analysis is included in the reference set. So,

no super efficient scores are allowed. By default inclusion = FALSE.

print If print = TRUE the number of the unit under evaluation is printed. In case

of large sample the function could require some time, so it could be useful to control how many units have already been evaluated and which one still have to

be evaluated. By default print = FALSE.

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Value

If the parameter alpha is specified, the function returns a data frame with three numeric columns. The first column is the vector representing the robust DEA scores (eff); the second column is the vector representing the lower bound of the condifence interval (ci_low); the third column is the vector representing the upper bound of the confidence interval (Ci_up). If alpha is not specified, the functions returns only the first column of the data frame (eff).

```
#Example with a very small sample to decrease computational time.
          x1 <-runif(50, 50, 75)
          x2 <-runif(50, 30, 75)
          x \leftarrow cbind(x1, x2)
          e <- rnorm(50, 0, 36)
          a1 <- 0.4
          a2 <- 0.6
          y <- a1*x1 + a2*x2 + e
          #Robust DEA
          r_DEA <- robust_DEA(input = x, output = y, m = 20, B = 50,
          RTS = "crs", ORIENTATION = "in", print = TRUE)
          summary(r_DEA$eff)
 #Example with random data x and y
          x1 <-runif(100, 50, 75)
          x2 <-runif(100, 30, 75)
          x \leftarrow cbind(x1, x2)
          y \leftarrow cbind(x+runif(100, -10, 0), rnorm(100, 15, 4))
          r_DEA <- robust_DEA(input = x, output = y, m = 30, B = 40,
          RTS = "crs", ORIENTATION = "in", print = TRUE)
          summary(r_DEA$eff)
```

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