

# Package ‘Pade’

July 21, 2025

**Type** Package

**Title** Padé Approximant Coefficients

**Version** 1.0.8

**Date** 2025-07-10

**Description** Given a vector of Taylor series coefficients of sufficient length as input, the function returns the numerator and denominator coefficients for the Padé approximant of appropriate order (Baker, 1975)  
<ISBN:9780120748556>.

**License** GPL (>= 2) | BSD\_2\_clause + file LICENSE

**Imports** utils

**Suggests** covr, tinytest

**URL** <https://github.com/aadler/Pade>

**BugReports** <https://github.com/aadler/Pade/issues>

**Encoding** UTF-8

**NeedsCompilation** no

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**Repository** CRAN

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## Contents

Padé-package . . . . .	2
Padé . . . . .	3

<b>Index</b>	<b>5</b>
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Pade-package

*Padé Approximant Coefficients*


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## Description

Given a vector of Taylor series coefficients of sufficient length as input, the function returns the numerator and denominator coefficients for the Padé approximant of appropriate order (Baker, 1975) <ISBN:9780120748556>.

## Details

The DESCRIPTION file:

```
Package:      Pade
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Title:        Padé Approximant Coefficients
Version:      1.0.8
Date:         2025-07-10
Authors@R:    c(person(given="Avraham", family="Adler", role=c("aut", "cph", "cre"), email="Avraham.Adler@gmail.com"))
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```

Index of help topics:

Pade	Padé Approximant Coefficients
Pade-package	Padé Approximant Coefficients

## Author(s)

Avraham Adler [aut, cph, cre] (ORCID: <https://orcid.org/0000-0002-3039-0703>)

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## Description

Given Taylor series coefficients  $a_n$  from  $n = 0$  up to  $n = T$ , the function will calculate the Padé  $[L/M]$  approximant coefficients so long as  $L + M \leq T$ .

## Usage

Pade(L, M, A)

## Arguments

L	Order of Padé numerator
M	Order of Padé denominator
A	vector of Taylor series coefficients, starting at $x^0$

## Details

As the Taylor series expansion is the “best” polynomial approximation to a function, the Padé approximants are the “best” rational function approximations to the original function. The Padé approximant often has a wider radius of convergence than the corresponding Taylor series, and can even converge where the Taylor series does not. This makes it very suitable for computer-based numerical analysis.

The  $[L/M]$  Padé approximant to a Taylor series  $A(x)$  is the quotient

$$\frac{P_L(x)}{Q_M(x)}$$

where  $P_L(x)$  is of order  $L$  and  $Q_M(x)$  is of order  $M$ . In this case:

$$A(x) - \frac{P_L(x)}{Q_M(x)} = \mathcal{O}(x^{L+M+1})$$

When  $q_0$  is defined to be 1, there is a unique solution to the system of linear equations which can be used to calculate the coefficients.

The function accepts a vector A of length  $T + 1$ , composed of the  $a_n$  of the of truncated Taylor series

$$A(x) = \sum_{j=0}^T a_j x^j$$

and returns a list of two elements, Px and Qx, the Padé numerator and denominator coefficients respectively, as long as  $L + M \leq T$ .

**Value**

Pade returns a list with two entries:

Px	Coefficients of the numerator polynomial starting at $x^0$ .
Qx	Coefficients of the denominator polynomial starting at $x^0$ .

**Author(s)**

Avraham Adler <Avraham.Adler@gmail.com>

**References**

Baker, George Allen (1975) *Essentials of Padé Approximants* Academic Press. ISBN 978-0-120-74855-6

**See Also**

This package provides similar functionality to the pade function in the **pracma** package. However, it does not allow computation of coefficients beyond the supplied Taylor coefficients and it expects its input and provides its output in ascending—instead of descending—order.

See the **minimaxApprox** package for polynomial and rational minimax approximations to functions.

**Examples**

```
A <- 1 / factorial(0:10) ## Taylor sequence for e^x up to x^{10} around x_0 = 0
Z <- Pade(5, 5, A)
print(Z)                    ## Padé approximant of order [5 / 5]
x <- -.01                    ## Test value
Actual <- exp(x)             ## Proper value
print(Actual, digits = 16)
Estimate <- sum(Z[[1L]] * x ^ (seq_along(Z[[1L]]) - 1)) /
  sum(Z[[2L]] * x ^ (seq_along(Z[[2L]]) - 1))
print(Estimate, digits = 16) ## Approximant value
all.equal(Actual, Estimate)
```

# Index

- \* **NumericalMathematics**

- Pade, [3](#)

- Pade-package, [2](#)

- \* **package**

- Pade-package, [2](#)

Pade, [3](#)

Pade-package, [2](#)