

Package ‘smmR’

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Description Performs parametric and non-parametric estimation and simulation for multi-state discrete-time semi-Markov processes. For the parametric estimation, several discrete distributions are considered for the sojourn times: Uniform, Geometric, Poisson, Discrete Weibull and Negative Binomial. The non-parametric estimation concerns the sojourn time distributions, where no assumptions are done on the shape of distributions. Moreover, the estimation can be done on the basis of one or several sample paths, with or without censoring at the beginning or/and at the end of the sample paths. Reliability indicators such as reliability, maintainability, availability, BMP-failure rate, RG-failure rate, mean time to failure and mean time to repair are available as well. The implemented methods are described in Barbu, V.S., Limnios, N. (2008) <[doi:10.1007/978-0-387-73173-5](https://doi.org/10.1007/978-0-387-73173-5)>, Barbu, V.S., Limnios, N. (2008) <[doi:10.1080/10485250701261913](https://doi.org/10.1080/10485250701261913)> and Trevezas, S., Limnios, N. (2011) <[doi:10.1080/10485252.2011.555543](https://doi.org/10.1080/10485252.2011.555543)>. Estimation and simulation of discrete-time k-th order Markov chains are also considered.

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Description

This package performs parametric and non-parametric estimation and simulation for multi-state discrete-time semi-Markov processes. For the parametric estimation, several discrete distributions are considered for the sojourn times: Uniform, Geometric, Poisson, Discrete Weibull and Negative Binomial. The non-parametric estimation concerns the sojourn time distributions, where no assumptions are done on the shape of distributions. Moreover, the estimation can be done on the basis of one or several sample paths, with or without censoring at the beginning or/and at the end of the sample paths. Estimation and simulation of discrete-time k-th order Markov chains are also considered.

Semi-Markov models are specified by using the functions `smmparametric()` and `smmnonparametric()` for parametric and non-parametric specifications respectively. These functions return objects of S3 class (`smm`, `smmparametric`) and (`smm`, `smmnonparametric`) respectively (`smm` class inherits from S3 classes `smmparametric` or `smmnonparametric`). Thus, `smm` is like a wrapper class for semi-Markov model specifications.

Based on a model specification (an object of class `smm`), it is possible to:

- **simulate** one or several sequences with the method `simulate.smm()`;
- **plot** conditional sojourn time distributions (method `plot.smm()`);
- compute **log-likelihood**, **AIC** and **BIC** criteria (methods `loglik()`, `aic()`, `bic()`);
- compute **reliability**, **maintainability**, **availability**, **failure rates** (methods `reliability()`, `maintainability()`, `availability()`, `failureRate()`).

Estimations of parametric and non-parametric semi-Markov models can be done by using the function `fitsmm()`. This function returns an object of S3 class `smmfit`. The class `smmfit` inherits from classes (`smm`, `smmparametric`) or (`smm`, `smmnonparametric`).

Based on a fitted/estimated semi-Markov model (an object of class `smmfit`), it is possible to:

- **simulate** one or several sequences with the method `simulate.smmfit()`;
- **plot** estimated conditional sojourn time distributions (method `plot.smmfit()`);
- compute **log-likelihood**, **AIC** and **BIC** criteria (methods `loglik()`, `aic()`, `bic()`);
- compute estimated **reliability**, **maintainability**, **availability**, **failure rates** and their **confidence intervals** (methods `reliability()`, `maintainability()`, `availability()`, `failureRate()`).

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References

- V. S. Barbu, N. Limnios. (2008). Semi-Markov Chains and Hidden Semi-Markov Models Toward Applications - Their Use in Reliability and DNA Analysis. New York: Lecture Notes in Statistics, vol. 191, Springer.
- R.E. Barlow, A.W. Marshall, and F. Prochan. (1963). Properties of probability distributions with monotone hazard rate. Ann. Math. Statist., 34, 375-389.
- T. Nakagawa and S. Osaki. (1975). The discrete Weibull distribution. IEEE Trans. Reliabil., R-24, 300-301.
- D. Roy and R. Gupta. (1992). Classification of discrete lives. Microelectron. Reliabil., 32 (10), 1459-1473.
- I. Votsi & A. Brouste (2019) Confidence interval for the mean time to failure in semi-Markov models: an application to wind energy production, Journal of Applied Statistics, 46:10, 1756-1773.

aic

Akaike Information Criterion (AIC)

Description

Generic function computing the Akaike Information Criterion of the model `x`, with the list of sequences `sequences`.

Usage

```
aic(x, sequences = NULL)
```

Arguments

- | | |
|------------------------|--|
| <code>x</code> | An object for which there exists a <code>loglik</code> attribute if <code>sequences = NULL</code> or a <code>loglik</code> method otherwise. |
| <code>sequences</code> | Optional. A list of vectors representing the sequences for which the AIC will be computed based on <code>x</code> using the method <code>loglik</code> . |

Value

Value of the AIC.

availability	<i>Availability Function</i>
--------------	------------------------------

Description

The pointwise (or instantaneous) availability of a system S_{system} at time $k \in N$ is the probability that the system is operational at time k (independently of the fact that the system has failed or not in $[0, k)$).

Usage

```
availability(x, k, upstates = x$states, level = 0.95, klim = 10000)
```

Arguments

<code>x</code>	An object of S3 class <code>smmfit</code> or <code>smm</code> .
<code>k</code>	A positive integer giving the time at which the availability should be computed.
<code>upstates</code>	Vector giving the subset of operational states U .
<code>level</code>	Confidence level of the asymptotic confidence interval. Helpful for an object <code>x</code> of class <code>smmfit</code> .
<code>klim</code>	Optional. The time horizon used to approximate the series in the computation of the mean sojourn times vector m (cf. meanSojournTimes function) for the asymptotic variance.

Details

Consider a system (or a component) S_{system} whose possible states during its evolution in time are $E = \{1, \dots, s\}$. Denote by $U = \{1, \dots, s_1\}$ the subset of operational states of the system (the up states) and by $D = \{s_1 + 1, \dots, s\}$ the subset of failure states (the down states), with $0 < s_1 < s$ (obviously, $E = U \cup D$ and $U \cap D = \emptyset$, $U \neq \emptyset$, $D \neq \emptyset$). One can think of the states of U as different operating modes or performance levels of the system, whereas the states of D can be seen as failures of the systems with different modes.

We are interested in investigating the availability of a discrete-time semi-Markov system S_{system} . Consequently, we suppose that the evolution in time of the system is governed by an E -state space semi-Markov chain $(Z_k)_{k \in N}$. The state of the system is given at each instant $k \in N$ by Z_k : the event $\{Z_k = i\}$, for a certain $i \in U$, means that the system S_{system} is in operating mode i at time k , whereas $\{Z_k = j\}$, for a certain $j \in D$, means that the system is not operational at time k due to the mode of failure j or that the system is under the repairing mode j .

The pointwise (or instantaneous) availability of a system S_{system} at time $k \in N$ is the probability that the system is operational at time k (independently of the fact that the system has failed or not in $[0, k)$).

Thus, the pointwise availability of a semi-Markov system at time $k \in N$ is

$$A(k) = P(Z_k \in U) = \sum_{i \in E} \alpha_i A_i(k),$$

where we have denoted by $A_i(k)$ the conditional availability of the system at time $k \in N$, given that it starts in state $i \in E$,

$$A_i(k) = P(Z_k \in U | Z_0 = i).$$

Value

A matrix with $k + 1$ rows, and with columns giving values of the availability, variances, lower and upper asymptotic confidence limits (if x is an object of class `smmfit`).

References

V. S. Barbu, N. Limnios. (2008). Semi-Markov Chains and Hidden Semi-Markov Models Toward Applications - Their Use in Reliability and DNA Analysis. New York: Lecture Notes in Statistics, vol. 191, Springer.

bic

Bayesian Information Criterion (BIC)

Description

Generic function computing the Bayesian Information Criterion of the model x , with the list of sequences `sequences`.

Usage

```
bic(x, sequences = NULL)
```

Arguments

<code>x</code>	An object for which there exists a <code>loglik</code> attribute if <code>sequences = NULL</code> or a <code>loglik</code> method otherwise.
<code>sequences</code>	Optional. A list of vectors representing the sequences for which the AIC will be computed based on x using the method <code>loglik</code> .

Value

Value of the BIC.

failureRate

*Failure Rate Function***Description**

Function to compute the BMP-failure rate or the RG-failure rate.

Consider a system S_{system} starting to work at time $k = 0$. The BMP-failure rate at time $k \in N$ is the conditional probability that the failure of the system occurs at time k , given that the system has worked until time $k - 1$.

The RG-failure rate is a discrete-time adapted failure rate, proposed by D. Roy and R. Gupta. Classification of discrete lives. *Microelectronics Reliability*, 32(10):1459–1473, 1992. We call it the RG-failure rate and denote it by $r(k)$, $k \in N$.

Usage

```
failureRate(
  x,
  k,
  upstates = x$states,
  failure.rate = c("BMP", "RG"),
  level = 0.95,
  epsilon = 0.001,
  klim = 10000
)
```

Arguments

x	An object of S3 class <code>smmfit</code> or <code>smm</code> .
k	A positive integer giving the period $[0, k]$ on which the BMP-failure rate should be computed.
upstates	Vector giving the subset of operational states U .
failure.rate	Type of failure rate to compute. If <code>failure.rate = "BMP"</code> (default value), then BMP-failure-rate is computed. If <code>failure.rate = "RG"</code> , the RG-failure rate is computed.
level	Confidence level of the asymptotic confidence interval. Helpful for an object <code>x</code> of class <code>smmfit</code> .
epsilon	Value of the reliability above which the latter is supposed to be 0 because of computation errors (see Details).
klim	Optional. The time horizon used to approximate the series in the computation of the mean sojourn times vector m (cf. meanSojournTimes function) for the asymptotic variance.

Details

Consider a system (or a component) S_{system} whose possible states during its evolution in time are $E = \{1, \dots, s\}$. Denote by $U = \{1, \dots, s_1\}$ the subset of operational states of the system (the up states) and by $D = \{s_1 + 1, \dots, s\}$ the subset of failure states (the down states), with $0 < s_1 < s$ (obviously, $E = U \cup D$ and $U \cap D = \emptyset$, $U \neq \emptyset$, $D \neq \emptyset$). One can think of the states of U as different operating modes or performance levels of the system, whereas the states of D can be seen as failures of the systems with different modes.

We are interested in investigating the failure rate of a discrete-time semi-Markov system S_{system} . Consequently, we suppose that the evolution in time of the system is governed by an E-state space semi-Markov chain $(Z_k)_{k \in N}$. The system starts to work at instant 0 and the state of the system is given at each instant $k \in N$ by Z_k : the event $\{Z_k = i\}$, for a certain $i \in U$, means that the system S_{system} is in operating mode i at time k , whereas $\{Z_k = j\}$, for a certain $j \in D$, means that the system is not operational at time k due to the mode of failure j or that the system is under the repairing mode j .

The BMP-failure rate at time $k \in N$ is the conditional probability that the failure of the system occurs at time k , given that the system has worked until time $k - 1$.

Let T_D denote the first passage time in subset D , called the lifetime of the system, i.e.,

$$T_D := \inf\{n \in N; Z_n \in D\} \text{ and } \inf \emptyset := \infty.$$

For a discrete-time semi-Markov system, the failure rate at time $k \geq 1$ has the expression:

$$\lambda(k) := P(T_D = k | T_D \geq k)$$

We can rewrite it as follows :

$$\lambda(k) = 1 - \frac{R(k)}{R(k-1)}, \text{ if } R(k-1) \neq 0; \lambda(k) = 0, \text{ otherwise}$$

The failure rate at time $k = 0$ is defined by $\lambda(0) := 1 - R(0)$, with R being the reliability function (see [reliability](#) function).

The calculation of the reliability R involves the computation of many convolutions. It implies that the computation error, may be higher (in value) than the "true" reliability itself for reliability close to 0. In order to avoid inconsistent values of the BMP-failure rate, we use the following formula:

$$\lambda(k) = 1 - \frac{R(k)}{R(k-1)}, \text{ if } R(k-1) \geq \epsilon; \lambda(k) = 0, \text{ otherwise}$$

with ϵ , the threshold, the parameter epsilon in the function `failureRate`.

Expressing the RG-failure rate $r(k)$ in terms of the reliability R we obtain that the RG-failure rate function for a discrete-time system is given by:

$$r(k) = -\ln \frac{R(k)}{R(k-1)}, \text{ if } k \geq 1; r(k) = -\ln R(0), \text{ if } k = 0$$

for $R(k) \neq 0$. If $R(k) = 0$, we set $r(k) := 0$.

Note that the RG-failure rate is related to the BMP-failure rate by:

$$r(k) = -\ln(1 - \lambda(k)), k \in N$$

Value

A matrix with $k + 1$ rows, and with columns giving values of the BMP-failure rate or RG-failure rate, variances, lower and upper asymptotic confidence limits (if x is an object of class `smmfit`).

References

- V. S. Barbu, N. Limnios. (2008). *Semi-Markov Chains and Hidden Semi-Markov Models Toward Applications - Their Use in Reliability and DNA Analysis*. New York: Lecture Notes in Statistics, vol. 191, Springer.
- R.E. Barlow, A.W. Marshall, and F. Prochan. (1963). Properties of probability distributions with monotone hazard rate. *Ann. Math. Statist.*, 34, 375-389.
- D. Roy and R. Gupta. (1992). Classification of discrete lives. *Microelectron. Reliabil.*, 32 (10), 1459-1473.

 fitmm

Maximum Likelihood Estimation (MLE) of a k-th order Markov chain

Description

Maximum Likelihood Estimation of the transition matrix and initial distribution of a k-th order Markov chain starting from one or several sequences.

Usage

```
fitmm(sequences, states, k = 1, init.estim = "mle")
```

Arguments

- | | |
|-------------------------|---|
| <code>sequences</code> | A list of vectors representing the sequences. |
| <code>states</code> | Vector of state space (of length s). |
| <code>k</code> | Order of the Markov chain. |
| <code>init.estim</code> | Optional. <code>init.estim</code> gives the method used to estimate the initial distribution. The following methods are proposed: <ul style="list-style-type: none"> • <code>init.estim = "mle"</code>: the classical Maximum Likelihood Estimator is used to estimate the initial distribution <code>init</code>; • <code>init.estim = "stationary"</code>: the initial distribution is replaced by the stationary distribution of the Markov chain (if the order of the Markov chain is more than one, the transition matrix is converted into a square block matrix in order to estimate the stationary distribution); • <code>init.estim = "freq"</code>: the initial distribution is estimated by taking the frequencies of the words of length k for all sequences; • <code>init.estim = "prod"</code>: <code>init</code> is estimated by using the product of the frequencies of each letter (for all the sequences) in the word of length k; • <code>init.estim = "unif"</code>: the initial probability of each state is equal to $1/s$, with s the number of states. |

Details

Let X_1, X_2, \dots, X_n be a trajectory of length n of the Markov chain $X = (X_m)_{m \in N}$ of order $k = 1$ with transition matrix $p_{trans}(i, j) = P(X_{m+1} = j | X_m = i)$. The maximum likelihood estimation of the transition matrix is $\widehat{p_{trans}}(i, j) = \frac{N_{ij}}{N_{i\cdot}}$, where N_{ij} is the number of transitions from state i to state j and $N_{i\cdot}$ is the number of transition from state i to any state. For $k > 1$ we have similar expressions.

The initial distribution of a k -th order Markov chain is defined as $\mu_i = P(X_1 = i)$. Five methods are proposed for the estimation of the latter :

Maximum Likelihood Estimator: The Maximum Likelihood Estimator for the initial distribution. The formula is: $\widehat{\mu}_i = \frac{N_{start_i}}{L}$, where N_{start_i} is the number of occurrences of the word i (of length k) at the beginning of each sequence and L is the number of sequences. This estimator is reliable when the number of sequences L is high.

Stationary distribution: The stationary distribution is used as a surrogate of the initial distribution. If the order of the Markov chain is more than one, the transition matrix is converted into a square block matrix in order to estimate the stationary distribution. This method may take time if the order of the Markov chain is high (more than three (3)).

Frequencies of each word: The initial distribution is estimated by taking the frequencies of the words of length k for all sequences. The formula is $\widehat{\mu}_i = \frac{N_i}{N}$, where N_i is the number of occurrences of the word i (of length k) in the sequences and N is the sum of the lengths of the sequences.

Product of the frequencies of each state: The initial distribution is estimated by using the product of the frequencies of each state (for all the sequences) in the word of length k .

Uniform distribution: The initial probability of each state is equal to $1/s$, with s , the number of states.

Value

An object of class `S3 mmfit` (inheriting from the S3 class `mm`). The S3 class `mmfit` contains:

- All the attributes of the S3 class `mm`;
- An attribute `M` which is an integer giving the total length of the set of sequences sequences (sum of all the lengths of the list sequences);
- An attribute `loglik` which is a numeric value giving the value of the log-likelihood of the specified Markov model based on the sequences;
- An attribute `sequences` which is equal to the parameter sequences of the function `fitmm` (i.e. a list of sequences used to estimate the Markov model).

See Also

[mm](#), [simulate.mm](#)

Examples

```
states <- c("a", "c", "g", "t")
s <- length(states)
k <- 2
```

```

init <- rep.int(1 / s ^ k, s ^ k)
p <- matrix(0.25, nrow = s ^ k, ncol = s)

# Specify a Markov model of order 2
markov <- mm(states = states, init = init, ptrans = p, k = k)

seqs <- simulate(object = markov, nsim = c(1000, 10000, 2000), seed = 150)

est <- fitmm(sequences = seqs, states = states, k = 2)

```

fitsmm

Maximum Likelihood Estimation (MLE) of a semi-Markov chain

Description

Maximum Likelihood Estimation of a semi-Markov chain starting from one or several sequences. This estimation can be parametric or non-parametric, non-censored, censored at the beginning and/or at the end of the sequence, with one or several trajectories. Several parametric distributions are considered (Uniform, Geometric, Poisson, Discrete Weibull and Negative Binomial).

Usage

```

fitsmm(
  sequences,
  states,
  type.sojourn = c("fij", "fi", "fj", "f"),
  distr = "nonparametric",
  init.estim = "mle",
  cens.beg = FALSE,
  cens.end = FALSE
)

```

Arguments

sequences	A list of vectors representing the sequences.
states	Vector of state space (of length s).
type.sojourn	Type of sojourn time (for more explanations, see Details).
distr	By default "nonparametric" for the non-parametric estimation case. If the parametric estimation case is desired, distr should be: <ul style="list-style-type: none"> • A matrix of distributions of dimension (s, s) if type.sojourn = "fij"; • A vector of distributions of length s if type.sojourn = "fi" or "fj"; • A distribution if type.sojourn = "f". The distributions to be used in distr must be one of "unif", "geom", "pois", "dweibull", "nbinom".

<code>init.estim</code>	Optional. <code>init.estim</code> gives the method used to estimate the initial distribution. The following methods are proposed: <ul style="list-style-type: none"> • <code>init.estim = "mle"</code>: the classical Maximum Likelihood Estimator is used to estimate the initial distribution <code>init</code>; • <code>init.estim = "limit"</code>: the initial distribution is replaced by the limit (stationary) distribution of the semi-Markov chain; • <code>init.estim = "freq"</code>: the initial distribution is replaced by the frequencies of each state in the sequences; • <code>init.estim = "unif"</code>: the initial probability of each state is equal to $1/s$, with s the number of states.
<code>cens.beg</code>	Optional. A logical value indicating whether or not sequences are censored at the beginning.
<code>cens.end</code>	Optional. A logical value indicating whether or not sequences are censored at the end.

Details

This function estimates a semi-Markov model in parametric or non-parametric case, taking into account the type of sojourn time and the censoring described in references. The non-parametric estimation concerns sojourn time distributions defined by the user. For the parametric estimation, several discrete distributions are considered (see below).

The difference between the Markov model and the semi-Markov model concerns the modeling of the sojourn time. With a Markov chain, the sojourn time distribution is modeled by a Geometric distribution (in discrete time). With a semi-Markov chain, the sojourn time can be any arbitrary distribution. In this package, the available distribution for a semi-Markov model are :

- Uniform: $f(x) = \frac{1}{n}$ for $1 \leq x \leq n$. n is the parameter;
- Geometric: $f(x) = \theta(1 - \theta)^{x-1}$ for $x = 1, 2, \dots, n$, $0 < \theta < 1$, θ is the probability of success. θ is the parameter;
- Poisson: $f(x) = \frac{\lambda^x \exp(-\lambda)}{x!}$ for $x = 0, 1, 2, \dots, n$, with $\lambda > 0$. λ is the parameter;
- Discrete Weibull of type 1: $f(x) = q^{(x-1)^\beta} - q^{x^\beta}$, $x = 1, 2, \dots, n$, with $0 < q < 1$, the first parameter and $\beta > 0$ the second parameter. (q, β) are the parameters;
- Negative binomial: $f(x) = \frac{\Gamma(x+\alpha)}{\Gamma(\alpha)x!} p^\alpha (1-p)^x$, for $x = 0, 1, 2, \dots, n$, Γ is the Gamma function, α is the parameter of overdispersion and p is the probability of success, $0 < p < 1$. (α, p) are the parameters;
- Non-parametric.

We define :

- the semi-Markov kernel $q_{ij}(k) = P(J_{m+1} = j, T_{m+1} - T_m = k | J_m = i)$;
- the transition matrix $(p_{trans}(i, j))_{i, j} \in \text{states}$ of the embedded Markov chain $J = (J_m)_m$, $p_{trans}(i, j) = P(J_{m+1} = j | J_m = i)$;
- the initial distribution $\mu_i = P(J_1 = i) = P(Z_1 = i)$, $i \in 1, 2, \dots, s$;
- the conditional sojourn time distributions $(f_{ij}(k))_{i, j} \in \text{states}$, $k \in N$, $f_{ij}(k) = P(T_{m+1} - T_m = k | J_m = i, J_{m+1} = j)$, f is specified by the argument `param` in the parametric case and by `distr` in the non-parametric case.

The maximum likelihood estimation of the transition matrix of the embedded Markov chain is $\widehat{p_{trans}}(i, j) = \frac{N_{ij}}{N_{i.}}$.

Five methods are proposed for the estimation of the initial distribution :

Maximum Likelihood Estimator: The Maximum Likelihood Estimator for the initial distribution. The formula is: $\widehat{\mu}_i = \frac{N_{start_i}}{L}$, where N_{start_i} is the number of occurrences of the word i (of length k) at the beginning of each sequence and L is the number of sequences. This estimator is reliable when the number of sequences L is high.

Limit (stationary) distribution: The limit (stationary) distribution of the semi-Markov chain is used as a surrogate of the initial distribution.

Frequencies of each state: The initial distribution is replaced by taking the frequencies of each state in the sequences.

Uniform distribution: The initial probability of each state is equal to $1/s$, with s , the number of states.

Note that $q_{ij}(k) = p_{trans}(i, j) f_{ij}(k)$ in the general case (depending on the present state and on the next state). For particular cases, we replace $f_{ij}(k)$ by $f_{i.}(k)$ (depending on the present state i), $f_{.j}(k)$ (depending on the next state j) and $f_{..}(k)$ (depending neither on the present state nor on the next state).

In this package we can choose different types of sojourn time. Four options are available for the sojourn times:

- depending on the present state and on the next state (fij);
- depending only on the present state (fi);
- depending only on the next state (fj);
- depending neither on the current, nor on the next state (f).

If `type.sojourn = "fij"`, `distr` is a matrix of dimension (s, s) (e.g., if the 1st element of the 2nd column is "pois", that is to say we go from the first state to the second state following a Poisson distribution). If `type.sojourn = "fi"` or `"fj"`, `distr` must be a vector (e.g., if the first element of vector is "geom", that is to say we go from (or to) the first state to (or from) any state according to a Geometric distribution). If `type.sojourn = "f"`, `distr` must be one of "unif", "geom", "pois", "dweibull", "nbinom" (e.g., if `distr` is equal to "nbinom", that is to say that the sojourn time when going from one state to another state follows a Negative Binomial distribution). For the non-parametric case, `distr` is equal to "nonparametric" whatever type of sojourn time given.

If the sequence is censored at the beginning and/or at the end, `cens.beg` must be equal to TRUE and/or `cens.end` must be equal to TRUE. All the sequences must be censored in the same way.

Value

Returns an object of S3 class `smmfit` (inheriting from the S3 class `smm` and `smmnonparametric` class if `distr = "nonparametric"` or `smmparametric` otherwise). The S3 class `smmfit` contains:

- All the attributes of the S3 class `smmnonparametric` or `smmparametric` depending on the type of estimation;
- An attribute `M` which is an integer giving the total length of the set of sequences sequences (sum of all the lengths of the list sequences);

- An attribute `loglik` which is a numeric value giving the value of the log-likelihood of the specified semi-Markov model based on the sequences;
- An attribute `sequences` which is equal to the parameter sequences of the function `fitsmm` (i.e. a list of sequences used to estimate the Markov model).

References

V. S. Barbu, N. Limnios. (2008). Semi-Markov Chains and Hidden Semi-Markov Models Toward Applications - Their Use in Reliability and DNA Analysis. New York: Lecture Notes in Statistics, vol. 191, Springer.

See Also

[smmnonparametric](#), [smmparametric](#), [simulate.smm](#), [simulate.smmfit](#), [plot.smm](#), [plot.smmfit](#)

Examples

```
states <- c("a", "c", "g", "t")
s <- length(states)

# Creation of the initial distribution
vect.init <- c(1 / 4, 1 / 4, 1 / 4, 1 / 4)

# Creation of the transition matrix
pij <- matrix(c(0, 0.2, 0.5, 0.3,
               0.2, 0, 0.3, 0.5,
               0.3, 0.5, 0, 0.2,
               0.4, 0.2, 0.4, 0),
              ncol = s, byrow = TRUE)

# Creation of the distribution matrix
distr.matrix <- matrix(c(NA, "pois", "geom", "nbinom",
                        "geom", NA, "pois", "dweibull",
                        "pois", "pois", NA, "geom",
                        "pois", "geom", "geom", NA),
                      nrow = s, ncol = s, byrow = TRUE)

# Creation of an array containing the parameters
param1.matrix <- matrix(c(NA, 2, 0.4, 4,
                        0.7, NA, 5, 0.6,
                        2, 3, NA, 0.6,
                        4, 0.3, 0.4, NA),
                      nrow = s, ncol = s, byrow = TRUE)

param2.matrix <- matrix(c(NA, NA, NA, 0.6,
                        NA, NA, NA, 0.8,
                        NA, NA, NA, NA,
                        NA, NA, NA, NA),
                      nrow = s, ncol = s, byrow = TRUE)

param.array <- array(c(param1.matrix, param2.matrix), c(s, s, 2))
```

```

# Specify the semi-Markov model
semimarkov <- smmparametric(states = states, init = vect.init, ptrans = pij,
                           type.sojourn = "fij", distr = distr.matrix,
                           param = param.array)

seqs <- simulate(object = semimarkov, nsim = c(1000, 10000, 2000), seed = 100)

# Estimation of simulated sequences
est <- fitsmm(sequences = seqs, states = states, type.sojourn = "fij",
              distr = distr.matrix)

```

getKernel

Method to get the semi-Markov kernel q

Description

Computes the semi-Markov kernel $q_{ij}(k)$.

Usage

```
getKernel(x, k, var = FALSE, klim = 10000)
```

Arguments

x	An object of S3 class <code>smmfit</code> or <code>smm</code> .
k	A positive integer giving the time horizon.
var	Logical. If TRUE the asymptotic variance is computed.
klim	Optional. The time horizon used to approximate the series in the computation of the mean sojourn times vector m (cf. meanSojournTimes function) for the asymptotic variance.

Value

An array giving the value of $q_{ij}(k)$ at each time between 0 and k if `var = FALSE`. If `var = TRUE`, a list containing the following components:

- `x`: an array giving the value of $q_{ij}(k)$ at each time between 0 and k;
- `sigma2`: an array giving the asymptotic variance of the estimator $\sigma_q^2(i, j, k)$.

is.mm	<i>Function to check if an object is of class mm</i>
-------	--

Description

is.mm returns TRUE if x is an object of class mm.

Usage

```
is.mm(x)
```

Arguments

x An arbitrary R object.

Value

is.mm returns TRUE or FALSE depending on whether x is an object of class mm or not.

is.mmfit	<i>Function to check if an object is of class mmfit</i>
----------	---

Description

is.mmfit returns TRUE if x is an object of class mmfit.

Usage

```
is.mmfit(x)
```

Arguments

x An arbitrary R object.

Value

is.mmfit returns TRUE or FALSE depending on whether x is an object of class mmfit or not.

is.smm	<i>Function to check if an object is of class smm</i>
--------	---

Description

is.smm returns TRUE if x is an object of class smm.

Usage

```
is.smm(x)
```

Arguments

x An arbitrary R object.

Value

is.smm returns TRUE or FALSE depending on whether x is an object of class smm or not.

is.smmfit	<i>Function to check if an object is of class smmfit</i>
-----------	--

Description

is.smmfit returns TRUE if x is an object of class smmfit.

Usage

```
is.smmfit(x)
```

Arguments

x An arbitrary R object.

Value

is.smmfit returns TRUE or FALSE depending on whether x is an object of class smmfit or not.

is.smmnonparametric *Function to check if an object is of class smmnonparametric*

Description

is.smmnonparametric returns TRUE if x is an object of class smmnonparametric.

Usage

```
is.smmnonparametric(x)
```

Arguments

x An arbitrary R object.

Value

is.smmnonparametric returns TRUE or FALSE depending on whether x is an object of class smmnonparametric or not.

is.smmparametric *Function to check if an object is of class smmparametric*

Description

is.smmparametric returns TRUE if x is an object of class smmparametric.

Usage

```
is.smmparametric(x)
```

Arguments

x An arbitrary R object.

Value

is.smmparametric returns TRUE or FALSE depending on whether x is an object of class smmparametric or not.

loglik	<i>Log-likelihood Function</i>
--------	--------------------------------

Description

Generic function computing the log-likelihood of the model `x`, with the list of sequences `sequences`.

Usage

```
loglik(x, sequences = NULL)
```

Arguments

<code>x</code>	An object for which there exists a <code>loglik</code> attribute if <code>sequences = NULL</code> . Otherwise, the log-likelihood will be computed using the model <code>x</code> and the sequences <code>sequences</code> .
<code>sequences</code>	Optional. A list of vectors representing the sequences for which the log-likelihood will be computed based on <code>x</code> .

Value

Value of the log-likelihood.

maintainability	<i>Maintainability Function</i>
-----------------	---------------------------------

Description

For a repairable system S_{system} for which the failure occurs at time $k = 0$, its maintainability at time $k \in N$ is the probability that the system is repaired up to time k , given that it has failed at time $k = 0$.

Usage

```
maintainability(x, k, upstates = x$states, level = 0.95, klim = 10000)
```

Arguments

<code>x</code>	An object of S3 class <code>smmfit</code> or <code>smm</code> .
<code>k</code>	A positive integer giving the period $[0, k]$ on which the maintainability should be computed.
<code>upstates</code>	Vector giving the subset of operational states U .
<code>level</code>	Confidence level of the asymptotic confidence interval. Helpful for an object <code>x</code> of class <code>smmfit</code> .
<code>klim</code>	Optional. The time horizon used to approximate the series in the computation of the mean sojourn times vector m (cf. meanSojournTimes function) for the asymptotic variance.

Details

Consider a system (or a component) S_{system} whose possible states during its evolution in time are $E = \{1, \dots, s\}$. Denote by $U = \{1, \dots, s_1\}$ the subset of operational states of the system (the up states) and by $D = \{s_1 + 1, \dots, s\}$ the subset of failure states (the down states), with $0 < s_1 < s$ (obviously, $E = U \cup D$ and $U \cap D = \emptyset$, $U \neq \emptyset$, $D \neq \emptyset$). One can think of the states of U as different operating modes or performance levels of the system, whereas the states of D can be seen as failures of the systems with different modes.

We are interested in investigating the maintainability of a discrete-time semi-Markov system S_{system} . Consequently, we suppose that the evolution in time of the system is governed by an E-state space semi-Markov chain $(Z_k)_{k \in N}$. The system starts to fail at instant 0 and the state of the system is given at each instant $k \in N$ by Z_k : the event $\{Z_k = i\}$, for a certain $i \in U$, means that the system S_{system} is in operating mode i at time k , whereas $\{Z_k = j\}$, for a certain $j \in D$, means that the system is not operational at time k due to the mode of failure j or that the system is under the repairing mode j .

Thus, we take $(\alpha_i := P(Z_0 = i))_{i \in U} = 0$ and we denote by T_U the first hitting time of subset U , called the duration of repair or repair time, that is,

$$T_U := \inf\{n \in N; Z_n \in U\} \text{ and } \inf \emptyset := \infty.$$

The maintainability at time $k \in N$ of a discrete-time semi-Markov system is

$$M(k) = P(T_U \leq k) = 1 - P(T_U > k) = 1 - P(Z_n \in D, n = 0, \dots, k).$$

Value

A matrix with $k + 1$ rows, and with columns giving values of the maintainability, variances, lower and upper asymptotic confidence limits (if x is an object of class `smmfit`).

References

V. S. Barbu, N. Limnios. (2008). Semi-Markov Chains and Hidden Semi-Markov Models Toward Applications - Their Use in Reliability and DNA Analysis. New York: Lecture Notes in Statistics, vol. 191, Springer.

meanRecurrenceTimes *Method to get the mean recurrence times μ*

Description

Method to get the mean recurrence times μ .

Usage

```
meanRecurrenceTimes(x, klim = 10000)
```

Arguments

x	An object of S3 class <code>smmfit</code> or <code>smm</code> .
klim	Optional. The time horizon used to approximate the series in the computation of the mean sojourn times vector m (cf. <code>meanSojournTimes</code> function).

Details

Consider a system (or a component) S_{system} whose possible states during its evolution in time are $E = \{1, \dots, s\}$.

We are interested in investigating the mean recurrence times of a discrete-time semi-Markov system S_{system} . Consequently, we suppose that the evolution in time of the system is governed by an E-state space semi-Markov chain $(Z_k)_{k \in N}$. The state of the system is given at each instant $k \in N$ by Z_k : the event $\{Z_k = i\}$.

Let $T = (T_n)_{n \in N}$ denote the successive time points when state changes in $(Z_n)_{n \in N}$ occur and let also $J = (J_n)_{n \in N}$ denote the successively visited states at these time points.

The mean recurrence of an arbitrary state $j \in E$ is given by:

$$\mu_{jj} = \frac{\sum_{i \in E} \nu(i) m_i}{\nu(j)}$$

where $(\nu(1), \dots, \nu(s))$ is the stationary distribution of the embedded Markov chain $(J_n)_{n \in N}$ and m_i is the mean sojourn time in state $i \in E$ (see `meanSojournTimes` function for the computation).

Value

A vector giving the mean recurrence time $(\mu_i)_{i \in [1, \dots, s]}$.

meanSojournTimes	<i>Mean Sojourn Times Function</i>
------------------	------------------------------------

Description

The mean sojourn time is the mean time spent in each state.

Usage

```
meanSojournTimes(x, states = x$states, klim = 10000)
```

Arguments

x	An object of S3 class <code>smmfit</code> or <code>smm</code> .
states	Vector giving the states for which the mean sojourn time should be computed. <code>states</code> is a subset of E .
klim	Optional. The time horizon used to approximate the series in the computation of the mean sojourn times vector m (cf. <code>meanSojournTimes</code> function).

Details

Consider a system (or a component) S_{system} whose possible states during its evolution in time are $E = \{1, \dots, s\}$.

We are interested in investigating the mean sojourn times of a discrete-time semi-Markov system S_{system} . Consequently, we suppose that the evolution in time of the system is governed by an E-state space semi-Markov chain $(Z_k)_{k \in N}$. The state of the system is given at each instant $k \in N$ by Z_k : the event $\{Z_k = i\}$.

Let $T = (T_n)_{n \in N}$ denote the successive time points when state changes in $(Z_n)_{n \in N}$ occur and let also $J = (J_n)_{n \in N}$ denote the successively visited states at these time points.

The mean sojourn times vector is defined as follows:

$$m_i = E[T_1 | Z_0 = j] = \sum_{k \geq 0} (1 - P(T_{n+1} - T_n \leq k | J_n = j)) = \sum_{k \geq 0} (1 - H_j(k)), \quad i \in E$$

Value

A vector of length $\text{card}(E)$ giving the values of the mean sojourn times for each state $i \in E$.

 mm

 Markov model specification

Description

Creates a model specification of a Markov model.

Usage

```
mm(states, init, ptrans, k = 1)
```

Arguments

states	Vector of state space of length s.
init	Vector of initial distribution of length s ^ k.
ptrans	Matrix of transition probabilities of dimension (s, s).
k	Order of the Markov chain.

Value

An object of class [mm](#).

See Also

[simulate.mm](#), [fitmm](#)

Examples

```

states <- c("a", "c", "g", "t")
s <- length(states)
k <- 1
init <- rep.int(1 / s, s)
p <- matrix(c(0, 0, 0.3, 0.4, 0, 0, 0.5, 0.2, 0.7, 0.5,
             0, 0.4, 0.3, 0.5, 0.2, 0), ncol = s)

# Specify a Markov model of order 1
markov <- mm(states = states, init = init, ptrans = p, k = k)

```

mttf

Mean Time To Failure (MTTF) Function

Description

Consider a system S_{system} starting to work at time $k = 0$. The mean time to failure (MTTF) is defined as the mean lifetime.

Usage

```
mttf(x, upstates = x$states, level = 0.95, klim = 10000)
```

Arguments

<code>x</code>	An object of S3 class <code>smmfit</code> or <code>smm</code> .
<code>upstates</code>	Vector giving the subset of operational states U .
<code>level</code>	Confidence level of the asymptotic confidence interval. Helpful for an object <code>x</code> of class <code>smmfit</code> .
<code>klim</code>	Optional. The time horizon used to approximate the series in the computation of the mean sojourn times vector m (cf. meanSojournTimes function) for the asymptotic variance.

Details

Consider a system (or a component) S_{system} whose possible states during its evolution in time are $E = \{1, \dots, s\}$. Denote by $U = \{1, \dots, s_1\}$ the subset of operational states of the system (the up states) and by $D = \{s_1 + 1, \dots, s\}$ the subset of failure states (the down states), with $0 < s_1 < s$ (obviously, $E = U \cup D$ and $U \cap D = \emptyset$, $U \neq \emptyset$, $D \neq \emptyset$). One can think of the states of U as different operating modes or performance levels of the system, whereas the states of D can be seen as failures of the systems with different modes.

We are interested in investigating the mean time to failure of a discrete-time semi-Markov system S_{system} . Consequently, we suppose that the evolution in time of the system is governed by an E-state space semi-Markov chain $(Z_k)_{k \in N}$. The system starts to work at instant 0 and the state of the system is given at each instant $k \in N$ by Z_k : the event $\{Z_k = i\}$, for a certain $i \in U$, means that

the system S_{system} is in operating mode i at time k , whereas $\{Z_k = j\}$, for a certain $j \in D$, means that the system is not operational at time k due to the mode of failure j or that the system is under the repairing mode j .

Let T_D denote the first passage time in subset D , called the lifetime of the system, i.e.,

$$T_D := \inf\{n \in N; Z_n \in D\} \text{ and } \inf \emptyset := \infty.$$

The mean time to failure (MTTF) is defined as the mean lifetime, i.e., the expectation of the hitting time to down set D ,

$$MTTF = E[T_D]$$

Value

A matrix with $\text{card}(U) = s_1$ rows, and with columns giving values of the mean time to failure for each state $i \in U$, variances, lower and upper asymptotic confidence limits (if x is an object of class `smmfit`).

References

V. S. Barbu, N. Limnios. (2008). Semi-Markov Chains and Hidden Semi-Markov Models Toward Applications - Their Use in Reliability and DNA Analysis. New York: Lecture Notes in Statistics, vol. 191, Springer.

I. Votsi & A. Brouste (2019) Confidence interval for the mean time to failure in semi-Markov models: an application to wind energy production, Journal of Applied Statistics, 46:10, 1756-1773

mttr

Mean Time To Repair (MTTR) Function

Description

Consider a system S_{system} that has just failed at time $k = 0$. The mean time to repair (MTTR) is defined as the mean of the repair duration.

Usage

```
mttr(x, upstates = x$states, level = 0.95, klim = 10000)
```

Arguments

<code>x</code>	An object of S3 class <code>smmfit</code> or <code>smm</code> .
<code>upstates</code>	Vector giving the subset of operational states U .
<code>level</code>	Confidence level of the asymptotic confidence interval. Helpful for an object <code>x</code> of class <code>smmfit</code> .
<code>klim</code>	Optional. The time horizon used to approximate the series in the computation of the mean sojourn times vector m (cf. meanSojournTimes function) for the asymptotic variance.

Details

Consider a system (or a component) S_{system} whose possible states during its evolution in time are $E = \{1, \dots, s\}$. Denote by $U = \{1, \dots, s_1\}$ the subset of operational states of the system (the up states) and by $D = \{s_1 + 1, \dots, s\}$ the subset of failure states (the down states), with $0 < s_1 < s$ (obviously, $E = U \cup D$ and $U \cap D = \emptyset$, $U \neq \emptyset$, $D \neq \emptyset$). One can think of the states of U as different operating modes or performance levels of the system, whereas the states of D can be seen as failures of the systems with different modes.

We are interested in investigating the mean time to repair of a discrete-time semi-Markov system S_{system} . Consequently, we suppose that the evolution in time of the system is governed by an E-state space semi-Markov chain $(Z_k)_{k \in N}$. The system has just failed at instant 0 and the state of the system is given at each instant $k \in N$ by Z_k : the event $\{Z_k = i\}$, for a certain $i \in U$, means that the system S_{system} is in operating mode i at time k , whereas $\{Z_k = j\}$, for a certain $j \in D$, means that the system is not operational at time k due to the mode of failure j or that the system is under the repairing mode j .

Let T_U denote the first passage time in subset U , called the duration of repair or repair time, i.e.,

$$T_U := \inf\{n \in N; Z_n \in U\} \text{ and } \inf \emptyset := \infty.$$

The mean time to repair (MTTR) is defined as the mean of the repair duration, i.e., the expectation of the hitting time to up set U ,

$$MTTR = E[T_U]$$

Value

A matrix with $\text{card}(U) = s_1$ rows, and with columns giving values of the mean time to repair for each state $i \in U$, variances, lower and upper asymptotic confidence limits (if x is an object of class `smmfit`).

References

V. S. Barbu, N. Limnios. (2008). Semi-Markov Chains and Hidden Semi-Markov Models Toward Applications - Their Use in Reliability and DNA Analysis. New York: Lecture Notes in Statistics, vol. 191, Springer.

I. Votsi & A. Brouste (2019) Confidence interval for the mean time to failure in semi-Markov models: an application to wind energy production, Journal of Applied Statistics, 46:10, 1756-1773

Description

Displays the densities for the conditional sojourn time distributions depending on the current state i and on the next state j .

Usage

```
## S3 method for class 'smm'
plot(x, i, j, klim = NULL, ...)
```

Arguments

x	An object of S3 class <code>smm</code> (inheriting from the S3 class <code>smmnonparametric</code> or <code>smmparametric</code>).
i	An element of the state space vector <code>x\$states</code> giving the current state in the following cases: <code>type.sojourn = "fij"</code> or <code>type.sojourn = "fi"</code> , otherwise, <code>i</code> is ignored.
j	An element of the state space vector <code>x\$states</code> giving the next state in the following cases: <code>type.sojourn = "fij"</code> or <code>type.sojourn = "fj"</code> , otherwise, <code>j</code> is ignored.
klim	An integer giving the limit value for which the density will be plotted. If <code>klim</code> is <code>NULL</code> , then quantile or order 0.95 is used.
...	Arguments passed to <code>plot</code> .

Value

None.

plot.smmfit

Plot function for an object of class smmfit

Description

Displays the densities for the conditional sojourn time distributions depending on the current state `i` and on the next state `j`.

Usage

```
## S3 method for class 'smmfit'
plot(x, i, j, klim = NULL, ...)
```

Arguments

x	An object of class <code>smmfit</code> (inheriting from the S3 classes <code>smm</code> , <code>smmnonparametric</code> or <code>smmparametric</code>).
i	An element of the state space vector <code>x\$states</code> giving the current state in the following cases: <code>type.sojourn = "fij"</code> or <code>type.sojourn = "fi"</code> , otherwise, <code>i</code> is ignored.
j	An element of the state space vector <code>x\$states</code> giving the next state in the following cases: <code>type.sojourn = "fij"</code> or <code>type.sojourn = "fj"</code> , otherwise, <code>j</code> is ignored.

`klim` An integer giving the limit value for which the density will be plotted. If `klim` is NULL, then quantile or order 0.95 is used.

`...` Arguments passed to plot.

Value

None.

References

V. S. Barbu, N. Limnios. (2008). Semi-Markov Chains and Hidden Semi-Markov Models Toward Applications - Their Use in Reliability and DNA Analysis. New York: Lecture Notes in Statistics, vol. 191, Springer.

Examples

```
states <- c("a", "c", "g", "t")
```

reliability *Reliability Function*

Description

Consider a system S_{system} starting to function at time $k = 0$. The reliability or the survival function of S_{system} at time $k \in N$ is the probability that the system has functioned without failure in the period $[0, k]$.

Usage

```
reliability(x, k, upstates = x$states, level = 0.95, klim = 10000)
```

Arguments

`x` An object of S3 class `smmfit` or `smm`.

`k` A positive integer giving the period $[0, k]$ on which the reliability should be computed.

`upstates` Vector giving the subset of operational states U .

`level` Confidence level of the asymptotic confidence interval. Helpful for an object `x` of class `smmfit`.

`klim` Optional. The time horizon used to approximate the series in the computation of the mean sojourn times vector m (cf. [meanSojournTimes](#) function) for the asymptotic variance.

Details

Consider a system (or a component) S_{system} whose possible states during its evolution in time are $E = \{1, \dots, s\}$. Denote by $U = \{1, \dots, s_1\}$ the subset of operational states of the system (the up states) and by $D = \{s_1 + 1, \dots, s\}$ the subset of failure states (the down states), with $0 < s_1 < s$ (obviously, $E = U \cup D$ and $U \cap D = \emptyset$, $U \neq \emptyset$, $D \neq \emptyset$). One can think of the states of U as different operating modes or performance levels of the system, whereas the states of D can be seen as failures of the systems with different modes.

We are interested in investigating the reliability of a discrete-time semi-Markov system S_{system} . Consequently, we suppose that the evolution in time of the system is governed by an E-state space semi-Markov chain $(Z_k)_{k \in N}$. The system starts to work at instant 0 and the state of the system is given at each instant $k \in N$ by Z_k : the event $\{Z_k = i\}$, for a certain $i \in U$, means that the system S_{system} is in operating mode i at time k , whereas $\{Z_k = j\}$, for a certain $j \in D$, means that the system is not operational at time k due to the mode of failure j or that the system is under the repairing mode j .

Let T_D denote the first passage time in subset D , called the lifetime of the system, i.e.,

$$T_D := \inf\{n \in N; Z_n \in D\} \text{ and } \inf \emptyset := \infty.$$

The reliability or the survival function at time $k \in N$ of a discrete-time semi-Markov system is:

$$R(k) := P(T_D > k) = P(Z_n \in U, n = 0, \dots, k)$$

which can be rewritten as follows:

$$R(k) = \sum_{i \in U} P(Z_0 = i)P(T_D > k | Z_0 = i) = \sum_{i \in U} \alpha_i P(T_D > k | Z_0 = i)$$

Value

A matrix with $k + 1$ rows, and with columns giving values of the reliability, variances, lower and upper asymptotic confidence limits (if x is an object of class `smmf it`).

References

V. S. Barbu, N. Limnios. (2008). Semi-Markov Chains and Hidden Semi-Markov Models Toward Applications - Their Use in Reliability and DNA Analysis. New York: Lecture Notes in Statistics, vol. 191, Springer.

setSeed

Set the RNG Seed from within Rcpp

Description

Set the RNG Seed from within Rcpp

Usage

```
setSeed(seed)
```

Arguments

seed An unsigned int that is the seed one wishes to use.

Value

A set RNG scope.

Examples

```
set.seed(10)
x <- rnorm(5, 0, 1)
setSeed(10)
y <- rnorm(5, 0, 1)
all.equal(x, y, check.attributes = FALSE)
```

simulate.mm

Simulates k-th order Markov chains

Description

Simulates k-th order Markov chains.

Usage

```
## S3 method for class 'mm'
simulate(object, nsim = 1, seed = NULL, ...)
```

Arguments

object An object of class [mm](#).

nsim An integer or vector of integers (for multiple sequences) specifying the length of the sequence(s).

seed Optional. seed for the random number generator. If no seed is given, then seed is set by using the command `set.seed(round(as.numeric(Sys.time())))`.

... further arguments passed to or from other methods.

Details

If `nsim` is a single integer then a chain of that length is produced. If `nsim` is a vector of integers, then `length(nsim)` sequences are generated with respective lengths.

Value

A list of vectors representing the sequences.

See Also

[mm](#), [fitmm](#)

Examples

```
states <- c("a", "c", "g", "t")
s <- length(states)
k <- 2
init <- rep.int(1 / s ^ k, s ^ k)
p <- matrix(0.25, nrow = s ^ k, ncol = s)

# Specify a Markov model of order 1
markov <- mm(states = states, init = init, ptrans = p, k = k)

seqs <- simulate(object = markov, nsim = c(1000, 10000, 2000), seed = 150)
```

simulate.mmfit

Simulates Markov chains

Description

Simulates sequences from a fitted Markov model.

Usage

```
## S3 method for class 'mmfit'
simulate(object, nsim = 1, seed = NULL, ...)
```

Arguments

object	An object of class <code>mmfit</code> .
nsim	An integer or vector of integers (for multiple sequences) specifying the length of the sequence(s).
seed	Optional. seed for the random number generator. If no seed is given, then seed is set by using the command <code>set.seed(round(as.numeric(Sys.time())))</code> .
...	further arguments passed to or from other methods.

Details

If `nsim` is a single integer then a chain of that length is produced. If `nsim` is a vector of integers, then `length(nsim)` sequences are generated with respective lengths.

Value

A list of vectors representing the sequences.

See Also

[mm](#), [fitmm](#)

simulate.smm	<i>Simulates semi-Markov chains</i>
--------------	-------------------------------------

Description

Simulates sequences from a semi-Markov model.

Usage

```
## S3 method for class 'smm'
simulate(object, nsim = 1, seed = NULL, ...)
```

Arguments

object	An object of S3 class <code>smm</code> (inheriting from the S3 class smmnonparametric or smmparametric).
nsim	An integer or vector of integers (for multiple sequences) specifying the length of the sequence(s).
seed	Optional. seed for the random number generator. If no seed is given, then seed is set by using the command <code>set.seed(round(as.numeric(Sys.time())))</code> .
...	further arguments passed to or from other methods.

Details

If `nsim` is a single integer then a chain of that length is produced. If `nsim` is a vector of integers, then `length(nsim)` sequences are generated with respective lengths.

Value

A list of vectors representing the sequences.

References

V. S. Barbu, N. Limnios. (2008). *Semi-Markov Chains and Hidden Semi-Markov Models Toward Applications - Their Use in Reliability and DNA Analysis*. New York: Lecture Notes in Statistics, vol. 191, Springer.

See Also

[smmparametric](#), [smmnonparametric](#), [fitsmm](#)

simulate.smmfit *Simulates semi-Markov chains*

Description

Simulates sequences from a fitted semi-Markov model.

Usage

```
## S3 method for class 'smmfit'  
simulate(object, nsim = 1, seed = NULL, ...)
```

Arguments

object	An object of class <code>smmfit</code> (inheriting from the S3 classes <code>smm</code> , smmnonparametric or smmparametric).
nsim	An integer or vector of integers (for multiple sequences) specifying the length of the sequence(s).
seed	seed for the random number generator.
...	further arguments passed to or from other methods.

Details

If `nsim` is a single integer then a chain of that length is produced. If `nsim` is a vector of integers, then `length(nsim)` sequences are generated with respective lengths.

Value

A list of vectors representing the sequences.

References

V. S. Barbu, N. Limnios. (2008). *Semi-Markov Chains and Hidden Semi-Markov Models Toward Applications - Their Use in Reliability and DNA Analysis*. New York: Lecture Notes in Statistics, vol. 191, Springer.

See Also

[smmnonparametric](#), [smmparametric](#), [fitsmm](#)

 smmnonparametric *Non-parametric semi-Markov model specification*

Description

Creates a non-parametric model specification for a semi-Markov model.

Usage

```
smmnonparametric(
  states,
  init,
  ptrans,
  type.sojourn = c("fij", "fi", "fj", "f"),
  distr,
  cens.beg = FALSE,
  cens.end = FALSE
)
```

Arguments

states	Vector of state space of length s .
init	Vector of initial distribution of length s .
ptrans	Matrix of transition probabilities of the embedded Markov chain $J = (J_m)_m$ of dimension (s, s) .
type.sojourn	Type of sojourn time (for more explanations, see Details).
distr	<ul style="list-style-type: none"> • Array of dimension $(s, s, kmax)$ if type.sojourn = "fij"; • Matrix of dimension $(s, kmax)$ if type.sojourn = "fi" or "fj"; • Vector of length $kmax$ if the type.sojourn = "f". $kmax$ is the maximum length of the sojourn times.
cens.beg	Optional. A logical value indicating whether or not sequences are censored at the beginning.
cens.end	Optional. A logical value indicating whether or not sequences are censored at the end.

Details

This function creates a semi-Markov model object in the non-parametric case, taking into account the type of sojourn time and the censoring described in references. The non-parametric specification concerns sojourn time distributions defined by the user.

The difference between the Markov model and the semi-Markov model concerns the modeling of the sojourn time. With a Markov chain, the sojourn time distribution is modeled by a Geometric distribution (in discrete time). With a semi-Markov chain, the sojourn time can be any arbitrary distribution.

We define :

- the semi-Markov kernel $q_{ij}(k) = P(J_{m+1} = j, T_{m+1} - T_m = k | J_m = i)$;
- the transition matrix $(p_{trans}(i, j))_{i, j} \in states$ of the embedded Markov chain $J = (J_m)_m$, $p_{trans}(i, j) = P(J_{m+1} = j | J_m = i)$;
- the initial distribution $\mu_i = P(J_1 = i) = P(Z_1 = i)$, $i \in 1, 2, \dots, s$;
- the conditional sojourn time distributions $(f_{ij}(k))_{i, j} \in states$, $k \in N$, $f_{ij}(k) = P(T_{m+1} - T_m = k | J_m = i, J_{m+1} = j)$, f is specified by the argument `distr` in the non-parametric case.

In this package we can choose different types of sojourn time. Four options are available for the sojourn times:

- depending on the present state and on the next state (f_{ij});
- depending only on the present state (f_i);
- depending only on the next state (f_j);
- depending neither on the current, nor on the next state (f).

Let define $kmax$ the maximum length of the sojourn times. If `type.sojourn = "fij"`, `distr` is an array of dimension $(s, s, kmax)$. If `type.sojourn = "fi"` or `"fj"`, `distr` must be a matrix of dimension $(s, kmax)$. If `type.sojourn = "f"`, `distr` must be a vector of length $kmax$.

If the sequence is censored at the beginning and/or at the end, `cens.beg` must be equal to `TRUE` and/or `cens.end` must be equal to `TRUE`. All the sequences must be censored in the same way.

Value

Returns an object of class `smm`, [smmnonparametric](#).

References

V. S. Barbu, N. Limnios. (2008). Semi-Markov Chains and Hidden Semi-Markov Models Toward Applications - Their Use in Reliability and DNA Analysis. New York: Lecture Notes in Statistics, vol. 191, Springer.

See Also

[simulate](#), [fitsmm](#), [smmparametric](#)

Examples

```
states <- c("a", "c", "g", "t")
s <- length(states)

# Creation of the initial distribution
vect.init <- c(1 / 4, 1 / 4, 1 / 4, 1 / 4)

# Creation of the transition matrix
pij <- matrix(c(0, 0.2, 0.5, 0.3,
               0.2, 0, 0.3, 0.5,
               0.3, 0.5, 0, 0.2,
               0.4, 0.2, 0.4, 0),
              ncol = s, byrow = TRUE)
```

```

# Creation of a matrix corresponding to the
# conditional sojourn time distributions
kmax <- 6
nparam.matrix <- matrix(c(0.2, 0.1, 0.3, 0.2,
                          0.2, 0, 0.4, 0.2,
                          0.1, 0, 0.2, 0.1,
                          0.5, 0.3, 0.15, 0.05,
                          0, 0, 0.3, 0.2,
                          0.1, 0.2, 0.2, 0),
                        nrow = s, ncol = kmax, byrow = TRUE)

semimarkov <- smmnonparametric(states = states, init = vect.init, ptrans = pij,
                              type.sojourn = "fj", distr = nparam.matrix)

semimarkov

```

smmparametric *Parametric semi-Markov model specification*

Description

Creates a parametric model specification for a semi-Markov model.

Usage

```

smmparametric(
  states,
  init,
  ptrans,
  type.sojourn = c("fij", "fi", "fj", "f"),
  distr,
  param,
  cens.beg = FALSE,
  cens.end = FALSE
)

```

Arguments

states	Vector of state space of length s .
init	Vector of initial distribution of length s .
ptrans	Matrix of transition probabilities of the embedded Markov chain $J = (J_m)_m$ of dimension (s, s) .
type.sojourn	Type of sojourn time (for more explanations, see Details).
distr	<ul style="list-style-type: none"> Matrix of distributions of dimension (s, s) if type.sojourn = "fij"; Vector of distributions of length s if type.sojourn = "fi" or "fj";

- A distribution if `type.sojourn = "f"`.

where the distributions to be used can be one of `unif`, `geom`, `pois`, `dweibull` or `nbinom`.

<code>param</code>	<p>Parameters of sojourn time distributions:</p> <ul style="list-style-type: none"> • Array of distribution parameters of dimension $(s, s, 2)$ (2 corresponds to the maximal number of distribution parameters) if <code>type.sojourn = "fij"</code>; • Matrix of distribution parameters of dimension $(s, 2)$ if <code>type.sojourn = "fi"</code> or <code>"fj"</code>; • Vector of distribution parameters of length 2 if <code>type.sojourn = "f"</code>. <p>When parameters/values are not necessary (e.g. the Poisson distribution has only one parameter that is λ, leave the value NA for the second parameter in the argument <code>param</code>).</p>
<code>cens.beg</code>	Optional. A logical value indicating whether or not sequences are censored at the beginning.
<code>cens.end</code>	Optional. A logical value indicating whether or not sequences are censored at the end.

Details

This function creates a semi-Markov model object in the parametric case, taking into account the type of sojourn time and the censoring described in references. For the parametric specification, several discrete distributions are considered (see below).

The difference between the Markov model and the semi-Markov model concerns the modeling of the sojourn time. With a Markov chain, the sojourn time distribution is modeled by a Geometric distribution (in discrete time). With a semi-Markov chain, the sojourn time can be any arbitrary distribution. In this package, the available distribution for a semi-Markov model are :

- Uniform: $f(x) = 1/n$ for $a \leq x \leq b$, with $n = b - a + 1$;
- Geometric: $f(x) = \theta(1 - \theta)^x$ for $x = 0, 1, 2, \dots, n$, $0 < \theta < 1$, with $n > 0$ and θ is the probability of success;
- Poisson: $f(x) = (\lambda^x \exp(-\lambda))/x!$ for $x = 0, 1, 2, \dots, n$, with $n > 0$ and $\lambda > 0$;
- Discrete Weibull of type 1: $f(x) = q^{(x-1)^\beta} - q^{x^\beta}$, $x = 1, 2, 3, \dots, n$, with $n > 0$, q is the first parameter and β is the second parameter;
- Negative binomial: $f(x) = \frac{\Gamma(x+\alpha)}{\Gamma(\alpha)x!} p^\alpha (1-p)^x$, for $x = 0, 1, 2, \dots, n$, Γ is the Gamma function, α is the parameter of overdispersion and p is the probability of success, $0 < p < 1$;
- Non-parametric.

We define :

- the semi-Markov kernel $q_{ij}(k) = P(J_{m+1} = j, T_{m+1} - T_m = k | J_m = i)$;
- the transition matrix $(p_{trans}(i, j))_{i, j} \in states$ of the embedded Markov chain $J = (J_m)_m$, $p_{trans}(i, j) = P(J_{m+1} = j | J_m = i)$;
- the initial distribution $\mu_i = P(J_1 = i) = P(Z_1 = i)$, $i \in 1, 2, \dots, s$;
- the conditional sojourn time distributions $(f_{ij}(k))_{i, j} \in states$, $k \in N$, $f_{ij}(k) = P(T_{m+1} - T_m = k | J_m = i, J_{m+1} = j)$, f is specified by the argument `param` in the parametric case.

In this package we can choose different types of sojourn time. Four options are available for the sojourn times:

- depending on the present state and on the next state (f_{ij});
- depending only on the present state (f_i);
- depending only on the next state (f_j);
- depending neither on the current, nor on the next state (f).

If `type.sojourn = "fij"`, `distr` is a matrix of dimension (s, s) (e.g., if the row 1 of the 2nd column is "pois", that is to say we go from the first state to the second state following a Poisson distribution). If `type.sojourn = "fi"` or `"fj"`, `distr` must be a vector (e.g., if the first element of vector is "geom", that is to say we go from the first state to any state according to a Geometric distribution). If `type.sojourn = "f"`, `distr` must be one of "unif", "geom", "pois", "dweibull", "nbinom" (e.g., if `distr` is equal to "nbinom", that is to say that the sojourn times when going from any state to any state follows a Negative Binomial distribution). For the non-parametric case, `distr` is equal to "nonparametric" whatever type of sojourn time given.

If the sequence is censored at the beginning and/or at the end, `cens.beg` must be equal to TRUE and/or `cens.end` must be equal to TRUE. All the sequences must be censored in the same way.

Value

Returns an object of class [smmparametric](#).

References

V. S. Barbu, N. Limnios. (2008). Semi-Markov Chains and Hidden Semi-Markov Models Toward Applications - Their Use in Reliability and DNA Analysis. New York: Lecture Notes in Statistics, vol. 191, Springer.

See Also

[simulate](#), [fitsmm](#), [smmnonparametric](#)

Examples

```
states <- c("a", "c", "g", "t")
s <- length(states)

# Creation of the initial distribution
vect.init <- c(1 / 4, 1 / 4, 1 / 4, 1 / 4)

# Creation of the transition matrix
pij <- matrix(c(0, 0.2, 0.5, 0.3,
               0.2, 0, 0.3, 0.5,
               0.3, 0.5, 0, 0.2,
               0.4, 0.2, 0.4, 0),
              ncol = s, byrow = TRUE)

# Creation of the distribution matrix
```

```
distr.matrix <- matrix(c(NA, "pois", "geom", "nbinom",  
                        "geom", NA, "pois", "dweibull",  
                        "pois", "pois", NA, "geom",  
                        "pois", "geom", "geom", NA),  
                      nrow = s, ncol = s, byrow = TRUE)  
  
# Creation of an array containing the parameters  
param1.matrix <- matrix(c(NA, 2, 0.4, 4,  
                          0.7, NA, 5, 0.6,  
                          2, 3, NA, 0.6,  
                          4, 0.3, 0.4, NA),  
                        nrow = s, ncol = s, byrow = TRUE)  
  
param2.matrix <- matrix(c(NA, NA, NA, 0.6,  
                          NA, NA, NA, 0.8,  
                          NA, NA, NA, NA,  
                          NA, NA, NA, NA),  
                        nrow = s, ncol = s, byrow = TRUE)  
  
param.array <- array(c(param1.matrix, param2.matrix), c(s, s, 2))  
  
# Specify the semi-Markov model  
semimarkov <- smmparametric(states = states, init = vect.init, ptrans = pij,  
                            type.sojourn = "fij", distr = distr.matrix,  
                            param = param.array)  
  
semimarkov
```

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