

Package ‘TUvalues’

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Type Package

Title Tools for Calculating Allocations in Game Theory using Exact and Approximated Methods

Version 1.0.0

Description The main objective of cooperative games is to allocate a good among the agents involved. This package includes the most well-known allocation rules, i.e., the Shapley value, the Banzhaf value, the egalitarian rule, and the equal surplus division value. In addition, it considers the point of view of a priori unions (situations in which agents can form coalitions). For this purpose, the package includes the Owen value, the Banzhaf-Owen value, and the corresponding extensions of the egalitarian rules. All these values can be calculated exactly or estimated by sampling.

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Encoding UTF-8

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URL <https://github.com/mariaguilleng/TUvalues>

BugReports <https://github.com/mariaguilleng/TUvalues/issues>

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| | |
|---------|----------------------|
| banzhaf | <i>Banzhaf value</i> |
|---------|----------------------|

Description

Calculate the Banzhaf value

Usage

```
banzhaf(
  characteristic_func,
  method = "exact",
  n_rep = 10000,
  n_players = 0,
  replace = FALSE
)
```

Arguments

| | |
|---------------------|--|
| characteristic_func | The valued function defined on the subsets of the number of players. |
| method | Method used to calculate the Banzhaf value. Valid methods are: exact for the exact calculation or appro for approximated polynomial calculation based on sampling. |
| n_rep | Only used if method is appro. The number of iterations to perform in the approximated calculation |
| n_players | Only used if characteristic_func is a function. The number of players in the game. |
| replace | should sampling be with replacement? |

Value

The Banzhaf value for each player

Examples

```
n <- 8
v <- function(coalition) {
  if (length(coalition) > n/2) {
    return(1)
  } else {
    return(0)
  }
}
banzhaf(v, method = "exact", n_players = n)
banzhaf(v, method = "appro", n_rep = 2000, n_players = n, replace = TRUE)

v<-c(0,0,0,1,2,1,3)
banzhaf(v, method = "exact")
banzhaf(v, method = "appro", n_rep = 2000, replace = TRUE)
```

banzhaf_appro

Banzhaf Index (approximated)

Description

Calculate the approximated Banzhaf Index based on sampling

Usage

```
banzhaf_appro(characteristic_func, n_players, n_rep, replace = TRUE)
```

Arguments

| | |
|---------------------|---|
| characteristic_func | The valued function defined on the subsets of the number of players |
| n_players | The number of players |
| n_rep | The number of iterations to perform in the approximated calculation |
| replace | should sampling be with replacement? |

Value

The Shapley value for each player

| | |
|---------------|------------------------------|
| banzhaf_exact | <i>Banzhaf Index (exact)</i> |
|---------------|------------------------------|

Description

Calculate the approximated Banzhaf Index

Usage

```
banzhaf_exact(characteristic_func, n_players)
```

Arguments

| | |
|---------------------|---|
| characteristic_func | The valued function defined on the subsets of the number of players |
| n_players | The number of players in the game. |

Value

The Banzhaf Index for each player

| | |
|--------------|---------------------------|
| banzhaf_owen | <i>Banzhaf-Owen value</i> |
|--------------|---------------------------|

Description

Calculate the Banzhaf-Owen value

Usage

```
banzhaf_owen(  
  characteristic_func,  
  union,  
  method = "exact",  
  n_rep = 10000,  
  n_players = 0,  
  replace = TRUE  
)
```

Arguments

| | |
|---------------------|---|
| characteristic_func | The valued function defined on the subsets of the number of players |
| union | List of vectors indicating the a priori unions between the players |
| method | Method used to calculate the Owen value. Valid methods are: exact for the exact calculation or appro for approximated polynomial calculation based on sampling. |
| n_rep | Only used if method is appro. The number of iterations to perform in the approximated calculation |
| n_players | Only used if characteristic_func is a function. The number of players in the game. |
| replace | should sampling be with replacement? |

Value

The Banzhaf-Owen value for each player

Examples

```
characteristic_func <- c(0,0,0,0,30,30,40,40,50,50,60,70,80,90,100)
union <- list(c(1,3),c(2),c(4))
banzhaf_owen(characteristic_func, union)
banzhaf_owen(characteristic_func, union, method = "appro", n_rep = 4000)
```

banzhaf_owen_appro *Banzhaf-Owen Value*

Description

Calculate the approximated Banzhaf-Owen value

Usage

```
banzhaf_owen_appro(characteristic_func, union, n_players, n_rep, replace)
```

Arguments

| | |
|---------------------|--|
| characteristic_func | The valued function defined on the subsets of the number of players |
| union | List of vectors indicating the a priori unions between the players |
| n_players | The number of players |
| n_rep | Only used if method is appro. The number of iterations to perform in the approximated calculation. |
| replace | should sampling be with replacement? |

Value

The Banzhaf-Owen Index for each player

| | |
|--------------------|---------------------------|
| banzhaf_owen_exact | <i>Banzhaf-Owen Value</i> |
|--------------------|---------------------------|

Description

Calculate the approximated Banzhaf-Owen value

Usage

```
banzhaf_owen_exact(characteristic_func, union, n_players)
```

Arguments

| | |
|---------------------|---|
| characteristic_func | The valued function defined on the subsets of the number of players |
| union | List of vectors indicating the a priori unions between the players |
| n_players | The number of players in the game. |

Value

The Banzhaf Index for each player

| | |
|------------|-------------------|
| coalitions | <i>coalitions</i> |
|------------|-------------------|

Description

Create all the possible coalitions given the number of players

Usage

```
coalitions(n_players)
```

Arguments

| | |
|-----------|-------------------|
| n_players | Number of players |
|-----------|-------------------|

Value

A list containing a data.frame of the binary representation of the coalitions and a vector of the classical representation (as sets) of the coalitions

| | |
|-------------|--------------------------|
| egalitarian | <i>Egalitarian value</i> |
|-------------|--------------------------|

Description

Calculate the egalitarian value

Usage

```
egalitarian(characteristic_func, n_players = 0)
```

Arguments

| | |
|---------------------|--|
| characteristic_func | The valued function defined on the subsets of the number of players |
| n_players | Only used if characteristic_func is a function. The number of players in the game. |

Value

The egalitarian value for each player

Examples

```
n <- 10
v <- function(coalition) {
  if (length(coalition) > n/2) {
    return(1)
  } else {
    return(0)
  }
}
egalitarian(v,n)
```

| | |
|------------------------|-------------------------------------|
| equal_surplus_division | <i>Equal Surplus Division value</i> |
|------------------------|-------------------------------------|

Description

Calculate the equal surplus division value

Usage

```
equal_surplus_division(characteristic_func, n_players = 0)
```

Arguments

| | |
|---------------------|--|
| characteristic_func | The valued function defined on the subsets of the number of players |
| n_players | Only used if characteristic_func is a function. The number of players in the game. |

Value

The equal surplus division value for each player

Examples

```
n <- 10
v <- function(coalition) {
  if (length(coalition) > n/2) {
    return(1)
  } else {
    return(0)
  }
}
equal_surplus_division(v,n)
```

owen

Owen value

Description

Calculate the Owen value

Usage

```
owen(
  characteristic_func,
  union,
  method = "exact",
  n_rep = 10000,
  n_players = 0
)
```

Arguments

| | |
|---------------------|---|
| characteristic_func | The valued function defined on the subsets of the number of players. |
| union | List of vectors indicating the a priori unions between the players. |
| method | Method used to calculate the Owen value. Valid methods are: exact for the exact calculation or appro for approximated polynomial calculation based on sampling. |

`n_rep` Only used if method is appro. The number of iterations to perform in the approximated calculation.

`n_players` The number of players in the game.

Value

The Owen value for each player.

Examples

```
n <- 10
v <- function(coalition) {
  if (length(coalition) > n/2) {
    return(1)
  } else {
    return(0)
  }
}
u <- lapply(1:(n/2), function(i) c(2*i - 1, 2*i))
owen(v, union = u, method = "appro", n_rep = 4000, n_players = n)

characteristic_func <- c(1,1,2,1,2,2,2)
union <- list(c(1,2),c(3))
owen(characteristic_func, union)
owen(characteristic_func, union, method = "appro", n_rep = 4000)
```

| | |
|-------------------------|-----------------------------------|
| <code>owen_appro</code> | <i>Owen value (approximation)</i> |
|-------------------------|-----------------------------------|

Description

Calculate the approximated Owen value based on sampling

Usage

```
owen_appro(characteristic_func, union, n_players, n_rep)
```

Arguments

`characteristic_func` The valued function defined on the subsets of the number of players

`union` List of vectors indicating the a priori unions between the players

`n_players` The number of players

`n_rep` The number of iterations to perform in the approximated calculation

Value

The Owen value for each player

| | |
|------------|---------------------------|
| owen_exact | <i>Owen value (exact)</i> |
|------------|---------------------------|

Description

Calculate the exact Owen

Usage

```
owen_exact(characteristic_func, union, n_players = NULL)
```

Arguments

| | |
|---------------------|---|
| characteristic_func | The valued function defined on the subsets of the number of players |
| union | List of vectors indicating the a priori unions between the players |
| n_players | The number of players |

Value

The Owen value for each player

| | |
|-------------|--------------------|
| predecessor | <i>Predecessor</i> |
|-------------|--------------------|

Description

Given a permutation σ of players and a player i , calculate the set of predecessors of the player i in the order σ

Usage

```
predecessor(permutation, player, include_player = FALSE)
```

Arguments

| | |
|----------------|--|
| permutation | A permutation of the players |
| player | Number of the player i |
| include_player | Whether the player i is included as predecessor of itself or not |

Value

The set of predecessors of the player i in the order σ

| | |
|---------|----------------------|
| shapley | <i>Shapley value</i> |
|---------|----------------------|

Description

Calculate the Shapley value

Usage

```
shapley(characteristic_func, method = "exact", n_rep = 10000, n_players = 0)
```

Arguments

| | |
|---------------------|--|
| characteristic_func | The valued function defined on the subsets of the number of players. |
| method | Method used to calculate the Shapley value. Valid methods are: exact for the exact calculation or appro for approximated polynomial calculation based on sampling. |
| n_rep | Only used if method is appro. The number of iterations to perform in the approximated calculation. |
| n_players | Only used if characteristic_func is a function. The number of players in the game. |

Value

The Shapley value for each player.

Examples

```
n <- 10
v <- function(coalition) {
  if (length(coalition) > n/2) {
    return(1)
  } else {
    return(0)
  }
}
shapley(v, method = "appro", n_rep = 4000, n_players = n)

n <- 3
v <- c(1,1,2,1,2,2,2)
shapley(v, method = "exact")
shapley(v, method = "appro", n_rep = 4000)
```

| | |
|---------------|--------------------------------------|
| shapley_appro | <i>Shapley value (approximation)</i> |
|---------------|--------------------------------------|

Description

Calculate the approximated Shapley value based on sampling

Usage

```
shapley_appro(characteristic_func, n_players, n_rep)
```

Arguments

| | |
|---------------------|---|
| characteristic_func | The valued function defined on the subsets of the number of players |
| n_players | The number of players |
| n_rep | The number of iterations to perform in the approximated calculation |

Value

The Shapley value for each player

| | |
|---------------|------------------------------|
| shapley_exact | <i>Shapley value (exact)</i> |
|---------------|------------------------------|

Description

Calculate the exact Shapley value

Usage

```
shapley_exact(characteristic_func, n_players)
```

Arguments

| | |
|---------------------|---|
| characteristic_func | The valued function defined on the subsets of the number of players |
| n_players | The number of players |

Value

The Shapley value for each player

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